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Characteristic of interior crack initiation and early growth for high cycle and very high cycle fatigue of a martensitic stainless steel



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ABSTRACT

In this paper, interior crack initiation and early growth are investigated to determine the high cycle and very high cycle fatigue of a martensitic stainless steel by constant and variable amplitude loading fatigue tests. It is shown that the tested material presents a very large fine granular area (FGA) size (72–176 μ m), and the value of the stress intensity factor range for FGA remains almost constant irrespective of the stress amplitude and the fatigue life. The equivalent crack growth rate in FGA is of the magnitude 10^{-13} - 10^{-11} m/cyc as determined by the "tree ring" patterns on the fracture surface under variable amplitude loading. Moreover, transmission electron microscopy shows both refined and coarse grains in the extracted samples beneath the FGA, i.e., there is no inevitable relationship between FGA morphology and refined grains beneath the FGA. Additionally, multi-site crack origins are observed under both constant and variable amplitude loadings. This indicates that the crack tends to initiate from the larger inclusion in the highly stressed region for the inclusion-induced fatigue failure.

1. Introduction

Very high cycle fatigue (VHCF) has drawn considerable attention in recent years [1–5]. For high-strength steels, the crack usually initiates from the interior inclusion, and the fracture surface often presents a fish-eye pattern with morphology of fine granular area (FGA) surrounding the inclusion [6,7]. This is also the case for the high cycle of some high-strength steels with relatively large fatigue life, such as GCr15 [8] and JIS SUJ2 [9]. It is generally considered that the FGA consumes most of the total fatigue life, especially for VHCF [10–12], although it has a very small size that usually ranges from approximately 10 to 80 μ m [13,14].

Many studies have shown that the stress intensity factor range at the front of the FGA remained almost constant corresponding to the threshold value $\Delta K_{\rm th}$ of the crack propagation [9,13–15]. Some observations beneath the FGA in the extracted samples indicate that the FGA is composed of a layer of nano-sized grains in high-carbon steel [16,17], medium-carbon steel [18], martensitic stainless steel, and duplex stainless steel [19].

Some methods have also been attempted to measure the crack growth rate in crack initiation and early growth region for VHCF. For example, Stanzl-Tschegg et al. [20] tested the tubular specimens with pre-notch in vacuum and ambient air by ultrasonic axial cycling for martensitic steels containing 12% chromium. By comparing the fractographic features between the crack growth specimens tested in vacuum and the fatigue specimen with fine granular and smooth areas of internal fish-eye morphology, they showed that the value of the crack growth rate was 10^{-12} m/cyc in FGA, 10^{-11} m/cyc in the fish-eye region outside the FGA, and 10^{-9} m/cyc in the region outside the fisheve. Ogawa et al. [21] quantified the crack growth rate in FGA and fisheve for SUJ2 steel by using the repeated two-step loading test. From the beach marks observed in the fish-eye region, they obtained the value of da/dN as 10^{-7} - 10^{-9} m/cyc. The crack growth rate in the FGA region was estimated as 10^{-13} - 10^{-14} m/cyc with the assumption that an ODA (i.e., FGA) of similar size as that observed in the constant amplitude test at the higher stress had been formed, and this ODA then increased to the size observed on the fracture surface after the subsequent lower stress without any effect of stress history. Sander et al. [22] used the arrest marks under variable amplitude loading to calculate the fatigue crack growth rate for 34CrNiMo6 steel in the fish-eye region, and the value of da/dN was obtained between 3×10^{-11} and 2×10^{-12} m/ cyc. However, they pointed out that no FGA was visible on the fracture surface, although the cracks nucleated predominately at the interior inclusions of the specimen and a fish-eye pattern was formed.

In this work, the interior crack initiation and early growth is further investigated for high cycle and VHCF of a martensitic stainless steel by constant and variable amplitude loading fatigue tests. The aim of the paper is to evaluate the characteristic of interior crack initiation and

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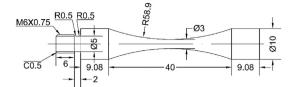


Fig. 1. Specimen shape and dimensions (in mm).

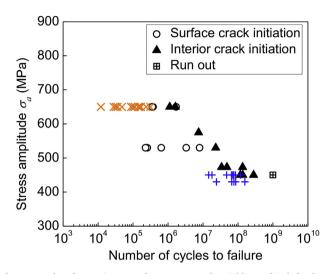


Fig. 2. S–N data for specimens under constant and variable amplitude loadings, in which the symbol "cross" denotes the cumulative cycles under higher stress amplitude and the symbol "plus" denotes the cumulative cycles under lower stress amplitude for the variable amplitude loading.

early growth in high cycle and VHCF regimes depending on the observations made from scanning electron microscopy (SEM) and transmission electron microscopy (TEM) studies.

2. Materials and methods

2.1. Materials

The material used in this study is a martensitic stainless steel (AISI630) with the chemical compositions 0.047C, 15.58 Cr, 3.65 Ni, 3.11 Cu, 0.74 Mn, 0.18 Nb, and 0.16 Mo in weight percent (Fe balance). Specimens were first heated at 1050 °C for 60 min and cooled in air, and then heated again at 850 °C for 3 h and oil-quenched; finally, they were

 Table 1

 Loading information of specimens under variable amplitude loading.

tempered for 4 h at 470 °C and air-cooled. The tensile strength was 1161 MPa, and the yield strength was 1130 MPa, the data of which were obtained from two cylindrical specimens of diameter 5 mm using the servohydraulic test system.

2.2. Methods

The fatigue test was conducted on a Shimadzu USF-2000 machine at a resonance of 20 kHz at room temperature in air with pulse of 200 ms and pause of 200 ms. The stress ratio R was -1. Compressive cold air was used to cool down the specimens during the fatigue test. The geometry of the specimen is shown in Fig. 1. The notch surface was ground and polished to eliminate the machine scratches before the fatigue test.

Both constant and variable amplitude loadings (repeated two-step loadings) were applied. Variable amplitude loading started from a block of lower stress amplitude $\sigma_{a,L} = 450$ MPa or 430 MPa with loading cycles $n_L = 2 \times 10^6$ or 3×10^6 and was then followed by a block of higher stress amplitude $\sigma_{a,H} = 650$ MPa with loading cycles $n_H = 4 \times 10^3$ except for two specimens that experienced first a large number of variable amplitude loadings (starting from a block of lower stress amplitude 400 MPa and followed by a block of higher stress amplitude 650 MPa). This process was repeated until the specimen failed or up to 10^9 cycles.

The fracture surfaces of the failed specimens were observed by SEM. Further, extracted cross-section samples were first prepared by the focused ion beam (FIB) technique and then observed by TEM with selected area diffraction (SAD) (diffraction area of 680 nm in diameter). The fracture surfaces of all extracted samples were protected by coating a thin layer of platinum before extraction.

3. Results and discussion

3.1. S–N data

Fig. 2 shows the S–N data for the specimens under constant and variable amplitude loadings. Detailed loading information for specimens under variable amplitude loading is given in Table 1. The fatigue data for specimens 1 and 2 experienced at first a large number of variable amplitude loadings, which are not included in Fig. 2. As shown in the figure, for constant amplitude loading, the specimens failed from both the surface and the interior of the specimen under higher stress and failed only from the interior of the specimen under lower stress (\leq 473 MPa). The fatigue life increased with decrease in the stress amplitude for the fatigue failure initiated from the interior of the specimens. For variable amplitude loading, the cumulative cycles (life

Specimen No.	$\sigma_{a,L}$ (MPa)	n_L (cycle)	$\sigma_{a,H}$ (MPa)	n_H (cycle)	Cumulative cycles at $\sigma_{a,L}$	Cumulative cycles at $\sigma_{a,E}$
1 ^a	450	$2.0 imes 10^6$	650	$4.0 imes 10^3$	$2.232 imes 10^7$	$4.4 imes 10^4$
2 ^a	450	$2.0 imes10^6$	650	$4.0 imes 10^3$	$1.389 imes 10^7$	$2.4 imes 10^4$
3	450	$2.0 imes10^6$	650	$4.0 imes 10^3$	$1.195 imes 10^8$	$2.4 imes 10^5$
4	450	$2.0 imes10^6$	650	$4.0 imes 10^3$	$8.473 imes 10^7$	1.7×10^5
5	450	$2.0 imes10^6$	650	$4.0 imes 10^3$	$7.60 imes 10^7$	$1.5 imes 10^5$
6	450	$2.0 imes10^6$	650	$4.0 imes 10^3$	$7.047 imes 10^7$	$1.4 imes 10^5$
7	450	$2.0 imes10^6$	650	$4.0 imes 10^3$	$1.455 imes 10^7$	$2.8 imes 10^4$
8	430	$2.0 imes10^6$	650	$4.0 imes 10^3$	1.572×10^{8}	$3.1 imes 10^5$
9	430	$3.0 imes10^6$	650	$4.0 imes 10^3$	8.565×10^{7}	1.1×10^{5}
10	430	$3.0 imes10^6$	650	$4.0 imes 10^3$	$7.60 imes 10^7$	$1.0 imes 10^5$
11	430	$3.0 imes10^6$	650	$4.0 imes 10^3$	$2.422 imes 10^7$	$3.2 imes10^4$
12	430	$3.0 imes10^6$	650	$4.0 imes 10^3$	6.617×10^{7}	$8.8 imes10^4$
13	450	$1.5 imes 10^7$	650	$1.2 imes 10^4$	1.802×10^{7}	$1.2 imes 10^4$
14	450	$1.5 imes 10^7$	650	$1.2 imes 10^4$	6.478×10^{7}	$4.8 imes10^4$
15	450	$1.5 imes 10^7$	650	$1.2 imes 10^4$	4.733×10^{7}	$3.6 imes 10^4$

^a Experiencing at first a number of variable amplitude loadings starting from a block of low-stress amplitude 400 MPa with 1.5×10^7 cycles and then followed by a block of high-stress amplitude 650 MPa with 1.2×10^4 cycles, which is 3.002×10^8 cycles for specimen 1 and 1.501×10^8 cycles for specimen 2.

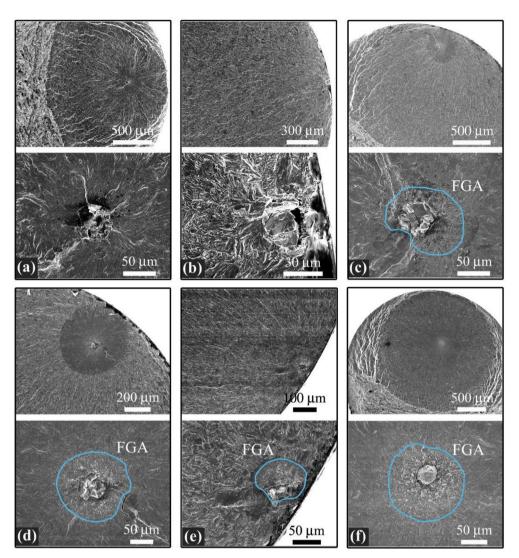


Fig. 3. SEM images for fracture surface of specimens under constant amplitude loading. (a) $\sigma_a = 650$ MPa, $N_f = 1.114 \times 10^6$; (b) $\sigma_a = 650$ MPa, $N_f = 1.621 \times 10^6$; (c) $\sigma_a = 575$ MPa, $N_f = 7.5 \times 10^6$; (d) $\sigma_a = 473$ MPa, $N_f = 4.816 \times 10^7$; (e) $\sigma_a = 473$ MPa, $N_f = 3.393 \times 10^7$; (f) $\sigma_a = 450$ MPa, $N_f = 1.362 \times 10^8$.

Table 2

Fatigue data, inclusion size, and FGA size for the specimens that failed from interior inclusions under constant amplitude loading.

Specimen No.	σ_a (MPa)	N_f (cycle)	<i>a</i> _{In} (μm)	$a_{\rm FGA}~(\mu { m m})$
1	650	1.114×10^{6}	47.4	-
2	650	1.621×10^{6}	31.9	-
3	575	$7.50 imes 10^6$	47.9	95.8
4	530	$2.316 imes 10^7$	48.6	107.3
5	473	1.353×10^{8}	34.3	96.1
6	473	4.816×10^{7}	54.4	136.4
7	473	3.393×10^7	38.9	71.9
8	450	$2.804 imes 10^8$	40.2	175.9
9	450	$1.362 imes 10^8$	33.9	129.7
10	450	$1.174 imes 10^8$	40.2	152.7

times) under lower stress amplitude were generally smaller than those under the identical constant amplitude loading. The result for the cumulative cycles under higher stress amplitude was similar compared to the result for those under identical constant amplitude loading. This indicates that higher stress in variable amplitude loading might result in shorter fatigue life for the specimens failed in the VHCF regime. The low stress (below the traditional fatigue limit defined at 10^7 cycles) in variable amplitude loading also might decrease the fatigue life of the specimens failed in high cycle fatigue regime.

3.2. SEM observation and analyses

3.2.1. Constant amplitude loading

The specimens under constant amplitude loading failed from the surface inclusion/defect or the interior inclusion. For the specimens that failed from the interior inclusion, the fracture surface under stress amplitude 650 MPa presented no FGA morphology, whereas the fracture surface under other stress amplitudes presented FGA morphology. Fig. 3 shows the fracture surfaces of some specimens with and without FGA that failed from interior inclusions.

The inclusion size a_{In} (square root of the projection area of the inclusion) and FGA size a_{FGA} (square root of the FGA area including the projection area of inclusion) were measured for specimens failed from interior inclusions, as listed in Table 2. As given in Table 2, the FGA size could be larger than 100 µm. This differs from the FGA size usually observed for high-strength steels, which is in tens of microns [13,14].

Fig. 4 shows the variation of inclusion size and FGA size on the fatigue life and stress amplitude. As shown in the figure, the inclusion size was independent of fatigue life and stress amplitude, although the FGA size seemed to increase with decrease in stress amplitude or increase in fatigue life.

Here, the variation of stress intensity factor range for FGA (i.e., ΔK_{FGA}) on the fatigue life and stress amplitude was also calculated, and the results are shown in Fig. 5, in which ΔK_{FGA} is calculated by

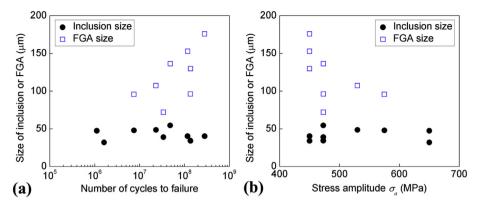


Fig. 4. Variation of inclusion size and FGA size with (a) fatigue life and (b) stress amplitude.

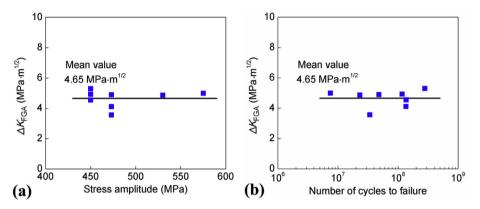


Fig. 5. Variation of ΔK_{FGA} with (a) fatigue life and (b) stress amplitude.

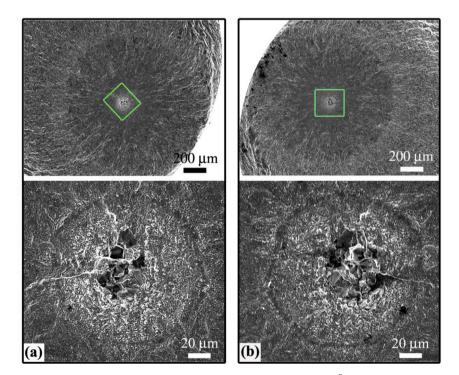


Fig. 6. SEM images of the mated fracture surfaces for specimen 14 failed at a total fatigue life of 6.483×10^7 under variable amplitude loading. (a) One side; (b) The other side.

 $\Delta K_{\rm FGA} = 0.5\sigma_a \sqrt{\pi a_{\rm FGA}}$ [6,13,23]. As shown in the figure, the value of $\Delta K_{\rm FGA}$ remained almost a constant, as reported for the high-strength steels with FGA size in tens of microns [13,14]. The value of $\Delta K_{\rm FGA}$ was also very close to the threshold value of crack propagation, i.e.,

 $4.5 \text{ MPa} \cdot \text{m}^{1/2}$, available for a similar steel (SUS 630) with yield strength 1251 MPa and tensile strength 1368 MPa reported in the literature [24,25].

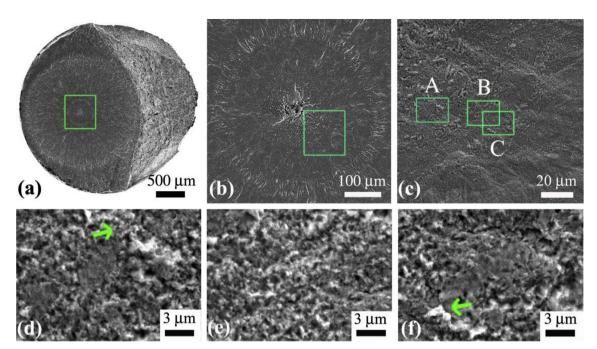


Fig. 7. SEM images of fracture surface for specimen 6 failed at a total fatigue life of 7.061×10^7 under variable amplitude loading. (a)–(c) Low magnification for an overall morphology; (d)–(f) High magnification for local areas in rectangles A, B, and C in (c), the arrows denote the granular feature in the relatively smooth area.

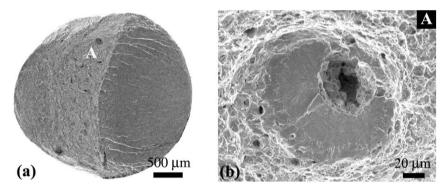


Fig. 8. SEM images of the fracture surface for the specimen failed at $\sigma_a = 650$ MPa and $N_f = 1.70 \times 10^6$ with multi-site crack initiations under constant amplitude loading. (a) Morphology of the fracture surface; (b) Morphology of secondary crack initiation site.

3.2.2. Variable amplitude loading

For variable amplitude loading, all the specimens failed from interior inclusions except one specimen (specimen 7 in Table 1), which failed from surface inclusion. The fracture surface of some specimens presented discernible traces because of the sequence of different cyclic stress amplitudes, as shown in Fig. 6. Based on the result shown in Fig. 4b under constant amplitude loading, the specimens under constant stress amplitude of 650 MPa barely presented FGA morphology. Therefore, the smooth annular area between rough areas shown in Fig. 6 corresponds to the loading sequence of the higher stress amplitude $\sigma_{a,H} = 650$ MPa. Fig. 6 indicates that the mated fracture surfaces of failed specimens have very similar morphology, i.e., the rough area or smooth area presents in the mated locations. The observation of the fracture surface for some other failed specimens also shows this result.

Particularly, some fracture surfaces present "tree ring"-like patterns, which paves the way to obtain insights into the involution process of interior crack initiation and early growth. The typical fracture morphology with "tree ring" pattern is shown in Fig. 7. Based on the result shown in Fig. 4b, the rough area (i.e., the granular feature) between relatively smooth areas shown in Fig. 7c corresponds to the loading sequence of the lower stress amplitude $\sigma_{a,L} = 450$ MPa. Fig. 7d–f shows the magnifications of the local areas for the rough and smooth areas

shown in Fig. 7c, respectively. As shown in Fig. 7e, the granular morphology is clear under lower stress amplitude. It was also observed that there is a granular feature in some local regions for the relatively smooth traces, as illustrated in Fig. 7d and f. This indicates that the crack extension in crack initiation and early growth stage occurs first in some local and weak regions.

Combined with the variable loading sequence, it takes 2×10^6 or 3×10^6 cycles for the rough area (i.e., the FGA morphology) between relatively smooth ones at the fracture with "tree ring" patterns, while it takes only 4×10^3 cycles for the relatively smooth traces. The widths of the rough and the relatively smooth traces were comparable in "tree ring" patterns, as shown in Fig. 7b and c. Compared with the fracture surface with FGA morphology under constant stress amplitude, it could be concluded that the FGA consumes most of the fatigue life in VHCF regime. The "tree ring" patterns at the fracture surface associated with the variable loading sequence also indicate that the formation of the rough area between relatively smooth ones consumes 2×10^6 or 3×10^6 cycles. This suggests that the rough area (i.e., the FGA morphology) could be formed with less than 1 million cycles.

3.2.3. Multi-sites crack initiation and analyses

It is observed that some fracture surfaces presented characteristic of

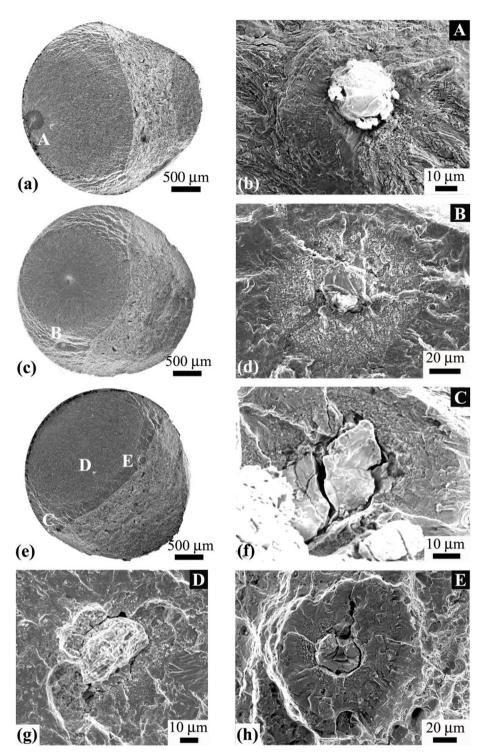
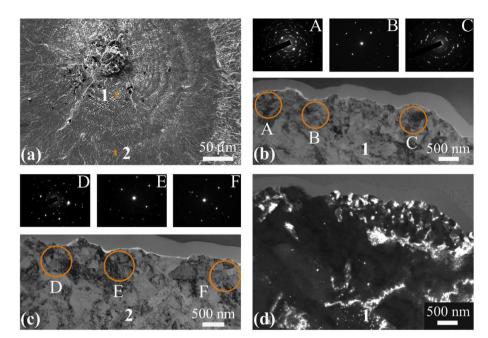


Fig. 9. SEM images of the fracture surface for specimens with multi-site crack initiations under variable amplitude loading. (a) and (b): Morphology of the fracture surface and the secondary crack initiation site for specimen 2, respectively; (c) and (d): Morphology of the fracture surface and the secondary crack initiation site for specimens 10, respectively; (e)–(h): Morphology of the fracture surface and the secondary crack initiation site for specimens 10, respectively; (e)–(h): Morphology of the fracture surface and the secondary crack initiation site for specimens 10, respectively; (e)–(h): Morphology of the fracture surface and the secondary crack initiation site for specimens 10, respectively; (e)–(h): Morphology of the fracture surface and the secondary crack initiation site for specimens 10, respectively; (e)–(h): Morphology of the fracture surface and the secondary crack initiation site for specimens 10, respectively; (e)–(h): Morphology of the fracture surface and the secondary crack initiation site for specimens 10, respectively; (e)–(h): Morphology of the fracture surface and the secondary crack initiation site for specimens 10, respectively; (e)–(h): Morphology of the fracture surface and the secondary crack initiation site for specimens 10, respectively.

multi-site crack initiation. Fig. 8 shows the specimen with surface failure mode and interior secondary crack initiation site under constant amplitude loading. It provides evidence of the competition between surface crack initiation and interior crack initiation in the fatigue of high-strength steels, namely, that the surface failure mode occurs when the fatigue life initiated from the surface is smaller than that initiated from the interior of the specimen; otherwise, the interior failure mode occurs.

Fig. 9 shows the specimens with interior failure mode and secondary

crack initiation sites under variable amplitude loading, which provides evidence that there might be multiple crack origins in the specimens. The crack origin that needs the shortest cyclic loadings to result in the fatigue failure will develop to the main crack. Here, the inclusion sizes of the crack origins were also measured and compared for specimens 2 and 10 in Fig. 9(a)-9(d). For specimen 2, the inclusion size was 36.3 µm for the main crack origin and 27.0 µm for the secondary crack origin. For specimen 10, the inclusion size was 37.5 µm for the main crack origin and 29.8 µm for the secondary crack origin. Both the inclusion C. Sun, et al.



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Fig. 10. SEM and TEM images of extracted crosssection samples cut along the loading direction for specimen 9 failed at a total fatigue life of 8.576×10^7 under variable amplitude loading. (a) SEM image of extracted cross-section locations; (b) and (c) Bright-field TEM images of extracted crosssection samples 1 and 2, respectively; the cycles indicate the locations where the SAD diffractions are obtained; (d) Dark-field TEM image of extracted cross-section sample 1.

sizes of the main crack origins were larger than those of the secondary crack origins, hence indicating that the crack tends to initiate from the larger inclusion under the identical loading condition.

3.3. TEM observation and analyses

Fig. 10 shows the SEM and TEM images of the extracted cross-section samples from the specimen with "tree ring" pattern under variable amplitude loading. Sample 1 locates in the rough area close to the crack origin (i.e., the inclusion). Sample 2 locates in the rough area by the lower stress amplitude, which is more than $100 \,\mu\text{m}$ from the crack origin.

It is seen from the TEM image of sample 1 in Fig. 10b, the SAD patterns composed of numerous tiny spots or diffused rings in locations A and C suggest polycrystalline structures consisting of many smaller sized grains (refined grains), while the SAD pattern of isolated spots in location B suggests just a few grains within the diffraction area. The dark field TEM image of sample 1 is given in Fig. 10d, in which the scattered small bright humps close to the fracture surface denote the refined grains. This indicates that the grain refinement regions are discontinuous beneath the rough area (i.e., FGA). The TEM image of sample 3 beneath the grain refinement regions are local beneath FGA, i.e., the refined grain does not always exist beneath FGA.

3.4. Equivalent crack growth rate in FGA

On the basis of the "tree ring" pattern in the fracture surface, the equivalent crack growth rate in FGA (i.e., crack initiation rate) could be estimated. The cracks after the high- and low-stress sequences are both approximately seen as concentric mode-I internal penny cracks in an infinite solid under a uniform remote tensile stress, and a direction of crack extension with relative clear marks in the SEM image is considered, as illustrated in Fig. 11a, 11c, 11e, 11g, and 11i. The radii of these concentric internal penny cracks are measured along this crack extension direction by using IPP software, as shown in Fig. 11b, 11d, 11f, 11h, and 11j, where r_1, r_3, \dots denote the radii of penny cracks after the lower stress sequence. The values of measured radii are listed in Table 3.

The (equivalent) crack growth rate da/dN and the associated stress intensity factor range ΔK are calculated by $(r_{i+1} - r_i)/n_H$ and

 $2\sigma_{a,H}\sqrt{2(r_i + r_{i+1})/\pi}$ for the higher stress, and $(r_{i+2} - r_{i+1})/n_L$ and $2\sigma_{a,L}\sqrt{2(r_{i+1} + r_{i+2})/\pi}$ for the lower stress, respectively, where i = 1, 3, 5. The results are plotted in Fig. 12. It is seen that the crack growth rate in the smooth area is larger than 10^{-10} m/cyc (magnitude of crack growth rate corresponding to the traditional crack propagation threshold), whereas the equivalent crack growth rate in the rough area (i.e., FGA morphology under constant stress amplitude) is much lower than 10^{-10} m/cyc, i.e., the mean crack advance in FGA is far below one lattice spacing per cycle. This indicates that the crack growth in FGA is discrete, i.e., the crack growth in FGA does not extend in all directions in one fatigue cycle, which occurs first in some local regions along the crack extension direction for a number of cycles. This is in agreement with the SEM observation result that there is a granular feature in some little local regions at the smooth traces due to the higher stress amplitude shown in Fig. 7d and f.

Considering that the equivalent crack growth rate in the rough area (i.e., FGA) has the tendency to increase with an increase in the stress intensify factor range, an attempt is made to extrapolate the equivalent crack growth rate in FGA close to the inclusion by the linear regression of the measured equivalent crack growth rate in Fig. 12. The inclusions are seen as an internal penny crack with radius $r_{\rm In} = \sqrt{area_{\rm In}/\pi}$ (*area_{\rm In* is the projection area of the inclusion), and the stress intensity factor range for the inclusion is calculated as $4\sigma_a \sqrt{r_{\rm In}/\pi}$. The inclusion sizes under constant amplitude $\sigma_a = 450$ MPa are used for analysis, the values of stress intensity factor range for which are between 4.44 and 4.84 MPa $\cdot m^{1/2}$. From the results shown in Fig. 12, the equivalent crack growth rate in FGA close to the inclusion might be lower than 10^{-12} m/ cyc. Therefore, the equivalent crack growth rate in FGA might be of the magnitude $10^{-13} \cdot 10^{-11}$ m/cyc.

4. Conclusions

This paper investigates the interior crack initiation and early growth of a martensitic stainless steel in high cycle and VHCF regimes. The main results are summarized as follows:

- (1) The FGA size of the present material could be larger than $100 \,\mu$ m, which differs from the usually observed FGA size in tens of microns for high-strength steels. The value of ΔK_{FGA} remains almost a constant independent of the stress amplitude and the fatigue life.
- (2) The crack growth in FGA is discrete, which occurs first in some local

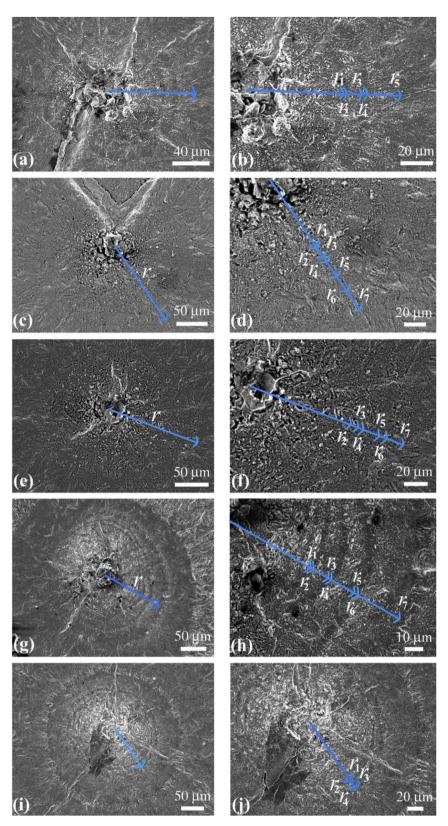


Fig. 11. Images of measurement for radii of penny cracks. (a) and (b): Specimen 2; (c) and (d): Specimen 3; (e) and (f): Specimen 6; (g) and (h): Specimen 9; (i) and (j): Specimen 10.

regions along the crack extension direction for a number of cycles. The equivalent crack growth rate in crack initiation and early growth stage (i.e. FGA) is of the magnitude 10^{-13} - 10^{-11} m/cyc and is in positive correlation with the stress intensity factor range of the

initiated cracks.

(3) TEM observation indicates that the refined grain does not always exist beneath FGA, i.e., there is no inevitable relation between the FGA morphology and the grain refinement beneath FGA.

Table 3

Values of measured radii for penny cracks shown in Fig. 11.

Specimen No.	2	3	6	9	10
r ₁ (μm)	60.67	74.37	-	71.96	88.36
r ₂ (μm)	62.99	77.25	90.84	73.47	91.55
r ₃ (μm)	72.31	87.04	97.05	82.87	99.81
r ₄ (μm)	75.86	92.53	102.38	84.74	103.05
r ₅ (μm)	96.3	108.72	115.81	98.84	-
r ₆ (μm)	-	124.22	123.05	101.04	-
r ₇ (μm)	-	145.13	137.96	126.62	-

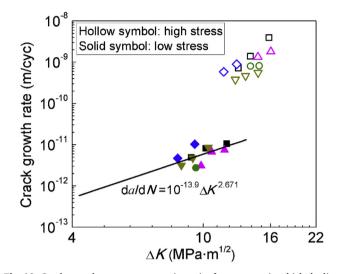


Fig. 12. Crack growth rate versus stress intensity factor range, in which the line denotes the linear regression result of the crack growth rate due to lower stress amplitude.

(4) Multi-site crack initiations are observed at the fracture surfaces of some specimens, which show the competition between the surface crack initiation and interior crack initiation, and the competition for different interior crack initiations. It indicates that, for the inclusion-induced fatigue failure, the crack tends to initiate from the larger inclusion in the highly stressed region.

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