Full-scale Detached Eddy Simulation of kerosene fueled scramjet combustor based on skeletal mechanism

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Large Eddy Simulation (LES) of kerosene fueled scramjet combustor is generally scare in the literature, due mainly to the formidable computational cost arisen by complex kerosene mechanism. In this study, the skeletal reduction of a detailed reaction mechanism (2185 species/8217 steps) of aviation kerosene is conducted using directed relation graph with error propagation and sensitivity analysis (DRGEPSA) method, resulting a skeletal mechanism consisting of 39 species/153 elemental reactions for China Daqing RP-3 aviation kerosene. The comparisons of adiabatic flame temperature, total heat release, ignition delay and laminar flame speed predicted by the skeletal mechanism show an overall good accordance with the original detailed reaction mechanism. Then a three-dimensional Detached Eddy Simulation (DES) modeling based on the skeletal kerosene mechanism is employed for the numerical analysis of a full-scale scramjet combustor, which has been experimentally tested in a long-time direct connect supersonic combustion test platform (abbreviated as DTZ) assembled in Chinese Academy of Sciences (CAS). Pressure and heat flux measurement systems are attached to the combustor assembly to monitor the real-time combustion performance and provide validation data for the numerical modeling. Three cases with fuel equivalence ratios from 0.8, 1.0 to 1.2 and the same crossflow conditions at Mach 2.0 are modeled. The time-averaged static pressure and heat flux are in generally good agreement with the experiment with the peak heat flux slightly underpredicted. The instantaneous and/or time-averaged pressure, momentum, temperature and turbulence fields, which are difficult to be measured, are analyzed to reveal the main flow and combustion physics, especially those related to the flame distribution and holding. The combustion is identified as in ramjet mode for the investigated cases. With the increasing of fuel equivalence ratio, the shock train propagates upstream in the isolator and the interaction between the upstream and downstream combustion assumes different patterns.

1. Introduction

More than 50 years of efforts in ground and flight tests prove the feasibility of the concept of scramjet for future hypersonic flight [1], while some remaining bottlenecks, such as the mixing and combustion mechanism, need to be eliminated through a physical understanding of the flow and combustion processes in scramjet combustors. Although experimental tests have been extensively conducted, little insight is provided for the transient internal flow and thermal environments due to that the difficulties in measuring the high-speed complex unsteady flowfield restrict the available experimental data. High-resolution numerical modeling, especially those based on large eddy simulation (LES) technique, is of great use for a close examination of the flow physics in scramjet combustors as well as their engineering design [2]. However, due to the prohibitive computational cost and the lack of experimental data, most of the modeling analysis focus primarily on individual scramjet component, e.g. inlet/isolator, supersonic combustor and expander/nozzle, while modeling of the integrated flow path in a full-scale combustion is generally scarce. From the literature, the most preferred modeling cases are the HyperShot I&II [3-10] and SCHOLAR [11-16], due a large degree to their relative complete data on experimental setup and measurements.

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for model validation. Simulations based on the experimental cases tested on some other scramjet combustor facilities, such as the DLR scramjet combustor [17, 18], the University of Virginia’s Supersonic Combustion Facility (SCF) [18-21] and the CUBRC Combustion Duct [22], are also growing vigorously. To date, promising work on modeling those experimental cases is still under way to validate the physical models and shock/turbulence capturing algorithms for supersonic combustion, as well as to improve the computational efficiency [23-25].

The supersonic combustion in scramjet combustors can be classified as high-Ma (Mach number) wall-bounded reacting flow, where the main flow physics are shock wave/turbulent boundary layer interaction (SWTBLI), shock/shear layer interaction, turbulence/chemistry interaction (TCI) and shock train/combustion interaction etc. A canonical flow encountered in scramjet combustors is the jet in supersonic crossflow (JISC), which is extensively utilized for transverse fuel injection to increase mixing in order to achieve the required heat release schedule with shorter combustor residence times. Some prior work in applying LES to JISCs at different jet-to-crossflow momentum flux ratios and with different fuel molecular weights has been extensively conducted [14, 26-50] based on the experimental cases of Lin et. al. [51, 52], Hammemann et. al. [53], Santiago and VanLerberghe [54-56], Gruber et. al.[57-60], Ben-Yakar [61], Asö et. al. [62], Spaid and Zukoski [63], and Maddalena et. al.[64], etc. to reveal the mixing and combustion mechanisms. And in order to reduce the grid requirement in near-wall regions, wall-modeled LES [15, 33, 37, 65-67] or hybrid RANS (Reynolds-Averaged Navier–Stokes) / LES [14, 16-21, 26, 28-31, 36, 68-70] is usually used. In terms of existing LES techniques, one of the main challenges for supersonic combustion modeling lies in accounting for the effect of Mach number on flame regime in the Borghi diagram [13, 71], which is essentially due to the general lack of physical understanding on the effects of supersonic conditions on turbulence, reaction rates, and flame regimes [25]. Finite-rate-chemistry Direct numerical simulation (DNS) model in conjunction with detailed kinetic mechanism may exactly reveal the TCI modes, but the computational cost is far beyond the affordance of current computer architectures. To properly address the subgrid (SGS) turbulent effects, chemical reactions as well as their complex interaction in supersonic combustion, persistent endeavor in developing and validating the SGS models, kinetic mechanisms and turbulent combustion models is necessary.

Most of those aforementioned LES based supersonic combustion modellings are based on hydrogen, e.g. those based on HyperShot I&II [3-10] or SCHOLAR cases [11-16], with a few based on pure hydrocarbons (e.g. ethylene [42, 72], methane [73, 74] and acetonitrile [75]), however few are based kerosene [76-79]. Kerosene is a more economic and practical fuel for scramjets cruising at Mach number 4-8, which is the short-term goal of hypersonic flight in the next few decades. However, compared with hydrogen fuel, the difficulty in using kerosene as scramjet fuel is that the slower reaction process and lower heating value hinder the improvement of combustion efficiency. Thus there is a more pressure need to gain a physical understanding of the flow and combustion processes in kerosene fueled scramjet combustors by aid of high-fidelity modeling techniques, when non-intrusive experimental diagnostic methods for supersonic combustion are insufficient. One important reason in the scarcity of modeling studies of kerosene fueled supersonic combustion can be attributed to the formidable computational cost arisen by large-scale kerosene mechanisms, which usually involve thousands of species and even more elemental reactions. The mechanisms used in those previous kerosene fueled supersonic combustion modeling [76-79] are all based on simple global or semi-kinetic mechanisms. Kerosene mechanisms developed for computational fluid dynamic (CFD) should meet the requirements of high fidelity of overall kinetic characteristics and high computational efficiency. In fact, even substituting kerosene by simple hydrocarbon species, e.g. purely n-Decane, the corresponding mechanism still contains hundreds or even thousands of elemental reactions and at least hundreds of species. On one hand, the computational cost is generally scaled with the square of species number [80]. On the other hand, the difference in the characteristic times of each elemental reactions will result in large stiffness of the reacting system [80, 81]. Detailed mechanism generally applies only to small-scale flow problems, while a proper species number for supersonic combustion modeling based on LES or DNS is typically around 20-50. Reduced or skeletal kerosene mechanisms specifically developed for supersonic combustion modeling are generally few in published studies. The global or semi-kinetic mechanisms [82-85] fitted based on experimental data apply only to a narrow region of combustion conditions, and the reduction is usually not conducted based on elemental reactions.

The typical combustion conditions in scramjet combustors are in the range of static pressure 0.5-3.0 KPa and static temperature 300-3000 K. Within the condition range, detailed mechanisms are usually reduced by two types of methods: (1) removing the species and elemental reactions having less influence on the physical quantities of interest (e.g. the total heat release, the production rates of main species) with the aid of sensitivity analysis (SA) [86] and Computational Singularity Perturbation (CSP) from the detailed mechanism to obtain a skeletal mechanism, (2) building algebraic relations among species concentrations through Quasi-Steady State Assumption (QSSA) [87, 88] and Partial Equilibrium Assumption (PEA) [89, 90] to actually reduce the number of unresolved species. However, the reduction efficiency measured by the mechanism sizes before and after the reduction by SA and CSP is generally low and hence the finial skeletal mechanism is usually still too large for supersonic combustion modeling, while the
application of QSSA and PEA involves complex matrix solving, which deteriorates the computational efficiency and numerical stability. Recently, Lu et al. [91-93] proposed a novel skeletal reduction method, i.e. directed relation graph with error propagation and sensitivity analysis (DRGEPSA), which has high reduction efficiency and reliability especially for large detailed mechanisms, e.g. the kerosene mechanisms with thousands of species [94, 95]. DRGEPSA [93] is the combination of the original DRG [91] method with (error propagation) EP [92] and SA, and has shown the best reduction efficiency among DRG-based methods [93]. The DRGEPSA method firstly evaluates the coupling relationship among species using a directed graph and then removes unimportant reaction paths based on the error propagation down the pathway, thus the stiffness of multi-step mechanisms can also be soothed.

In this study, a skeletal reduction based on Dagaut’s detailed mechanism [94] for China Daqing RP-3 aviation kerosene was conducted using DRGEPSA method. Then DES modeling based on the skeletal kerosene mechanism is employed for the reacting flow in a full-scale scramjet combustor, which has been experimentally tested in a long-term direct connect supersonic combustion test platform (abbreviated as DTZ) in Chinese Academy of Sciences. Experimental measurements of static pressure and wall heat flux on the full-scale combustor assembly including isolator, combustor and expander were compared to validate the modeling results. Analysis on the integrated flow fields are presented to reveal the influence of fuel equivalence ratio on the supersonic flow and combustion characteristics which have not been measured experimentally.

II. Numerical models

A. Turbulence model

To reduce the computational cost in modeling the wall boundary layers, a hybrid Reynolds-averaged Navier-Stokes / large-eddy simulation (RANS/LES) technique known as Detached Eddy Simulation 97 (DES97) [96, 97] is applied. The background RANS model as one-equation Spalart–Allmaras model [98], which is set to cover the full wall boundary layer through well-designed inflation grid layer. The boundary layer is estimated firstly based on a pre-trial modeling, then the inflation layer is set to have a total thickness of around 3 mm. The Spalart–Allmaras model is initially designed for the modeling of wall bounded flows in aerospace applications [98], and shows good predictive accuracy for boundary layer with negative pressure gradient. Since only one additional variable known as modified turbulent kinetic viscosity is required to solve, the Spalart–Allmaras is relative simple and thus computationally efficient. The model contains a wall destruction term to reduce the turbulent viscosity of laminar sub-layer and logarithmic sub-layer, ensuring a smooth transition from laminar to turbulent status [99]. In DES97, the length scale d determines in a large degree the order of magnitude of the production and destruction of turbulent viscosity. In the original Spalart–Allmaras model near-wall distance \( d_{\text{wall}} \) is used as the length scale, while in DES97 the length scale is calculated as

\[
    d = \min(d_{\text{wall}}, C_{\text{DES}} \Delta_{\text{grid}})
\]

where \( \Delta_{\text{grid}} \) is the grid size calculated as the cube root of the grid volume or the largest dimension, and the coefficient \( C_{\text{DES}} = 0.65 \) [100]. Usually the RANS mesh has a high aspect ratio in the boundary layer, i.e. the grid size parallel to the wall is much larger than the boundary layer thickness, to ensure the whole boundary layer is modeled in RANS mode according to the definition of length scale. Note that although the concept of DES was initially proposed with the one-equation Spalart–Allmaras as its background RANS model [97], the RANS model can be replaced by any turbulence model that has an appropriately defined turbulence length scale and is a sufficiently localized model, e.g. Menter’s SST two-equation model [65, 101]. In addition, there are some implementations of DES, such as DDES [101, 102] and IDDES [103, 104], allow for regions to be explicitly designated as in RANS or LES mode, and accordingly the current transition based simply on the distance function is classified as DES97. However, in DDES or IDDES approaches, the switch function not only depends on the grid but also of the local solution, thus a careful calibration for the switching parameters are required. Since no previous calibrations have been conducted for a wide range of high-speed compressible flows, in this study the simple DES97 is used.

The Favre-filtered or Favre-averaged Navier–Stokes equations including transport equations for individual species and sensible enthalpy are solved in a uniform framework by equally treating the turbulent viscosity in RANS and the subgrid scale (SGS) viscosity in LES. The Boussinesq hypothesis is used to relate unresolved stresses to the rate of strain of the resolved velocity field, i.e. a functional SGS model is used to dissipate turbulent kinetic energy at a rate mimicking the real physical value. Meanwhile, the gradient diffusion models with constant Prandtl and Schmidt numbers are used to account for the heat and mass diffusions due to unresolved turbulent eddies. The LES is closed also by the Spalart–Allmaras one-equation mixing length model through setting the length scale as \( C_{\text{DES}} \Delta_{\text{grid}} \) in the LES region.

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B. Turbulent combustion model and reduced kerosene mechanism

Understanding of the flame regime in scramjet combustors is crucial for the choice of turbulence chemistry coupling model. The difference in the time and spatial scales of turbulent flow and chemical reactions determines the micro mixing and reaction process of the fuel, leading to different flame regimes. The turbulent chemistry interaction (TCI) in supersonic combustors depends not only on the flow condition, but also is affected by the fuel type [71, 105]. In the Da (Damkohler number) - Re (Reynolds number) diagram shown in Fig. 1, the non-premixed flame in scramjet combustors can be divided into three typical regimes, i.e. wrinkled laminar flames \((Da > 1, \delta_i < l_k, \delta_f - \text{flame thickness}, \ l_k - \text{Kolmogorov scale}), \) flamelets in eddies \((l_k < \delta_i < l_p, \ l_p - \text{integral turbulence scale})\) and distributed reactions \((Da < 1, \delta_i > l_p)\) [106], denoted respectively by A, B and C in the diagram. In the typical flight conditions of scramjets, the flame thickness \(\delta_i\) in the combustor is generally between Kolmogorov scale \(l_k\) and Taylor scale \(l_p\), \(\delta_i\) is close to \(l_i\) at low inlet pressure and temperature, but gradually tends towards \(l_k\) with the increasing of inlet pressure and temperature [107]. In addition, compared with subsonic flows, the compressibility drives the transfer of kinetic energy from larger to smaller scales at a faster rate (i.e. a steeper slope in the scaling law of kinetic energy transfer), and the dissipative eddies (i.e. those in Kolmogorov scale) are larger in high Mach number supersonic flows [71]. The high compressibility also increases collisional frequency and results in faster kinetics and thus higher flame speed and thinner flame [71]. Thus in scramjet combustors, the flame thickness may become smaller than the smallest turbulent eddies, which hence can only wrinkle the flame front to form corrugated flame rather than thicken the flame thickness through entering the reaction zone. For hydrogen fuels with small ignition delay time scale, experimental data and theoretical calculation show that most of the supersonic combustion region is in the regime of wrinkled laminar flames (\(Ki<1\)) or the upper regime of flamelets in eddies (\(1<Ka<100\)), where flamelet based turbulent combustion models are correct or approximately applicable [71, 105]. Whereas for complex hydrocarbon fuels (e.g. kerosene), the time scale of chemical reactions is close to that of turbulence eddies, all the combustion region is in the regime of flamelets in eddies (\(Ka>1\)), where the micro interactions between turbulence chemistry within the subgrid scale should be modeled by an approximate turbulent combustion model to close the filtered reaction rate term in the filtered species equations. Besides, there are subsonic combustion regions in the scramjet combustors since the combustors may run in ramjet mode under a certain fuel equivalence ratio, the nonuniform combustion condition can results in local regions in different flame regimes, therefore the selected turbulent combustion model should cover different flame regimes.

In this study, the PaSR (Partially Stirred Reactor) model initially proposed for internal engine combustion [108, 109] is used to account for the effect of mixture imperfections on chemical reaction rates. PaSR model is an extension of the classic EDC (Eddy Dissipation Concept) model [110, 111] but has a more accurate prediction on flame structures [112]. In PaSR, the final filtered reaction rate \(\omega_i\) is mutually determined by the characteristic times of chemical reactions \(\tau_c\) and turbulent micro-mixing \(\tau_{mix}\),

\[
\omega_i = \omega_l \frac{\tau_c}{\tau_c + \tau_{mix}} \tag{2}
\]

where \(\omega_l\) is the laminar reaction rate calculated using the filtered quantities, micro-mixing time is the same order of magnitude of Kolmogorov time scale \(\tau_{mix} = C_{mix} \left(\frac{\nu_{eff}}{\epsilon}\right)^{1/2}\) with \(C_{mix} = 1.0\). From the above formula, the PaSR is a blending of quasi laminar model and eddy dissipation model (EDM) [113] depending the absolute dominance of chemistry or mixing in the rate control. In the DES based on Spalart-Allmaras model, the dissipation rate of turbulent kinetic energy is calculated as \(\epsilon = 2\nu_{eff}|\mathbf{S}_{ij}|^2\), where \(\mathbf{S}_{ij}\) is the strain rate. The characteristic chemical time is calculated as the reciprocal of elements of Jacobian matrix

\[
\tau_c = \left(\frac{\partial \omega}{\partial c}\right)^{-1} \approx \sum_{i} \frac{\omega_{ci}}{N_{rec}} \tag{3}
\]

where \(c_i\) is the initial concentration of species \(i\), \(\omega_i\) is the total production rate of species \(i\) summarized from all related element reactions, \(N_{rec}\) is the total number of element reactions.
The prior problem to conduct numerical modeling of supersonic combustion based on kerosene is to find proper surrogates to simulate the complex multi-component hydrocarbon fuel, which usually has a component number larger than 1000 and the mole fraction of individual component is usually less than 10%. The major components of kerosene type fuels (e.g. Jet-A1 and JP-8) are straight chain paraffins, branched chain paraffins, cycloparraffins, aromatics and alkenes, most in the molecular formula of C7-C16 [114]. In addition, the composition of each kerosene type fuel also varies with the band and the producing area.

Since 2000, the institute of mechanics (Chinese academy of sciences) has conducted extensive research on the thermophysical properties and combustion characteristics of China RP-3 aviation kerosene [81]. Chromatographic analysis shows that China Daqing RP-3 consists of 92.5% saturated hydrocarbons, 0.5% unsaturated hydrocarbons and 7% aromatics, and the critical temperature and pressure are 630 K and 2.4 MPa respectively [115], i.e. similar with Jet-A in both chemical composition and thermophysical properties. Therefore the combustion modeling based on China RP-3 aviation kerosene usually adopts directly the mechanisms developed for Jet-A and JP series aviation kerosenes. Analysis based on the principle of extended corresponding states (ECS) [116] shows that the three-species surrogate proposed by Dagaut et al. [95, 117] can accurately simulate the thermophysical and transport properties of China RP-3 kerosene, including those in supercritical state. In the latest release of detailed mechanism, Dagaut et al. [94] updated the surrogate compositions on the basis GC (gas chromatography) and GC/MS (gas chromatography / mass spectrometry) multidimensional analyses. In this study, the updated surrogate will be adopted to simulate the chemical composition of China RP-3 kerosene, and reduction on the corresponding mechanism will be conducted for the typical working condition range of scramjet combustors within a given error tolerance.

The mechanism reduction for RP-3 kerosene is conducted with the aid of computer program through a trial and error procedure, which mainly consists of three steps.

1) Using the directed relation graph with error propagation (DRGEP) method to remove unimportant species in the original detailed kerosene mechanism until the error in ignition delay reaches the maximum allowance. Firstly, choose appropriate target species, such as fuel surrogate species, oxygen, nitrogen and the final products (e.g. water vapor and carbon dioxide) according to the reaction path analysis for kerosene combustion in the combustor. Then a graph search in the network composed of interconnecting element reactions in the kerosene mechanism is performed to build the dependency paths for all species from the user-specified target species. Along each reaction path, calculate the direct interaction coefficients (DICs) between adjacent species, then cumulatively multiply all the intermediate DICs to obtain the path interaction coefficient (PIC). The maximum of all PICs between the target and each species of interest is defined as the overall interaction coefficient (OIC), which distinguishes the relative importance of all the graphic search paths connected the target and the examined species. Remove unimportant species in the detailed kerosene mechanism should their OICs fall below the an automatically-determined OIC threshold \( e_{OIC} \), and eliminate reactions participated by those already removed species. Calculate the ignition delay based on the reduced mechanism using the SENKIN package [118] distributed with CHEMKIN-III under the typical thermodynamic conditions of scramjet combustors, if the ignition delay error falls within the maximum

![Figure 1. Non-premixed flame regimes in scramjet combustors](image-url)
allowance, then increases the OIC threshold in a small step to remove more unimportant species until the ignition delay reaches the maximum allowance, i.e. a user-specified error limit e.g. 50%.

2) In the previous DRGEP reduction phase, part of limbo species have been retained through increasing the OIC threshold by a small factor of e.g. $e^{0.1}$. Then sensitivity analysis on those limbo species in the range of $[e_{OIC}, e_{OIC}e^{0.1}]$ further removes intermediate species and corresponding element reactions. Firstly calculate the ignition delay errors when those limbo species are removed one by one from the original detailed mechanism, retain those with induced errors higher the user-specified error limit, and sort the remaining limbo species in ascending order according to their induced errors. Then the global error is calculated when each of those remaining limbo species is removed in order from the mechanism produced in the previous DRGEP phase, until it reaches the user-specified error limit. Following the sensitivity analysis phase, a final skeletal mechanism consisting of 39 species and 153 reactions is reduced from the original 2185 species and 8217 reactions [94] with approximately 50% maximum error in ignition delay.

3) Through the above directed relation graph with error propagation and sensitivity analysis (DRGEP-SA) phases, only the error in ignition delay is controlled within an allowed limit while the other kinetic properties have not been validated. Fig. 2 shows the comparisons of kinetic properties between the skeletal mechanism and the original mechanism. Fig. 2 (a)-(c) are the modeling results of a closed homogeneous reactor, where reaction occurs in a constant-pressure adiabatic container with well-stirred mixture in unity equivalence ratio. The container pressure is maintained at 1 atm and the initial mixture temperatures are set as 1200 K, 1500 K, 1800 K, 2100 K and 2400 K for parameter study. Here the ignition is defined when the temperature reaches a value of 400 K above the initial temperature. Fig. 2 (d) is the modeling result of a one-dimensional freely propagating flame model, where different equivalence ratios from 0.7 to 1.5 are set. In overall, the adiabatic flame temperature, total heat release, ignition delay and laminar flame speed predicted by the skeletal mechanism show an overall good accordance with those predicted by the original detailed reaction mechanism. The total heat release determines the heat addition to the combustor and thus the peak pressure, while the ignition delay determines the downstream lifting distance of main reaction zones, which usually corresponds to the location of peak pressure, thus an accurate skeletal mechanism is of vital importance for the flowfield predictions in the supersonic combustor.

![Figure 2](image_url)

Figure 2. Comparisons of kinetic properties between the reduced skeletal mechanism (39s/153r) and the original detailed mechanism (2185s/8217r), (a) flame temperature, (b) total heat release, (c) ignition delay, (d) laminar flame speed.

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Detailed mechanisms for the oxidation hydrocarbon fuels usually contain hundreds of or thousands of element reactions, even if the skeletal mechanisms contain at least more than one hundred reactions, based on which three-dimensional reacting flow modeling requires huge computational resources and the existent computer technology cannot meet the practical demand in solving engineering problems. To further speed the solving of large hydrocarbon chemistry systems, In Situ Adaptive Tabulation (ISAT) method [119, 120] is adopted to tabulate and map the initial and final thermodynamic states in the multidimensional space coordinated by thermodynamic parameters. ISAT firstly solves the final thermodynamic state by direct integration (DI) for a given initial thermodynamic state after a certain reaction time, then stores the initial and final states in an in situ table. In the subsequent calculations, the time consuming integration process is replaced by simple algebraic interpolation on the final state parameters corresponding to the initial state parameters most matchable to the current thermodynamic parameters. It is worthwhile to note that most reacting system involves only a subspace of the complete multi-dimensional space coordinated by thermodynamic parameters, which depends on the local combustion conditions, such as the reaction mechanism, thermophysical properties and turbulence characteristics, and cannot be determined beforehand. In order to save storage space and improve the efficiency of subsequent lookups, ISAT table need to be progressively built during the modeling process. In parallel computations, the ISAT table is built in situ for each dividing computational zone, and there are no ISAT data interexchange among the processors. In scramjet combustors, the main reaction zone lies around the jet wake and the cavity, building separated ISAT table helps to reduce the CPU communication cost and improve the computation speed. With the completing of the table, most of the direct integrations can be avoided and thus the solving of large hydrocarbon reacting systems can be greatly accelerated.

C. Solver setup and numerical details

The modeling is performed based on an in-house developed supersonic combustion solver, AstroFoam, which is based on Finite Volume Method (FVM) to be compatible with the unstructured meshes generated for supersonic combustors in complex geometry shape. AstroFOAM is developed on the basis of a compressible rhoCentralFoam solver distributed with the OpenFOAM v2.3.0 CFD package [121], mainly through adding the features of multi-species transport and multi-component reaction. Correspondingly, the sensible enthalpy equation instead of the sensible internal energy equation is solved in AstroFoam for the modeling of transient reacting flows. The inviscid flux scheme in the rhoCentralFoam solver, i.e. the second-order semi-discrete Kurganov-Tadmor (KT) central scheme [122], has been demonstrated to be non-oscillatory in capturing flow discontinuities (e.g. shock waves) while computationally efficient since neither Riemann solvers, Jacobians nor characteristic decompositions are involved [123]. Similar OpenFOAM solvers have been developed to study subsonic flows by Vuorinen et. al. [124] and Baba-Ahmadi and Tabor [125], as well as supersonic flows by Vuorinen et. al. [126, 127] and Fureby et. al. [3, 10]. In AstroFoam, the flux discretization is extended to second order spatial accuracy by reconstructing the primitive variables on interfaces using Total Variation Diminishing (TVD) scheme, for which the Minmod limiter is used in this study. The molecular viscosity is calculated based on Sutherland formula, and unity Prandtl number and Schmidt number are applied for the calculation of thermal and mass diffusion coefficients.

The computational domain consists of an isolator, a combustor and an expander in full size of the square supersonic combustor that has been experimentally studied. To relief the prohibitive computational cost, only half of the actual combustor (split in the spanwise direction) is used as the computation domain with symmetrical boundary condition applied to the splitting plane. Although the domain splitting will restrain the three-dimensional evolution of coherent structures in some extent, its influence on the average flow fields is generally considered small. The mesh is generated using the Cartesian CutCell method, which uses a patch independent volume meshing approach with surface mesh automatically created from boundary of volume mesh, thereby producing high-quality and uniform hexahedral grid cells for most internal volume of the computational domain, while tetrahedron, wedge or pyramid grid cells are filled only in the border regions or corners with large local curvature. Different cell size can be specified for the three combustor parts and boundary surfaces, then the mesh is then adaptively refined based on the local size function values. The minimum cell size is 0.25 mm distributed mainly around the fuel injectors, and the rest domain is meshed with the maximum cell size of 1 mm and a size growth rate of 1.2. The total cell number in the half-splitting combustor domain is 20.55 million. Inflation layers are laid on the lateral wall boundaries with the near wall nondimensional cell size $y^+ < 1$. The inflation layers have a total thickness of 3 mm which is approximately the boundary layer thickness estimated from a prior modeling. The cells in the inflation layers have a high aspect ratio, i.e. the cell dimension parallel to the wall is much larger than that normal to the wall, to ensure the DES model acts as a RANS model there. Grid quality analysis shows that (1) the proportion of hexahedral cells is close to 100%, thus ensuring high solving efficiency and convergence rate; (2) 99.9% of the cell has a skewness smaller than 0.05, indicating approximate equilateral cells in shape; (3) 99.9% of the cells have orthogonal quality higher than 0.963, which can improve the accuracy in face interpolation. The excellent grid quality demonstrates

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that the CutCell method can mesh complex geometric features without compromising the overall grid quality. In the following analysis, the coordinate origin locates at the lower left corner of the square combustor, X represents the streamwise direction, Y represents the height direction, and Z represents the spanwise direction.

The experimental configurations corresponding to the current modeling setup are shown in Table 1. The experiment was conducted on a long-time direct-connect supersonic combustion test facility (abbreviated as DTZ in the following) built in State Key Laboratory of High Temperature Gas Dynamics (China). DTZ consists of an air supply system, a nozzle section, a combustor assembly, a water-cooling system, a data acquisition and control system, a fuel heating and delivery system. Static pressure and wall heat flux were measured during the whole test period by pressure transmitters and heat flux sensors attached to the combustor assembly. The incoming vitiated air, which is supplied by burning hydrogen in air with oxygen replenishment in unity equivalence ratio, has a raised stagnation temperature of 1300 K and a Mach number (Ma) of 2.0 at the entrance of isolator. The compositions of vitiated air are N₂ in 65.2% mole fraction, O₂ in 20.9% and H₂O in 13.9%, with more water content than the high enthalpy flow encountered in a real flight test. The fuel equivalence ratio is changed from 0.8, 1.0 to 1.2 while the incoming vitiated air is maintained at the same flow conditions, in order to investigate the influence of fuel equivalent ratio on the combustion characteristics in the combustor. The fuel is injected from 2 upstream and 2 downstream (in the half-sectioned modeled combustor) 2.8-mm-diameter circular injectors oriented normal to the wall (approximately normal to the supersonic crossflow since the upper wall has a small expanding angle) and before each belonging cavity. Hydrogen is used as ignition fuel in each test and turned off once the kerosene has been ignited.

The inlet boundary conditions on the isolator inlet and the fuel injectors are set according to the experimental configurations listed in Table 1. Open boundary condition is applied to the expander outlet, where zero gradient is used for outflow and ambient flow parameters are specified should backflow occur. Nonslip boundary condition is applied on the combustor walls. In the experiment, the combustor walls were cooled by a water-cooling system to maintain a low wall temperature far below the material melting point. The thermal condition on the wall boundaries is estimated by an Integrated Gas-liquid-solid Thermal Analysis Model for Hydrocarbon based Regenerative-Cooled Supersonic Combustor developed by the authors’ group. Turbulent viscosity on the non-slip combustor walls is modeled by a wall function model, which bridges the viscosity-affected sublayer (VASL) and the fully turbulent region through formulating the turbulent viscosity as a semi-empirical expression,

\[ \mu_t = \mu \left( \frac{y'}{\ln(Ey')} - 1 \right) \]  

where \( y' \) is the nondimensional distance from the wall, Von Karman constant \( \kappa = 0.4187 \), empirical constant \( E = 9.793 \), \( k \) is the turbulence kinetic energy at the wall-adjacent cell centroid.

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<th>Table 1. Experimental and modeling configurations</th>
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<td><strong>Air</strong></td>
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<td>MPA</td>
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III. Results and discussion

A. Pressure fields

Figure 3 shows the static pressure contours predicted for the cases with different fuel equivalence ratios. An obvious observation is that the pressure rise due to combustion propagates towards the isolator inlet with increasing equivalence ratio. Several oblique shocks in train structure can be observed in the isolator from the abrupt pressure rises, indicating a thin boundary layer developed since the isolator inlet. High pressure mainly distributes around the upstream injector in the combustor, and the high pressure region enlarges as well with increasing equivalence ratio. Whereas, the pressure rise due to combustion around the downstream fuel injector is unobvious, with only a small pressure rise region observed immediately after the downstream injector for the equivalence ratio of 1.2. Fig. 4 compares the time-averaged static pressure profiles predicted by the current modeling with those measured in the tests. The agreements are generally good for all the modeling cases whether in the general trend or the peak value. Note that the inlet conditions for the incoming vitiated air is influenced by the combustion efficiency of upstream heater and also the roughness of converging-diverging nozzle, thus the inlet pressure varies within 10 KPa in the

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tests, which is one of the uncertainties in the modeling setup. The locations of initial pressure rise near the isolator inlet are well predicted. Then the pressure increases almost linearly towards the combustor inlet. There are noticeable abrupt pressure rises due to the first oblique shock wave in the cases with $\phi=1.0$ and 1.2 both in the modeling and the tests. The peak pressure located at the upstream injector is slightly overpredicted by around 10 KPa. The pressure ratio between the peak pressure and the initial pressure increases from 4, 4.5 to 5 for the three equivalence ratios. There are slight pressure rises at the downstream injector, corresponding to the small higher pressure rise regions observed in Fig. 3. The pressure rises at the expander outlet in the measured data are due to the upstream propagation of background pressure, which is ambient atmosphere pressure (1 atm) in the experiment while zero-gradient open boundary condition is applied for the outlet in the modeling.

![Figure 3. Instantaneous static pressure contours on the streamwise plane through one fuel injector (Z=57 mm) for different fuel equivalence ratios: (a) 0.8, (b) 1.0, (c) 1.2](image)

![Figure 4. Time-averaged static pressure profiles on the centerline of the lateral wall (Y=35 mm) for different fuel equivalence ratios: (a) 0.8, (b) 1.0, (c) 1.2](image)
B. Temperature fields

Figure 5 shows the time-averaged temperature contours on the slices through one injector for different equivalence ratios. The maximum instantaneous temperature is around 2700 K. The instantaneous distribution of conserved scalars, e.g. temperature and species concentrations, varies significantly with time, thus the mean fields are analyzed instead. The shock train in the isolator increases the static temperature of incoming air to above 1000 K, which facilitates the initial chain reactions and the autoignition of supercritical kerosene. As can be seen, the fuel is not ignited immediately after the injector, but mainly oxidized since the cavity. The temperature in the wake region following the fuel injection has a lower temperature, which is caused not only by the expanding but also by the endothermic chain reactions there. Those initial chain reactions between the fuel injector and the cavity prepare radial pool for the subsequent ignition. The regions with high temperature (>1966 K) are distributed in the mixing layer following the cavities and attached to the walls. With the increasing of equivalence ratio, the upper high-temperature region thickens gradually and the lower high-temperature region expands towards both the cavity and the expander.

Figure 6 shows the instantaneous heat release distributions for the three equivalence ratios. The main reaction occurs in the mixing layer starting from the leading edge of the cavities, indicating the importance of cavity in the flame anchoring. There are generally three flame anchoring modes observed both in the modeling and experiments, i.e. (a) jet-wake mode, the flame resides in the jet wake immediately after the injector, (b) cavity mode, the flame resides in the mixing layer since the leading edge of cavity, (3) oscillation mode, the flame resides in the above two locations periodically. The jet-wake mode usually occurs for fuels (e.g. hydrogen) with short ignition delay or incoming flow with high enthalpy. For multi-component fuels, e.g. kerosene with large ignition delay, the most commonly encountered flame anchoring mode is the cavity mode, where the cavity acts the four roles of preheater, mixer, residing bay (low flow speed) and radical pool. The oscillation mode is seldom observed, but can occur at a medium ignition delay within a small marginal region and has been confirmed in an ethylene fueled test (results not shown here) conducted by the authors’ group. As the equivalence ratio increases from 0.8, the upstream reacting layer extends and corrugated by large-scale vortices. The heat release on the top of the downstream cavity is negligible compared with the upstream one for $\phi=0.8$. In addition to the reacting layer anchored at the leading edge of the downstream cavity, the downstream reaction zone is multi-layer for $\phi=1.0$ and 1.2. This is because that the downstream fuel jet is preheated by the upstream high-temperature mixing layer as shown in Fig. 5, and the fuel in the jet wake is ignited after some distance downstream, especially a co-exist jet-wake mode becomes apparent for $\phi=1.2$.

Figure 7 compares the predicted heat flux profiles with the measurements for the three equivalence ratios. The agreement in the general trends is good, but the peak and overall heat flux are both overpredicted. The heat flux on the isolator wall is well predicted. The heat flux has a sharp increase at the leading edge of the upstream cavity and then peaks in a small distance since the trailing edge, where large heat release usually occurs as shown in Fig. 6. Both the and measured predicted heat release has a plateau in the region between the upstream and downstream cavities, where the heat flux is overpredicted for about 20%. The heat flux then decreases towards the outlet in the expander, where the heat flux is well predicted for $\phi=1.0$ but overpredicted by almost 50% for $\phi=0.8$ and 1.2. The cavity effect on the predicted heat flux is not obvious, for example the small sharp rise observed in the measurements around the downstream cavity is not observed in the prediction. This is because the thermal boundary condition determined from the Integrated Gas-liquid-solid Thermal Analysis Model is based on a one-dimensional flow analysis, where the effect of cavities on the combustion cannot be well accounted for. The heat flux is generally sensitive to the thermal boundary condition and the thickness of turbulent boundary layer, thus an accurate description of the heat flux needs to accurately model the development of boundary layer, which is still a involved problem for supersonic flows due to the complex Shock Wave/Turbulent Boundary Layer Interaction (SWTBLI). Hot spots on the instantaneous heat flux distribution on the walls were observed in the modeling, due to the separated regions (appear as bubbles) caused by impinging shock wave strengthen the convective heat transfer [128]. However, a sensitivity analysis on the heat transfer to the RANS boundary layer modeling merits future research.
Figure 5. Time-averaged static temperature contours on the streamwise plane through one fuel injector (Z=57 mm) for different fuel equivalence ratios: (a) 0.8, (b) 1.0, (c) 1.2

Figure 6. Instantaneous heat release rate distributions on the streamwise plane through one fuel injector (Z=57 mm) for different fuel equivalence ratios: (a) 0.8, (b) 1.0, (c) 1.2

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Figure 7. Instantaneous heat flux profiles on the upper wall for different fuel equivalence ratios: (a) 0.8, (b) 1.0, (c) 1.2.

C. Velocity fields and shock structures

Figure 8 and 9 show the predicted instantaneous contours of velocity magnitude and corresponding Mach number for different fuel equivalence ratios. The flow is quite uniform before the first oblique shock wave in the isolator and the boundary layer is much thin. With the origination or the impinging of shock waves, the boundary layer is discontinuously thickened or separated by the negative pressure gradient imposed by the combustion pressure rise. Corresponding to the shock train, there are a succession of speeding regions in the remainder of isolator. The flow speed decreases significantly to even below 100 m/s around the upstream injector and in the cavities, the low speed (<390 m/s) region expands greatly as the equivalence ratio or heat release increases. While the flow is only slowdown in the fuel jet wake region and inside the cavity for the downstream, where the high-diverging-angle expander tends to relief the thermal choking in some degree. Due to the significantly low flow speed (locally <100 m/s) in the cavities, the flow residence time is of the order of 1 ms, which is on the same order magnitude of the ignition delay of kerosene, implying a quasi-equilibrium reaction can be reached there to provide not only high temperature but also rich radicals for the flame anchoring.

The sound speed line in Fig. 9 delimits the supersonic and subsonic regions. As can be seen, most of the combustion occurs under subsonic condition and thus the scramjet combustor actually run a ramjet mode with the shock train acts as the first aerodynamic throat. At $\phi=0.8$, there are some discontinuous supersonic flow regions around the downstream cavity. The length of subsonic regions increases with increasing equivalence ratio. The flow is then reaccelerate to supersonic in the expander, implying a second aerodynamic throat is formed in the combustor due to the pressure rise around the upstream fuel injector and cavity.

Figure 8. Instantaneous velocity magnitude contours on the streamwise plane through one fuel injector (Z=57 mm) for different fuel equivalence ratios: (a) 0.8, (b) 1.0, (c) 1.2.
Figure 9. Instantaneous Mach number contours on the streamwise plane through one fuel injector (Z=57 mm) for different fuel equivalence ratios: (a) 0.8, (b) 1.0, (c) 1.2

Figure 10 shows Instantaneous magnitude contours of density gradient (|∇ρ|), which is similar to the schlieren images but without knife edge cutoff. Four types of flow regions with large variation in density are clearly shown, i.e. shock waves, fuel stream, reacting layer and boundary layer. At least four successive shock wave structures consisting the shock train can be observed in the isolator, and they propagates upstream as the equivalence ratio increases. The penetration height of the large-density kerosene fuel increases significantly. The reacting layer generally corresponds to the distribution of heat release rate in Fig. 6, where the flame is anchored at the leading edge of the cavity and extends over the cavity for one or two cavity length(s). The upstream reacting layer, as also shown in Fig. 5, can penetrate across the combustor in transverse direction and extends to reach the downstream jet wake, thus the downstream fuel is ignited before they entering the cavity and additional reacting layers appear over the downstream cavity. For the upstream part, the fuel stream interacts with the reacting layer rooting at the leading edge of cavity at a cross point, form which the flame can propagate upstream to ignite the fuel in the jet wake should the flame speed becomes high enough under certain conditions, e.g. high-enthalpy incoming flow shortens the ignition delay or the fuel stream is simply changed in compositions. Thereby, the intersection point act as an important bridging role in the oscillation flame-anchoring mode. The downstream fuel stream penetrates deeper thus does not intersect with the reacting layer starting from the cavity leading edge, because the momentum flux of the cross flow has been decreased by the upstream heat addition and wall friction [129, 130] while isotropic one-dimension analysis indicates that a Mach number of $\sqrt{2}$, far beyond the current subsonic value, could achieve the maximum momentum flux [131]. Thickened or separated boundary layer can also be visualized in the end part of isolator and the combustor with large negative pressure gradient, while the boundary layer in the expander is thinner.
D. Turbulence fields

Figure 11 shows the instantaneous contours of vorticity magnitude for different equivalence ratios. With the increasing of equivalence ratio, the vorticity strengthens and broadens due to the increasing in combustion heat release and the distortion of crossflow by transverse jet with increasing penetration height. The vorticity distribution in the isolator denotes the basic shape of boundary layer along with the separated and detached flow regions, under the impinging of shock waves. The formation of shock wave, or so called pseudo shock wave (PSW), in the isolator is to rise the static pressure of cross flow in order to match the back pressure propagates upstream from the combustor. From this point of view, the negative pressure gradient, which counterbalances the forward momentum and finally separated or thicken the boundary layer, phenomenally caused by the shock waves but actually originates from the combustion pressure. As evidenced by the current modeling results, in the back part of isolator and in the combustor, boundary layer still thicken or separated without the origination or impinging of shock waves. With the increasing of combustion pressure rise, the boundary layer is firstly influenced by the negative pressure gradient, then the vorticity generation in the internal flow field in the upstream is enhanced, indicating the boundary layer acts as the key role in the information propagation from downstream to upstream for supersonic flows. The vorticity enhancement in the isolator will promote the turbulent mixing in the downstream combustor, which will further increase the combustion efficiency and thereby total heat release. The region with the most intense vorticity generation is in front of the upstream injector, corresponding to the pressure plateau in Fig. 3. Unlike in subsonic flows, vorticity distribution is not exclusively driven by vortex stretching, but also by baroclinic and expansion effects [71]. Between the upstream and the downstream cavities, the high vorticity generation is due to the baroclinic torque arisen by the combustion heat release. On the other hand, the expansion effect due to combustion tends to redistribute the vorticity in the combustor. Large-scale vortexes can be observed from the vorticity distribution in the expander, where no reaction occurs but only the mixing between the hot layers and the relative cold crossflow as shown in Fig. 5.

Figure 12 provides a detailed insight into the development of coherent structures in the full-scale scramjet combustor identified by the iso-surface of a positive value of the Q-criterion, which measures the balance between the magnitudes of vorticity and strain rate [132]. The successive oblique shock waves can be seen in the beginning of isolator, vortexes are formed since the origination of the first shock wave. One important behavior of vortexes is that then can be transported, merge, breakup and finally dissipate like distinct individuals. With the increasing of fuel equivalence ratio, the vortexes span upstream to the isolator, and the vortex structures in the combustor become richer both in the amount and the hierarchy. The vortexes in the isolator are generally streamwise and in large scales, then break up to small scales and in more random orientation in the combustor. The breakup of large-scale vortexes to small-scale twisted vortexes occurs to the location with the maximum combustion pressure in Fig. 3, i.e. around the upstream cavity for $\phi=0.8$ while around the upstream injector for $\phi=1.0$ and 1.2. This is because the reduction in the through area $A$ of aerodynamic throat by heat addition increases the turbulence Reynolds number as $Re\sim\rho U\sim 1/A$, therefore after the upstream cavity the generation of turbulent vortexes diminishes gradually and becomes trivial in the expander. It is noticed that vortexes in roller or $\Omega$ shape are formed near the wall boundary and in the cavity due to large shear stress there. Those vortexes originated from the boundary layer have low speeds compared with those forming in the internal field. The $\Omega$-shaped vortices are three-dimensional coherent structures resulting from the interaction between the boundary layer and the flow due to Kelvin-Helmholtz (K-H) instability. A large number of fine vortexes are formed due to the on-going breakup of large-scale vortexes and then dissipate gradually in the expander.
IV. Conclusions

DES modelings for three reacting cases with different fuel equivalence ratios in a full-scale rectangular scramjet combustor have been presented to validate the modeling framework as well as to investigate the effect of equivalence ratio on the flow and combustion characteristics. The modelings are based on a set of skeletal kerosene mechanism, which was reduced in accordance with the specific conditions in the supersonic combustor and to be size affordable for high-fidelity LES based modeling. The modeling results were validated against available experimental measurements and analyzed to reveal the flow and combustion physics which are difficult to be measured, with particular attention given to the flame distribution and holding. The main findings and conclusions are summarized as follows.

1) The predicted and measured time-averaged static pressure on the streamwise direction agree well both in the general trend and the peak value. High pressure mainly distributes around the upstream injector in the combustor, while the pressure rise due to combustion around the downstream fuel injector is unobvious. The pressure rise due to combustion propagates towards the isolator inlet with increasing equivalence ratio, and the high pressure region enlarges as well. The pressure ratio between the peak pressure and the initial pressure increases from 4, 4.5 to 5 as the equivalence ratio increases from 0.8, 1.0 to 1.2. Abrupt pressure rises due to the oblique shocks in train structure can be observed in the isolator.

2) The maximum instantaneous temperature is around 2700 K, and the regions with high temperature (>1966 K) are distributed mainly in the mixing layer following the cavities and attached to the walls. With the increasing of equivalence ratio, the upper high-temperature region thickens gradually and the lower high-temperature region...
expands towards both the cavity and the expander. The main reaction occurs in the mixing layer starting from the leading edge of the cavities, indicating a cavity flame anchoring mode. The predicted heat flux profiles agree well with the measurements in the general trend for the three equivalence ratios, but the peak heat flux is overpredicted for about 20% in the combustor region.

3) Most of the combustion occurs under subsonic condition and thus the scramjet combustor actually run a ramjet mode with the shock train acts as the first aerodynamic throat. The length of subsonic regions increases with increasing equivalence ratio. Due to the significantly low flow speed (locally <100 m/s) in the cavities, the flow residence time is on the same order magnitude of the ignition delay of kerosene, implying a quasi-equilibrium reaction can be reached there to provide not only high temperature but also rich radicals for the flame anchoring. For the upstream part, the fuel stream interacts with the reacting layer rooting at the leading edge of cavity at a cross point, form which the flame can propagate upstream to ignite the fuel in the jet wake should the flame speed becomes high enough under certain conditions, e.g. high-enthalpy incoming flow shortens the ignition delay or the fuel stream is simply changed in compositions.

4) With the increasing of equivalence ratio, the vorticity strengthens and broadens due to the increasing in combustion heat release and the distortion of crossflow by transverse jet with increasing penetration height. The vorticity enhancement in the isolator will promote the turbulent mixing in the downstream combustor, which will further increase the combustion efficiency and thereby total heat release. The region with the most intense vorticity generation is in front of the upstream injector, corresponding to the static pressure plateau. The vortexes in the isolator are generally streamwise and in large scales, then break up to small scales and in more random orientation in the combustor. The breakup of large-scale vortexes to small-scale twisted vortexes occurs to the peak pressure location, i.e. around the upstream cavity for ϕ=0.8 while around the upstream injector for ϕ=1.0 and 1.2.

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V. References


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