

On the fragility of $\text{Cu}_{47}\text{Ti}_{33}\text{Zr}_{11}\text{Ni}_8\text{Si}_1$ metallic glass

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Abstract

This study reports on calorimetric measurements of the glass transition at various heating rates stretching over three orders of magnitude for $\text{Cu}_{47}\text{Ti}_{33}\text{Zr}_{11}\text{Ni}_8\text{Si}_1$ metallic glass powders synthesized by gas-atomization and subjected to varying thermal treatments. A Vogel–Fulcher–Tammann-type relation was fitted to the data recorded for the heating rate dependent shift of the glass transition. The fragility of the alloy is evaluated in terms of the fragility parameter. Its value is 44 for the as-prepared $\text{Cu}_{47}\text{Ti}_{33}\text{Zr}_{11}\text{Ni}_8\text{Si}_1$ metallic glass powder and decreases with increasing annealing treatment temperature. The decrease in the fragility parameter is due to partial crystallization, which shifts the composition of the remaining supercooled liquid to that of a strong glass-forming alloy.

1. Introduction

The discovery of improved physical and mechanical properties of multicomponent metallic glasses has led to increased research in this area [1–5]. The possibility of preparing metallic glasses at cooling rates as low as $1\text{--}100\text{ K s}^{-1}$ has generated a lot of attention because this enables these alloys to be manufactured not only in the form of ribbons, but also in the form of bulk materials, known as bulk metallic glasses (BMGs) [2–5]. To further develop this possibility, a greater understanding of the glass-forming ability (GFA) of these systems is essential. GFA can be defined as the ease with which the melt of a metallic material can vitrify and is conventionally evaluated in terms of the critical cooling rate (R_c), defined as the minimum cooling rate necessary for freezing the melt into a glass without any precipitation of crystals during solidification [6]. The smaller the R_c , the higher the GFA of a system should be. However, R_c is a parameter that is difficult to measure precisely. As a result, numerous criteria have been

proposed to reflect the GFA of different BMGs on the basis of characteristic temperatures measured by differential scanning calorimetry (DSC) and/or differential thermal analysis [7]. The most widely used criteria are the reduced glass transition criterion proposed by Spaepen and Turnbull [8], T_{rg} , defined as the ratio of the glass transition temperature (T_g) and the liquidus temperature (T_l), as well as the concept of using the width of the supercooled liquid region, ΔT , defined as the temperature difference between the onset glass transition temperature, T_g , and the onset crystallization temperature, T_x [4]. It has been proposed that the larger the ΔT and/or T_{rg} , the lower is the critical cooling rate and hence higher the GFA [4]. However, this is not always true, since there are many notable exceptions to this rule. For example, in the case of Zr–Ti–Cu–Ni–Be alloys it has been found that the compositions with the largest ΔT are the poorest glass formers in the system [9]. On the other hand, it was found that the T_{rg} ratio relates well with the GFA in the Zr–Ti–Cu–Ni–Be system [9]. In contrast, the GFA in the case of Pd–Ni–Fe–P [10], Fe–(Co,Cr,Mo,Ga,Sb)–P–B–C [11] as well as $\text{Mg}_{65}\text{Cu}_{15}\text{Y}_{10}\text{M}_{10}$ ($M = \text{Ni, Al, Zn, Mn}$) [12] alloy

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systems is better explained on the basis of the ΔT values rather than the T_{rg} values. Although the ΔT as well as T_{rg} are the most widely used parameters there have been numerous other parameters developed over the years, which have been used to reflect the GFA in metallic alloys [7, 13–18]. However, to date, there exists no single unified criterion, which can explain the GFA effectively.

One of the pioneering works for evaluating the GFA of supercooled liquids is the concept of fragility, as introduced by Angell [19, 20]. According to this concept, glass-forming liquids can be classified into three general categories, i.e. strong glass formers, which show an Arrhenius behaviour in the Angell plot, fragile glass formers in which the temperature dependence of the viscosity is of non-Arrhenius type but can be fitted by a Vogel–Fulcher–Tammann (VFT) type relation, as described later in the section 3, and intermediate glass formers, which lie between the strong and the fragile glass formers [20]. The fragility (Angell) plots are conventionally evaluated on the basis of viscosity data [20]. However, it has been shown that the heating rate dependence of T_g as measured in a DSC cell can also adequately be used to describe the fragility [21, 22]. There have been numerous reports where the GFA of metallic glasses has been analyzed in terms of the fragility concept using calorimetric data. These reports deal with Mg-base [22, 23], Fe-base [24, 25], Co-base [26], Pr-base [27], Ti-base [28], Zr-base [29] and Nb–Ni [29] metallic glasses. But so far there have been only a few investigations on the fragility of Cu-base metallic glasses [30, 31].

Cu-base BMGs have been found in Cu–Ti–Zr–Ni [32], Cu–Ti–Zr–Si–B [33], Cu–Ti–Zr–Ni–Sn [34], Cu–Zr/Hf–Ti [35], Cu–Ti–Zr–Nb–Ni–Si [36], Cu–Zr–Al [37], Cu–Zr [38–40], Cu–Zr–Ag [41] as well as in the Cu–Ni–Ag–Zr–Ti [18] system recently and have attracted much interest because of their good GFA as well as mechanical properties. Of particular interest is the $\text{Cu}_{47}\text{Ti}_{33}\text{Zr}_{11}\text{Ni}_8\text{Si}_1$ alloy. This alloy composition has an excellent GFA as manifested by an extended supercooled liquid region of 62 K and an estimated R_c on the order of 70 K s^{-1} [42, 43]. The addition of 1 at.% Si to the $\text{Cu}_{47}\text{Ti}_{34}\text{Zr}_{11}\text{Ni}_8$ base alloy is beneficial in increasing the GFA [42]. The very fact that there are numerous reports on the formation of $\text{Cu}_{47}\text{Ti}_{33}\text{Zr}_{11}\text{Ni}_8\text{Si}_1$ glass, albeit with contrasting results [42–44], suggests that it is a rather well-studied system. However, there are no reports on the fragility of this metallic glass. A previous study on the fragility of the very similar $\text{Cu}_{47}\text{Ti}_{34}\text{Zr}_{11}\text{Ni}_8$ BMG based on viscosity data showed that the fragility parameter is 59 [30, 45]. On the other hand, Tang *et al* reported a fragility parameter of 62 for the binary $\text{Cu}_{50}\text{Zr}_{50}$ BMG based on DSC measurements [31]. It has been shown that the fragility parameter is a good indicator of the GFA of glass-forming liquids and the smaller the fragility parameter the lower is the R_c [30].

In this paper, the fragility of the $\text{Cu}_{47}\text{Ti}_{33}\text{Zr}_{11}\text{Ni}_8\text{Si}_1$ glassy powders synthesized by gas atomization has been studied using DSC. After determining T_g from isochronal DSC scans, the data were fitted with a VFT-type relation and the fragility parameter was calculated. Additionally, the influence of isothermal treatment on the fragility of the glass/supercooled liquid is also studied and compared with that in the as-prepared state.

2. Experimental methods

$\text{Cu}_{47}\text{Ti}_{33}\text{Zr}_{11}\text{Ni}_8\text{Si}_1$ powders were produced by high pressure Ar gas atomization at a dynamic pressure of 2.8 MPa after heating a pre-alloy to 1623 K using a close coupled annular nozzle having a melt delivery inner diameter of 3.2 mm at Ames Laboratory [46]. The purity of the starting elements used to prepare the prealloy ranged from 99.9% to 99.999%. The size of the powder particles used in the present study is 45–53 μm . To investigate the effect of isothermal annealing, the as-atomized metallic glass powder (referred to as alloy A) was annealed at 688 K for 60 min (referred to as alloy B) and at 723 K for 30 min (referred to as alloy C). The isothermal annealing of the powder samples was done in a vacuum furnace operated at $1 \cdot 10^{-3}$ bar. Structural characterization was carried out by x-ray diffraction (XRD) measurements. The XRD patterns were recorded at room temperature using a Philips x-ray diffractometer with Co K_α radiation ($\lambda = 0.179 \text{ nm}$). Thermal analysis of the powders was done with a Perkin–Elmer Diamond DSC differential scanning calorimeter (DSC) under flowing argon atmosphere at constant heating rates ranging from 0.08 to 3.33 K s^{-1} . The calorimeter was calibrated for each heating rate using the melting transition of indium and zinc standards in order to account for the temperature shift on changing heating rates. A second run on each specimen was directly carried out after the first cycle without changing the conditions of the measurement to construct a baseline. Additionally, in case of alloy A, the powders were initially heated to 703 K at 0.66 K s^{-1} and cooled at 1.66 K s^{-1} in order to achieve a relaxed state prior to thermal analysis. The onset values of the glass transition, T_g , as well as the onset value of first crystallization event, T_x , were determined directly from the DSC curves. T_g was defined as the point of intersection between the linearly extrapolated curve below the transition with the steepest tangent of the rise in the heat flow signal [21]. Microstructural characterization of the atomized powders was accomplished by transmission electron microscopy (TEM) investigations, which were performed on ion-milled powder samples using a JEOL 2000 FX TEM operated at 200 kV.

3. Results

3.1. Structural and microstructural characterization

Figure 1 shows the XRD patterns of the $\text{Cu}_{47}\text{Ti}_{33}\text{Zr}_{11}\text{Ni}_8\text{Si}_1$ powder in the as-atomized condition as well as after different annealing treatments. The pattern for the as-prepared powder (alloy A) only consists of broad diffraction maxima, which are characteristic for an amorphous phase. The XRD pattern for the powders annealed for 60 min at 688 K (alloy B) as well as that for the alloy annealed at 723 K for 30 min (alloy C) also exhibit no visible crystalline reflections within the sensitivity limits of XRD. The scattering vector, defined as $Q_p = 4\pi \sin \theta_{\text{max}} / \lambda$ (θ_{max} corresponding to the diffraction angle of the first amorphous maximum and λ being the wavelength of the Co K_α radiation), calculated by fitting the first broad peak at $2\theta \approx 45^\circ$ (shown in figure 1) using Gauss line profiles, is $29 \pm 0.02 \text{ nm}^{-1}$ in all cases. Although the Q_p value suggests a very similar short-range order for all the alloys there is a reduction in the peak width at half maximum (FWHM). The

FWHM decreases by a factor of 15% from the as-prepared state (alloy A) to the sample annealed at 723 K for 30 min (alloy C).

In order to study the possible microstructural alterations caused by annealing, TEM characterization was done for all the powders. Figure 2(a) shows a characteristic bright field TEM image and the corresponding selected area diffraction (SAD) pattern for alloy A. The bright field image shows no contrast resembling crystalline structures and the SAD pattern shows diffuse halo rings, i.e. characteristic features of an amorphous structure. In the case of alloy B (figure 2(b)), the bright field image exhibits an uneven contrast and the first diffuse amorphous halo becomes much narrower as compared with the diffraction pattern of alloy A (figure 2(a)). The second ring is more pronounced and a third very faint ring appears.

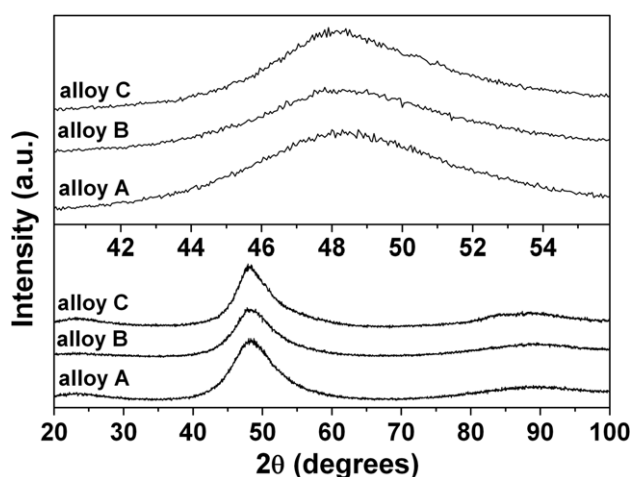


Figure 1. XRD patterns of $\text{Cu}_{47}\text{Ti}_{33}\text{Zr}_{11}\text{Ni}_8\text{Si}_1$ powders in the as-prepared state (alloy A), after isothermal treatment at 688 K for 60 min (alloy B) and after isothermal treatment at 723 K for 30 min (alloy C).

The microstructure of alloy C is displayed in figure 2(c). The bright field image clearly reveals the presence of 5–15 nm sized nanocrystals in an amorphous matrix. The SAD pattern exhibits spots with varying intensity and size. In addition, a broad but faint halo can be observed that overlaps with the inner rings. Identification of the crystallographic structure of the nanocrystals was not possible.

3.2. Thermal analysis

Figure 3 shows a typical DSC trace scanned at a heating rate of 0.66 K s^{-1} for the different powders. For all the alloys A–C, the scans show an endothermic heat effect due to the glass transition followed by a wide supercooled liquid region before crystallization. The crystallization proceeds via two exothermic peaks in case of alloys A and B while there is only one exothermic peak for alloy C. The onset T_g and onset T_x values for alloy A are 700 K and 762 K while those for alloy B are 703 K and 754 K, respectively. The width of the supercooled liquid region ($\Delta T = T_x - T_g$), is 62 K and 51 K for alloy A and alloy B, respectively. In the case of alloy C, T_g is 689 K and T_x is 781 K, resulting in a ΔT value of 92 K. It has to be noted that these values are measured at a heating rate of 0.66 K s^{-1} . The heating rate dependence of the characteristic temperatures reflects the kinetic mechanisms of the structural relaxation and the phase transformation in the glasses/supercooled liquids and these processes can be evaluated in terms of the fragility of supercooled liquids [19–21]. The fragility can be determined from the heating rate dependence of the calorimetric glass transition because the viscosity relaxation and the glass transition measured by calorimetry occur on the same time scale [47]. Hence, the fragility values of the alloys reflect the sensitivity of the liquid to temperature changes. Figure 4 shows the variation of the DSC traces at various heating rates for all the alloys. A distinct glass transition can be found at all heating rates.

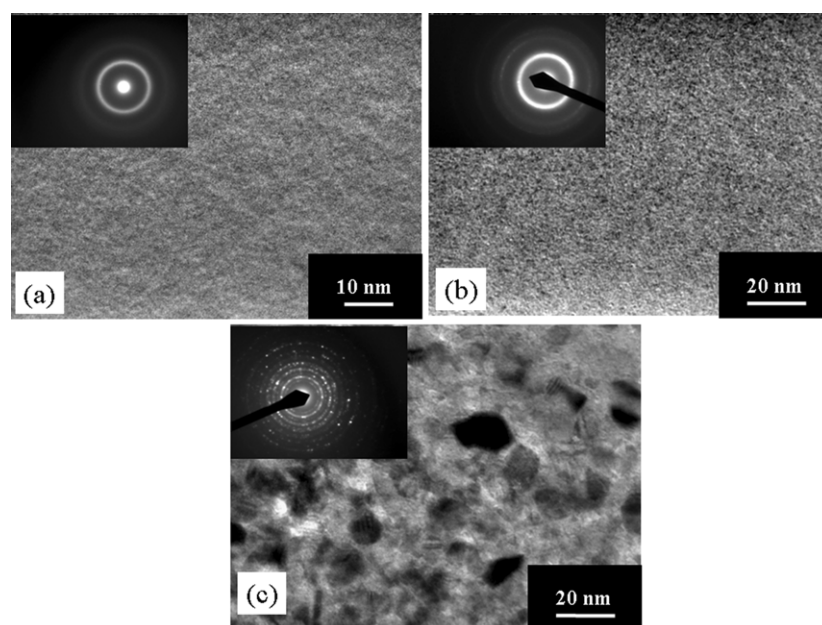


Figure 2. Bright-field TEM micrographs and SAD patterns (shown as inset) for the as-prepared and thermally treated $\text{Cu}_{47}\text{Ti}_{33}\text{Zr}_{11}\text{Ni}_8\text{Si}_1$ powders.

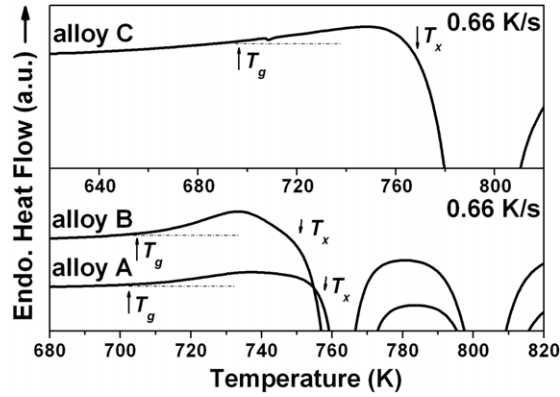


Figure 3. DSC traces (0.66 K s⁻¹) for Cu₄₇Ti₃₃Zr₁₁Ni₈Si₁ powders for alloys A, B and C.

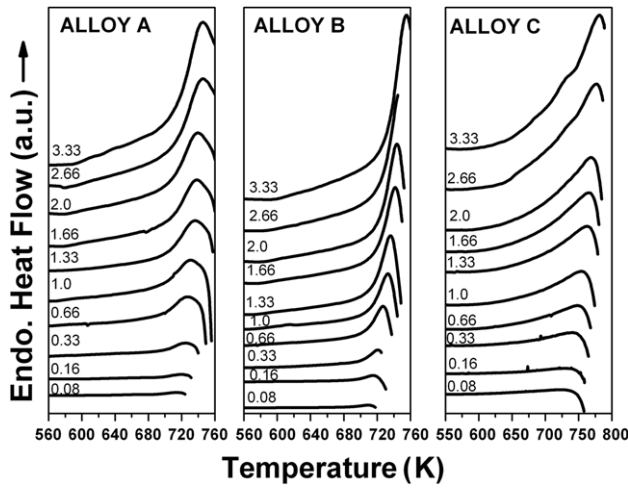


Figure 4. Isochronal DSC plots for all the alloys.

The dependence of the glass transition temperature, T_g , on the heating rate, β , was evaluated in terms of the VFT equation written in the form [21]

$$\beta(T_g) = B \exp[DT_g^0/(T_g^0 - T_g)]. \quad (1)$$

Here, T_g^0 is the asymptotic value of T_g , which is usually approximated as the onset of the glass transition at the limit of infinitely slow cooling, B has the dimension of a heating rate and D is the strength parameter. For the data analysis, the T_g corresponding to each heating rate (0.08–3.33 K s⁻¹) was evaluated from the DSC scans recorded at these heating rates for all the alloys. The fitting of the experimental data was done using the equation

$$\ln \beta(T_g) = \ln B - \frac{DT_g^0}{(T_g - T_g^0)} \quad (2)$$

with three adjustable VFT parameters, B , D and T_g^0 . The calculated values are given in table 1 and the best fits are shown by lines in figure 5. All the fit parameters show a decrease in magnitude with increasing annealing treatment. Generally, the fragility can be classified in terms of the strength parameter, D (as in (2)) or by the fragility parameter (m) defined as [48]

$$m = \left. \frac{d \log(\tau)}{d(T_g/T)} \right|_{T=T_g}, \quad (3)$$

Table 1. Thermal stability data and VFT parameters for the best fit of the DSC data according to equation (2). $T_{g,0.33}$ and $T_{g,0.66}$ refers to T_g measured at a heating rate of 0.33 K s⁻¹ and 0.66 K s⁻¹, respectively, $T_{x,0.66}$ refers to T_x measured at a heating rate of 0.66 K s⁻¹. $\Delta T_{0.66} = T_{x,0.66} - T_{g,0.66}$ and $\ln B$, D and T_g^0 are VFT fit parameters.

Alloy	$T_{g,0.66}$	$T_{x,0.66}$	$\Delta T_{0.66}$	$\ln B$	D	T_g^0	$T_{g,0.33}$	m
A	700	762	62	5	0.42	652	696	44
B	703	754	51	4	0.40	648	696	35
C	689	781	92	3	0.36	621	680	19

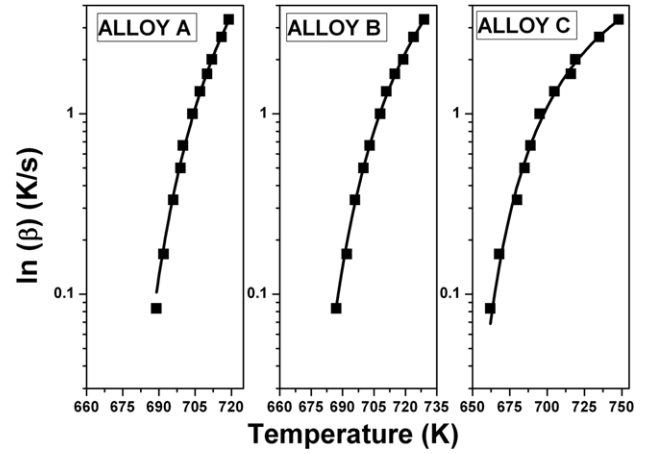


Figure 5. Glass transition temperature as a function of the applied heating rate and the VFT fit for the as-prepared and isothermally treated Cu₄₇Ti₃₃Zr₁₁Ni₈Si₁ alloy powders.

where T is the temperature, T_g the glass transition and $\langle \tau \rangle$ is the average relaxation time. From the VFT fits the fragility parameter (m) at a particular T_g can be calculated as in equation (4) [49]:

$$m = \frac{DT_g^0 T_g}{(T_g - T_g^0)^2 \ln 10}. \quad (4)$$

It is obvious from equation (4) that the value of m depends on the definition of T_g . In order to make a uniform comparison with fragility data found in the literature, m has been evaluated at T_g corresponding to a heating rate of 0.33 K s⁻¹. The m values are also listed in table 1. In the case of alloy A the m value is 44 while for alloys B and C it is 35 and 19, respectively. This reveals that the fragility parameter changes with increasing annealing temperature. There are three key temperatures that are widely used to characterize the vitrification of a supercooled liquid: glass transition temperature (T_g), Vogel–Fulcher temperature ($T_0 = T_g^0$, as in (4)) and the Kauzmann temperature (T_K) [50]. T_g^0 and T_K refer to the kinetic and thermodynamic instability points, respectively [50]. The heating rate (β) dependence of T_g and T_x is plotted by a linear fit for alloys A and B in figure 6. The extrapolation of both curves to lower temperatures as well as heating rates leads to a point of intersection. The temperature that corresponds to this point of intersection has been reported to correspond to the Kauzmann temperature [51]. The T_K values are 645 K and 575 K for alloys A and B, respectively. The T_K value for alloy C could not be determined due to very large errors involved in the extrapolation.

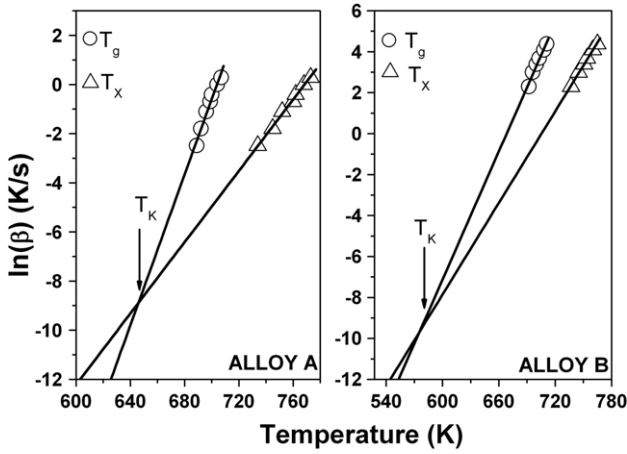


Figure 6. Glass transition temperature and onset temperature of the first crystallization exotherm as a linear function of applied heating rate for the as-prepared and isothermally treated $\text{Cu}_{47}\text{Ti}_{33}\text{Zr}_{11}\text{Ni}_8\text{Si}_1$ alloy powders. The point of intersection is the Kauzmann temperature (T_K).

4. Discussion

The XRD as well as the TEM data for alloy A clearly indicate that the as-prepared powder is fully amorphous. Additionally, the DSC trace of alloy A clearly reveals a distinct glass transition. The thermal stability data of this alloy are in good agreement with previously reported data [42–44]. The purpose of the annealing experiments has been to study the influence of thermal treatment undertaken at temperatures below (688 K for 60 min) and above (723 K for 30 min) the experimentally observed glass transition temperature (700 K at a heating rate of 0.66 K s^{-1}) and to study its effect on the fragility of the metallic glass powders. Since microstructural alterations are possible upon thermal treatment, the influence of microstructure on the fragility is also investigated. After annealing at 688 K for 60 min (alloy B) the XRD pattern gives no hint of the presence of sharp peaks related to any crystallinity. The bright-field TEM image shows no features indicating crystallization but the contrast observed could be due to variations in material density as well as thickness variations [52]. The thermal stability data for alloy B are also different from alloy A, indicating that the composition of the glass has indeed changed upon thermal treatment. A change in composition can lead to local density variations [52]. Additionally, the SAD pattern displays sharper rings and hence suggests an enhanced short-range order upon thermal treatment and points to the beginning of crystallization. The TEM observations are very similar to observations reported for the $\text{Zr}_{52}\text{Ti}_5\text{Cu}_{17.9}\text{Ni}_{14.6}\text{Al}_{10}$ metallic glass that was isothermally annealed near the glass transition [53]. In contrast, the TEM results for alloy C (figure 2(c)) clearly reveal the presence of nanocrystals in an amorphous matrix. This is also corroborated by the DSC trace of alloy C where the first exothermic event seen in the DSC traces of alloys A and B (figure 3) is eliminated. Surprisingly, the XRD pattern for alloy C (figure 1) also does not exhibit any diffraction peaks. A previous study on the crystallization of $\text{Cu}_{47}\text{Ti}_{33}\text{Zr}_{11}\text{Ni}_8\text{Si}_1$ metallic glass powders has shown that the product of the first crystallization exotherm is the $\text{Cu}_{51}\text{Zr}_{14}$ phase with nanometer sized grains [54]. It has been reported

Table 2. GFA data of various glass-forming alloys having similar fragility parameter (m) value. The data are taken from [56].

Alloy composition	ΔT (K)	T_{rg}	R_c (K s^{-1})	m
$\text{Fe}_{30.8}\text{Co}_{46.2}\text{P}_{14}\text{B}_6\text{Al}_3$	38	—	$\sim 10^3$	43
$\text{Pd}_{48}\text{Ni}_{32}\text{P}_{20}$ (non-fluxed)	89	0.67	$\sim 10^3$	41
$\text{Pd}_{40}\text{Ni}_{40}\text{P}_{20}$ (non-fluxed)	88	0.67	$\sim 10^3$	41
$\text{Pt}_{45}\text{Ni}_{30}\text{P}_{25}$	56	0.67	$\sim 10^3$	42
$\text{Cu}_{47}\text{Ti}_{33}\text{Zr}_{11}\text{Ni}_8\text{Si}_1$	62	0.60	~ 70	44
$\text{Co}_{62}\text{Nb}_6\text{Zr}_2\text{B}_{30}$	50	0.63	—	44
$\text{Co}_{46}\text{Fe}_{16}\text{Nb}_6\text{Zr}_2\text{B}_{30}$	88	0.63	—	44

by Jiang *et al* by a simulation study that the $\text{Cu}_{51}\text{Zr}_{14}$ phase, when formed with small grain size (8–15 nm) and defects, shows a broadened amorphous-like feature [55]. Additionally, it has been shown by XRD/high-resolution TEM (HRTEM) studies in case of the $\text{Zr}_{54.5}\text{Ti}_{7.5}\text{Cu}_{20}\text{Ni}_8\text{Al}_{10}$ quasicrystal-forming alloy that though there is a decrease in FWHM by 10%, there is a particle size effect for the non-detectable XRD peaks of quasicrystals [56]. Hence, it is not surprising that the diffraction pattern of alloy C shows an amorphous-like feature.

The fragile/strong behaviour of the supercooled liquid can be classified by the fragility parameter (m) [19, 20]. Open network liquids or strong liquids like SiO_2 and GeO_2 show an Arrhenius-type temperature dependence and exhibit m values in the range of $16 \leq m \leq 30$ [19, 20]. In contrast, fragile liquids, such as ionic melts and polymers, which are characterized by simple nondirectional Coulomb attractions or by Van der Waals interactions, exhibit large values ($m \geq 100$) [19, 20]. Metallic glassy alloys typically have m values in the range of $32 \leq m \leq 66$ and, hence, can be classified in the intermediate category according to Angell's classification scheme [57]. Alloy A with $m = 44$ lies in the area closer to the strong side in the Angell plot. A previous study on the melt fragility of the $\text{Cu}_{47}\text{Ti}_{34}\text{Zr}_{11}\text{Ni}_8$ glass-forming alloy gave a m value of 59 [30, 45]. Hence, it is clear that the addition of 1 at.% Si renders the supercooled liquid stronger in the Angell classification. It was shown that the $\text{Cu}_{50}\text{Zr}_{50}$ BMG has a fragility parameter of 62 [31]. Accordingly, alloy A is a stronger liquid compared with $\text{Cu}_{50}\text{Zr}_{50}$. The m value of 44 is comparable to that of $\text{Fe}_{30.8}\text{Co}_{46.2}\text{P}_{14}\text{B}_6\text{Al}_3$ ($m = 43$) [58] as well as to that of the well-known $\text{Pd}_{48}\text{Ni}_{32}\text{P}_{20}$, $\text{Pd}_{40}\text{Ni}_{40}\text{P}_{20}$ ($m = 41$) [58] and $\text{Pt}_{45}\text{Ni}_{30}\text{P}_{25}$ ($m = 42$) [59] metallic glasses, but smaller than that of $\text{Pd}_{40}\text{Cu}_{30}\text{Ni}_{10}\text{P}_{20}$ ($m = 52$) [60], $\text{Ni}_{75}\text{P}_{16}\text{B}_6\text{Al}_3$ ($m = 53$) [58] and $\text{Au}_{76.9}\text{Ge}_{13.65}\text{Si}_{9.45}$ ($m = 60$) [61, 62]. However, the m value is larger than for $\text{Zr}_{65}\text{Cu}_{17.5}\text{Ni}_{10}\text{Al}_{7.5}$ ($m = 35$) [63], $\text{Zr}_{41.2}\text{Ti}_{13.8}\text{Cu}_{12.8}\text{Ni}_{10}\text{Be}_{22.5}$ ($m = 39$) [64], $\text{Zr}_{46.75}\text{Ti}_{8.25}\text{Cu}_{7.5}\text{Ni}_{10}\text{Be}_{27.5}$ ($m = 18$) [34] and Pr-Cu-Ni-Al ($m = 31$) [27] metallic glasses. Table 2 lists the GFA parameters of numerous metallic glasses having more or less the same fragility parameter as alloy A. Though the m value for alloy A is similar to $\text{Pd}_{48}\text{Ni}_{32}\text{P}_{20}$ and $\text{Pt}_{45}\text{Ni}_{30}\text{P}_{25}$ metallic glasses, $\text{Pd}_{48}\text{Ni}_{32}\text{P}_{20}$ can be formed in bulk form only after fluxing the melt in molten B_2O_3 over several thermal cycles [65] and $\text{Pt}_{45}\text{Ni}_{30}\text{P}_{25}$ has so far not been quenched into a bulk glass. From table 2 it is clear that there is no general correlation between the m value and ΔT as well as with T_{rg} . There seems to be also no correlation between m and the critical cooling rate (R_c). Although the fragility parameter of all the alloys requiring critical cooling rates of the order of 10^3 K s^{-1}

Table 3. GFA data for various Cu-based metallic glasses.

Alloy composition	ΔT (K)	T_g	R_c (K s ⁻¹)	m
Cu ₅₀ Zr ₅₀	47	0.55	250	62
Cu ₄₇ Ti ₃₄ Zr ₁₁ Ni ₈	46	0.57	~250	59
Cu ₄₇ Ti ₃₃ Zr ₁₁ Ni ₈ Si ₁	62	0.60	~70	44

is 41–44, it does not explain the ease of glass formation in the many metallic glass compositions. For example, R_c for Pd₄₀Cu₃₀Ni₁₀P₂₀ ($m = 52$), Zr_{46.75}Ti_{8.25}Cu_{7.4}Ni₁₀Be_{27.5} ($m = 34$) and Mg₆₅Cu₂₅Y₁₀ ($m = 41$) is 0.1 K s⁻¹ [66], 30 K s⁻¹ [9] and 50 K s⁻¹ [22], respectively. It has been shown that the Pd₄₃Ni₁₀Cu₂₇P₂₀ composition is a very good glass former and has a critical cooling rate as low as 0.01 K s⁻¹ [67]. However, the fragility parameter is 65 for this alloy. Not only the m parameter but also the lower driving force for crystal nucleation as well as the diffusion lengths necessary for primary crystallization in the Pd₄₃Ni₁₀Cu₂₇P₂₀ alloy are influencing factors in determining the excellent GFA of this alloy [67]. Hence, the fragility index itself can only give a rough estimate of the GFA but the GFA also depends on the thermodynamics of the system.

However, there seems to be a decent trend in case of Cu-based metallic glasses. Table 3 shows the GFA parameters for the Cu-based metallic glasses. It was mentioned that R_c of Cu₅₀Zr₅₀ ($m = 62$) [31] as well as of the Cu₄₇Ti₃₄Zr₁₁Ni₈ ($m = 59$) glass is 250 K s⁻¹ [32]. The present study gives a m value for Cu₄₇Ti₃₃Zr₁₁Ni₈Si₁ of 44. It was shown that the addition of 1 at.% Si increases the GFA (i.e. increases ΔT and decreases R_c) [42]. R_c decreases by a factor of 3 and the critical casting thickness can be increased by a factor of 1.7 for the alloy containing Si vis-a-vis the alloy without Si [42]. A similar trend has been found in case of the Zr–Cu–Ti–Ni–Be alloy system. For Zr_{46.75}Ti_{8.25}Cu_{7.5}Ni₁₀Be_{27.5}, the m value is 34 [47]. When the composition is slightly changed to Zr_{41.2}Ti_{13.8}Cu_{12.5}Ni₁₀Be_{22.5} the m value obtained is 39 [64] and $m = 31$ for Zr_{42.1}Ti_{12.9}Cu_{11.5}Ni_{10.2}Be_{23.3} [68]. Hence, summarizing the results from tables 2 and 3 it can be said that the idea that ‘a lower m value essentially means a higher GFA in terms of a higher T_g value and a lower R_c ’ holds true only for metallic glasses of a particular family of metallic glasses and cannot be generalized for all glass-forming alloys. The tables also possibly provide a hint that the viscosity is rather material-specific and not a primary factor causing differences in the GFA among these liquids and thermodynamic factors are possibly very important. It has been empirically established that the relation $T_K \cong T_g^0$ holds for many glass-forming liquids [69]. The T_K/T_g^0 ratio is 0.99 and 0.89 for alloys A and B, respectively. It was reported by Tanaka [50] that the higher the T_K/T_g^0 ratio the stronger is the glass. However, it needs to be mentioned that the existence of such a correlation depends critically on how the thermodynamic fragility is evaluated. Conventionally, the entropy is normalized by the value at the melting point or by the value at the glass transition temperature [69, 70]. A study by Fan *et al* [71] proposed an alternate way of defining the thermodynamic fragility. It was suggested that the quantity $\Delta S_f/(T_m - T_K)$, where ΔS_f is the entropy of fusion and T_m is the melting temperature, can adequately define the thermodynamic fragility. Since our alloy has a composition very close to that of Cu₄₇Ti₃₄Zr₁₁Ni₈

whose $\Delta S_f = 10.1$ J mol⁻¹ [72], and $T_m = 1170$ K, this ratio is found to be 0.0192 and 0.0161 for alloys A and B, respectively. The smaller the value of $\Delta S_f/(T_m - T_K)$ the more thermodynamically strong is the liquid [71]. Hence, alloy B is stronger than alloy A. This finding is in accordance with the m values of 44 and 35 obtained for alloys A and B, respectively. The m values are a measure of the kinetic fragility. Hence, it can be said that there exists a relation between the thermodynamic and kinetic fragility. Indeed, it has been shown that there exists a close relation between kinetics and thermodynamics in the determination of the fragility of metallic glass-forming liquids [73, 74]. However, a recent detailed study by Battezzatti [45] has reported that although there exists such a link it is not necessarily proved given the uncertainties in thermodynamic data. Hence, it is logical to say that both the kinetic and thermodynamic contributions play essential roles in the fragility of glass-forming alloys.

With increasing thermal treatment temperature, the fragility parameter of Cu₄₇Ti₃₃Zr₁₁Ni₈Si₁ powders (alloys B and C) shifts to lower values and shifts more towards the side of the strong liquids according to Angell’s classification. This can be explained on the basis of the crystallization behaviour of the Cu₄₇Ti₃₃Zr₁₁Ni₈Si₁ metallic glass. Metallic glasses crystallize by a nucleation and growth process [75]. It has been shown that Cu₄₇Ti₃₃Zr₁₁Ni₈Si₁ exhibits multi-step crystallization behaviour [76]. The crystallization of this alloy starts with the primary precipitation of Cu₅₁Zr₁₄ crystals [54]. Primary crystallization results in the formation of a crystalline phase with an essentially different composition than the starting glass [77]. Alloy B has been annealed below the experimentally measured glass transition of alloy A while alloy C was thermally treated above the experimentally determined T_g . It is well known that crystallization of metallic glasses can occur at temperatures above and below the glass transition temperature [78]. More recently, it has been shown that the crystallization of Cu₄₇Ti₃₃Zr₁₁Ni₈Si₁ glassy powders occurs heterogeneously at temperatures below T_g by the growth of quenched-in nuclei while it occurs homogeneously at temperatures above T_g [79]. From our DSC measurements it is clear that the isothermal treatments done for alloy B and C change the values of T_g and T_x as compared with alloy A. The change is rather marginal in the case of alloy B (T_g changes by 3 K and T_x by 8 K) but more pronounced in the case of alloy C (T_g changes by 11 K and T_x by 19 K). Additionally, the isothermal treatment of alloy C results in the formation of nanocrystals embedded in an amorphous matrix. This suggests that the remaining glassy matrix changes its composition under isothermal conditions. The VFT fit of alloy C (figure 5) describes essentially the steepness of the viscosity curve of the amorphous matrix and reveals that after primary crystallization the matrix is a stronger liquid than the homogeneous Cu₄₇Ti₃₃Zr₁₁Ni₈Si₁ alloy (alloy A). An earlier report on the fragility data of Zr_{41.2}Ti_{13.8}Cu_{12.5}Ni₁₀Be_{22.5} clearly showed that the fragility parameter as well as the T_g^0 value change significantly after primary crystallization [64]. The fragility parameter of the remaining supercooled liquid shifts to the stronger side while T_g^0 shifts to lower values [64]. This suggests that the equilibrium (metastable equilibrium) viscosity value has indeed changed for the matrix (alloy C) towards a higher value. This viscosity change is essentially

caused by changes in the concentration of the matrix towards a composition with a higher viscosity at a given annealing temperature. The lower value of m (i.e. stronger liquid) can be also linked to an increased short-range ordering of the amorphous phase in the case of alloy C. For example, a positive correlation between icosahedral ordering, well known in metallic glasses, and the fragility index has been found [47,50]. It has been shown that the m value is more dependent on the structural gradient between neighbouring clusters (δ) and the activation energy difference (ΔE) for a system to change from one minimum to the neighbouring minimum in a multidimensional energy landscape [73]. However, further studies seem to be necessary to validate this correlation in a more quantitative way.

5. Conclusion

The thermal stability of $\text{Cu}_{47}\text{Ti}_{33}\text{Zr}_{11}\text{Ni}_8\text{Si}_1$ glassy powders synthesized by gas-atomization has been evaluated in terms of the fragility parameter (m) using the VFT relation based on the glass transition temperature determined on the basis of isochronal DSC runs. The fragility parameter is 44 in the as-prepared state and decreases to a value of 19 for a partially crystallized powder. This indicates that $\text{Cu}_{47}\text{Ti}_{33}\text{Zr}_{11}\text{Ni}_8\text{Si}_1$ behaves more like a strong glass. This implies sluggish kinetics and hence contributes to the GFA. The shift of the m value towards a stronger liquid stems from the changed composition of the remaining supercooled liquid. In the case of Cu-based metallic glasses, a lower m value is essentially indicative of a reduced R_c . The fragility of a metallic glass is linked not only to kinetic factors but also to thermodynamic ones.

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