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The time-temperature-maturity relationship: A chemical kinetic model of kerogen evolution based on a developed molecule-maturity index

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ABSTRACT

Kerogen maturity is an important indicator for evaluating source rocks. We propose a kerogen maturity index (molecule-maturity index, MMI) based on the changes in the molecular structure of organic matter during thermal evolution. The MMI has a positive correlation with vitrinite reflectance. Molecular dynamics simulations indicate that the weight loss is with a positive linear correlation with the MMI, demonstrating the ability of the index to reflect the hydrocarbon generation of organic matter. In addition, a new conversion is introduced by the MMI to analyze the kinetics of kerogen thermal evolution. The activation energy is expressed as a continuous function of the MMI linking by the new conversion. The activation energy was calculated at the isoconversional points of previous conversion, which was not defined as a continuous function before. A linear relationship between the activation energy of kerogen is observed, and a new chemical kinetic model of kerogen thermal maturity is established based on the MMI (kinetic model of the maturity evolution, MEKM). The MEKM equation has a simple form and is convenient for engineering applications. Our findings provide insights into the kinetics of kerogen thermal maturity.

1. Introduction

Kerogen is the most important form of organic carbon on the planet. Kerogen gradually matures and generates oil/gas after being exposed for a long geological period as chemical evolution of the molecular structure occurs. During this time, the reservoir environment changes [1,2]. In addition, kerogen is an extremely complex polymer, consisting of an amorphous porous carbon skeleton [3-5]. The micro/nanopores serve as the primary storage and circulation channels for shale gas [6]. Changes in the pore structure during kerogen evolution are important for understanding the accumulation and migration of shale oil/gas [7,8]. During the pyrolysis of kerogen, solids decompose into gas to form micropores. Micropores develop into microcracks under the action of geostress and pore pressure. The microcracks will cause the asymptotic failure of kerogen [9]. In addition, the chemical transformation caused by the kerogen evolution causes a change from a plastic to a brittle rupture mechanism, affecting the hydraulic fracturing of kerogen [3]. Kerogen-rich rock closes rapidly during hydraulic fracturing because kerogen-rich shale exhibits high tensile strength. The reason is that kerogen exhibits strain softening under tension [10]. Therefore, the hydraulic fracturing process of kerogen-rich shale requires large amount of fracturing fluid [11]. The micro-cracks and changes in the mechanical properties of kerogen caused by its evolution affect the hydraulic fracturing process of the rock formation [12,13]. The degree of the metamorphism of organic matter (OM) is referred to as maturity, which is a reliable indicator of source rocks. In-situ ripening of kerogen can be achieved through in situ conversion process (ICP), ElectrofracTM and other method to achieve efficient exploitation of oil and gas resources. Technical methods of clean gasification of organic energy have been investigated in depth [14–16]. Therefore, it is important to study the evolution of maturity to understand the generation of shale gas and provide guidance for hydraulic fracturing.

As one of the most important evaluation indices, the kerogen-based evaluation index primarily depends on the organic geochemistry, organic petrology and mineralogy, and chemical kinetics of a site [17]. Optical indices, such as the vitrinite reflectance (VR), microsome reflectance, bitumen reflectance, and gravel reflectance, have been used in organic petrology to characterize the maturity [18–21]; the VR is one of the most reliable and widely used index [22,23]. The vitrinite is widespread in various sedimentary rocks, and is rich in content. The VR changes systematically with the increase of burial temperature [23]. The VR curve is corrected by the algae fluorescence parameters (wavelength of the maximum intensity (λ_{max}), spectral maxima, emission intensities, etc.) [24,25]. The change in the VR is used as a measure of

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Nomenclature		$M_{\rm gas/oil}$	the mass of oil and gas (g)
		R_m	the rate of change of the MMI
$r_{ m H/C}$	the atomic ratios of H/C	Time ste	ep 0.25 fs/step
r _{O/C}	the atomic ratios of O/C	t*	step $\times 10^{-4}$ (2.5 $\times 10^{-12}$ s)
$r_{\rm N/C}$	the atomic ratios of N/C	x	the conversion
r _{s/C}	the atomic ratios of S/C	k	the rate constant (s^{-1})
т	the molecule-maturity index (MMI)	t	time (s)
Ro	the vitrinite reflectance (%)	ν	the pre-exponential factor (s^{-1})
w	the weight loss as well as the portion of oil/gas in mass	Ε	the apparent activation energy (J/mol)
λ	the slope of w-m	R	the gas constant (J/mol/K)
$M_{ m in}$	the initial mass of kerogen (g)	Т	temperature (K)

coal conversion in the gasification experiment of coal samples [26]. Zhang et al. used the VR as a benchmark to evaluate the maturity and established the relationship between the parameters of the Raman spectrum (the position of D band (P_D), full width at half maximum of G band (FWHMG)) and the VR [27]. Another standard detection method is the use of organic geochemistry. T_{max} at which maximum hydrocarbon generation occurs is another commonly used maturity index, because it increases with increasing maturity. T_{max} is the maximum S2 peak temperature obtained by Rock-Eval (RE) pyrolysis [28]. Hai et al. analyzed T_{max} and detected the gas products by combining thermogravimetric analysis (TGA), derivative thermogravimetry (DTG), differential scanning calorimetry (DSC), online gas analyzer and offline gas chromatography (GC) analyzer [29]. However, the VR can only be used in kerogen where huminite/vitrinite phytoclasts are present. The method is not suitable for pre-Silurian shales or marine shale (such as sapropelic sediments) lacking huminite/vitrinite particles [30,31]. The VR suppression is observed in the hydrogen-rich samples and in lacustrine shales under over-pressure. Therefore, the VR is abnormal in the Dongying sample which includes type I and part type II kerogen [32]. The use of T_{max} is limited in overmature kerogen because S2 peak of overmature kerogen is weak, so T_{max} is inaccurate [33]. The mineral matrix in the kerogen will cause an abnormally high T_{max} , whereas the soluble organic matter will cause a low T_{max} [34]. The hydrogen/ carbon (H/C) atomic ratio, oxygen/carbon (O/C) atomic ratio, and aromatic/aliphatic ratios were also used to study the maturity. The corrected organic carbon mass content (COC) was also used as a maturity index [35]. Elemental analysis (EA) is typically performed to determine the maturity by defining the evolution path of the kerogen chemical structure with increasing burial depth [36]. The VR value of kerogen is correlated with the H/C and O/C atomic ratios of kerogen, and the relationship is obtained by experimental fitting [37,38]. The type I and type II H/C atomic ratios of pyrolyzed kerogen are excellent indicators of the thermal maturity of kerogen because the ratios are related to the degree of thermal conversion of OM [39]. Sinces different types of kerogen have different H/C ratios (Type I > Type II > Type III), the atomic ratio is used to describe the maturity based on known kerogen types. The initial and current values of the H/C ratios of the kerogen samples are required to determine the kerogen conversion. Type II kerogen follows the trend of the H/C and O/C atomic ratios in the thermal maturity process [40]. The OM thermal maturity is a continuous process of side-chain detachment and condensation of OM. It is convenient to report the continuous change in the molecular structure of kerogen during its thermal maturity process using simulations. The molecular composition to characterize the maturity is the basis for the thermal evolution of the macromolecular structure and is commonly determined in addition to the T_{max} and VR. As the activation energy is related to molecular structure, functional relationship between the maturity index we proposed and the activation energy can be easily established comparing with the maturity index using the VR or T_{max} . Therefore, it is of great significance to define a physical maturity index and to investigate its evolution based on the analysis of kerogen molecular elements.

Chemical kinetic models of kerogen pyrolysis can be used to predict the maturity evolution and the hydrocarbon generation of kerogen. The models include the first-order reaction model, independent reaction model, multi-stage first-order reaction model, n-order reaction model, parallel first-order reaction model, pseudo-reaction model, and the Friedman model [28,41-43]. TGA and DSC have been performed to analyze the pyrolysis characteristics and kinetic parameters of kerogen [44-47]. The reactivity of biomass in different atmospheres was investigated using TGA and DSC techniques. An n-order reaction equation was used to study the kinetic decomposition process of cellulose [48]. The first-order kinetic model has been considered sufficient to characterize the thermal evolution of the Green River oil shale [49]. The parallel first-order reaction model was used to evaluate the accuracy of the TGA and RE methods, and the latter proved to be more accurate [50]. The catalytic effect of water on the pyrolysis has been investigated using the consecutive first-order reaction model [51]. A multi-stage parallel reaction model was used, and the thermal stability of oil shale during pyrolysis was determined by changing the heating rate [52]. Currently, kinetic models that include the weight loss, heat endothermic/exothermic rate, and hydrocarbon generation rate are used to characterize the reaction rate [53]. The activation energy is always calculated using kinetic models which is obtained by hydrocarbon generation/weight loss, whose calculation is not associated with kerogen components. Moreover, in previous models of changes in the activation energy during conversion, the activation energy was calculated at the isoconversional points of the conversion [54]. However, the activation energy is related to the molecular structure. In the index we proposed in this study, the changes in the activation energy resulting from changed in the kerogen structure are obtained, and a continuous equation between the activation energy and maturity is established through the conversion introduced by maturity. We can establish a kinetic equation based on the thermal evolution of kerogen molecular structure.

In this study, a maturity index of kerogen based on the evolution of the elemental content is established (molecule-maturity index (MMI). We use experiments to investigate the temperature-dependent elemental composition changes of OM to obtain the relationship between the MMI and VR. The relationship between the MMI and the weight loss is obtained by simulations and experiments. A kinetic model of the maturity index is proposed under isothermal conditions, and the evolution of the activation energy is established based on the change in the macromolecular structure. The kinetic equation is highly concise and convenient for engineering application, which is used in choosing the temperature and time for artificial maturity of kerogen in future. Our findings provide insights into the thermal evolution laws of kerogen and facilitate the prediction of oil and gas production for artificial maturity.

2. Methods

2.1. Construction of the kerogen molecule using experiments and simulations

The burial depth of kerogen is about 3000 m from Ordos Basin. And the sample is obtained by GBT 19144-2010 (insoluble organic kerogen in sedimentary rocks) method. Soluble organic matter and minerals are removed. The atomic ratios of C, H, O, N, and S in kerogen were obtained by EA (Thermo fisher Flash 2000) and X-ray photoelectron spectroscopy (XPS, ESCALab220i-XL). A computation multi-peak resolution method was performed by XPSPEAK41 to analyze the XPS spectra to obtain the chemical states and quantitative relationships of the elements in the kerogen. Under X-ray excitation, the energy-level splitting is generated in 2p layer electrons of S due to spin-orbit coupling (2p1/2 and 2p3/2). For example, N and S exist in the form of amino, thioether, etc. The functional groups of the kerogen molecule were determined by Fourier-transform infrared (FT-IR) spectroscopy, and the relative content was qualitatively characterized by the peak intensity. The aromaticity, aliphaticity, branching degree of the alkyl chain and the average aliphatic chain lengths were obtained by crosspolarization/magic angle spinning (CP/MAS) ¹³C solid nuclear magnetic resonance (¹³C NMR) spectrum technology; subsequently, the kerogen carbon skeleton was established. The methods and instruments used in the experiments are listed in Table 1.

The process of determining the average molecular structure of the kerogen is shown in Fig. 1: first, the aromatic rings and the condensed aromatic rings are the basic units, which are connected by the alkyl side chain. The contents of aromatic C and aliphatic C are determined by the XPS spectra and the ¹³C NMR spectrum, and the ratio of methylene C, protonic aromatic C, etc. are obtained from the ¹³C NMR spectrum. Then, the O. N. and S atoms are distributed in the carbon skeleton based on the heteroatom chemical state information obtained from XPS. A two-dimensional (2D) macromolecule is constructed. Subsequently, the ¹³C NMR spectrum of 2D molecule is predicted by the MestReNova software suite to verify the accuracy of the molecule. The experimental and calculation results are compared. The 2D molecular structure is continuously adjusted until the spectrum is consistent with that of the experiment. Finally, a reliable average molecular structure of kerogen is obtained. The 2D kerogen macromolecule is optimized by molecular mechanics and an annealing algorithm, to obtain a three-dimensional minimum energy configuration. The structure energy minimization process was implemented in the Materials Studio/Forcite module. The specific process is described in Ref. [55]. The kerogen macromolecule is used to study the pyrolysis of kerogen using reactive force field-molecular dynamics (Reaxff-MD). The reaction mechanism, oil/gas content, residue quality and molecular structure can be obtained to use in the reaction kinetic models.

2.2. Simulations of kerogen pyrolysis

Kerogen evolved during a long geological process. Molecular dynamics (MD) simulation of the reaction force field was performed to calculate the process of bond breaking and generation in the chemical reactions (Fig. A1) [56–58]. A heating strategy is generally used to ensure that the kerogen pyrolysis occurs on picosecond time scale.

Thus, the simulation temperature is much higher than the experimental temperature. First, we used pyrolysis-gas chromatography-mass spectrometry (PY-GC-MS) to analyze the kerogen pyrolysis and demonstrate that ReaxFF-MD simulations can be used for kerogen pyrolysis. The pyrolysis products include CH₄, H₂, alkanes, alkenes, aromatic cluster structure and fatty acids. The types of pyrolysis products obtained from the simulations are the same as those obtained from the experiment. However, since the experiments are conducted in an open system and the temperature is lower than that of the simulation, more long chains (C₆₊) are obtained in the experiment, and more short chains are obtained in the simulation. The intermediate and final products of kerogen obtained from the Reaxff-MD simulation are also similar to that of GC-MS in the previous study [59]. Second, an accelerated Reaxff-MD simulation is used to compare the proportional relationship between the gas products and residue. The mass fractions of CH₄, C₂ and the residue are 0.0039, 0.0044, and 0.81, respectively in the pyrolysis experiment and 0.0046, 0.0053, and 0.73, respectively in the simulation. The higher residue fraction in the experiment is attributed to the impurities in the kerogen. The experimental and simulation results are very close. Third, the dehydrogenation reaction, long chain cleavage, and CO₂ generation by removing the carboxyl functional groups were obtained from the simulation. The results were consistent with the reaction mechanism obtained in previous experiments, and the simulation results are shown in Fig. A1. Salmon et al. found that the thermal decomposition process of Morwell coal obtained by ReaxFF-MD was in good agreement with that of the experiment, indicating that the method can be applied to complex OM [60]. Finally, the activation energy and pre-exponential factor were obtained using Reaxff-MD to simulate the pyrolysis of *n*-dodecane, and the results were similar to the experimental results. In addition, when the model obtained through macro experiments was mapped to the time length and temperature using ReaxFF-MD, a simple comparison between the kinetic model and the ReaxFF simulation results at different temperatures was used to determine the conversion rate of hydrocarbons; satisfactory results are obtained [61]. Although the simulation temperature and time scale were different from those of the experiments, the simulation results could be compared with the experimental results. In addition, the radical reaction mechanism cannot be obtained experimentally [62]. The temperature is the main factor affecting pyrolysis, and different temperatures have a significant influence on the pyrolysis reaction. Therefore, we used a large temperature range in the simulation. In addition, this work is focused on the evolution of pyrolysis residues at different temperatures. In the simulations we can easily obtain the structure and composition changes of the kerogen residues at different temperatures. Since the simulation temperature range is large, we extend the law of OM evolution to natural or experimental temperatures. The force field was HCONSB.ff, which has been used in polymer systems, such as coal pyrolysis. The kerogen molecule was placed in a large lattice (70 \times 70 \times 70 ų). A 2 \times 2 \times 1 supercell of kerogen molecules was generated to ensure appropriate simulation results. The supercell had 6536 atoms, as shown in Fig. 2. The MD simulations were performed using the NVT (Velocity Verlet + Berendsen) ensemble, and periodic boundary conditions (PBC) were used. Since the temperature is the most important factor affecting the reaction rate of kerogen, we investigated the effect of temperature on the evolution of kerogen using constant temperature simulations in the range of 1900-2800 K. The

Table 1

Th	ie met	hods	and	instruments	used	to	construct	the	kerogen	mole	ecul	e.
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Experiment	Instrument	Analysis performed	Software	Results
XPS	ESCALab220i-XL	Peak splitting	XPSPEAK41	Chemical states
EA	Thermo fisher Flash 2000	–	-	Element content
¹³ C NMR	BRUKER AVANCE III 400 M	Peak splitting	MestReNova	Carbon skeleton information
FT-IR	Nicolet 6700	–	-	Functional groups



Fig. 1. The flow chart of kerogen molecular structure analysis.



Fig. 2. The macromolecular supercell.

temperature interval of each simulation was 100 K, and the time step was 400,000 (100 ps).

3. Results and discussion

3.1. The molecule-maturity index

3.1.1. Experimental results of kerogen molecular information

We briefly describe the spectra results obtained by the experiments, because they have been systematically described in our previous paper for the construction of kerogen molecules [55]. The kerogen sample is a type III kerogen based on the van Krevelen diagram; it is at the catagenetic stage. The atomic ratios of H/C and O/C are about 0.86 and 0.12-0.15, respectively. By FT-IR spectrum of kerogen, the functional groups contain hydroxyl, aromatic, alkane, ether, aldehyde/ketone, carboxylic, aldehyde, and amidogen. By the overlapping peak resolution of ¹³C NMR spectrum, the C skeleton information is obtained. The C atom contents of methyl, methylene, methine/quaternary, oxy-Methylene, oxy-Methine/oxy-quaternary, ortho-Oxyaromatic protonated, ortho-Oxyaromatic branched, aromatic protonated, bridging ring junction/aromatic branched, oxy-aromatic, and carboxyl/carbonyl are 4.0%, 22%, 12%, 1.5%, 2.8%, 2.5%, 11%, 20%, 21%, 0.5%, and 1.8%, respectively. The elemental states of C contain aromatic hydrocarbon (37.38%), aliphatic hydrocarbon (48.64%), ether/alcohol (6.31%), carbonyl/O-C-O (1.80%), ester/carboxyl (5.87%)); these of O contain ester/carbonyl (52.72%), ether/hydroxy (31.47%), ester/carboxyl (15.81%)); these of N contain nitrile (56.93%), pyrrole (32.59%), amino(10.48%)); and these of S contain mercaptan/thioether (44.28%), thiophene (15.26%), sulfoxide (4.35%), sulfone (36.11%)).

The aromaticity degree, aliphaticity degree, branching degree and average aliphatic chain length are 55.9%, 42.3%, 28.4% and 3, respectively. The average molecular formula is about $C_{100}H_{86}O_{13}NS_{0.8}$. The macromolecular structure of the kerogen was constructed based on the experimental results, and the rationality of the structure has been verified in Ref. [55]. The Reaxff-MD was performed to study the thermal evolution of kerogen by the macromolecule (Fig. 2).

3.1.2. The definition of the molecule-maturity index

During the evolution of kerogen for geological or artificial maturity, the H/C and O/C atomic ratios decrease, and the maturity of kerogen increase along with oil/gas generation. Fig. 3 shows the evolution of the kerogen macromolecules at different temperatures based on the kerogen molecule C₈₅₃H₇₅₆N₈O₁₁₅S₆, which is type III kerogen from the Ordos basin [55]. Under the combined action of time and temperature, pyrolysis of kerogen occurs, and the evolution of the H/C and O/C atomic ratios in the residue (C_{40\,+}\, molecules) is obtained. The O/C and H/C atomic ratios in the kerogen decrease as the pyrolysis proceeds, which means the burial depth and maturity increase in the van Krevelen diagram. The result indicates the O/C and H/C atomic ratios change the pathway of the geological maturity rather than that of the laboratory pyrolysis. However, the temperatures of the simulations are closer to the lab temperatures. This may be due to the fact that no oxygen was injected during the simulations and the pyrolysis products were always in the simulation systems. Compared with the experiment in an open system, in the simulation system, there is material exchange with the outside world. In addition, during the cracking process, gas molecules are continuously generated and the pressure increases at high temperatures. Monthioux et al. [35] found that the experimental results of artificial maturity were qualitatively similar to those of natural systems in a closed and confined system under high temperature. Thus, the simulation pathway is closer to the geological process. With the increase in the temperature, the O/C and H/C atomic ratios of the residue approach the origin (the black line in Fig. 3), which indicates that the kerogen evolution and maturity are accelerated at high temperatures.

The decline rates of the H/C and O/C atomic ratios are both positively related to the temperature, as shown in Fig. 4(a) and (b).

Therefore, the H/C and O/C atomic ratios can be used to predict the maturity. Because the chemical composition of kerogen affects its oil–gas potential and mechanical properties, it is necessary to define a maturity index of the kerogen based on the elemental composition of the molecule. Thus, the atomic ratios of H/C and O/C are used to characterize the maturity. However, to date, few studies have focused on the quantitative maturity index based on the molecular structure; therefore, we define the index as follows:

$$m = \frac{1}{1 + r_{\rm H/C} + r_{\rm O/C} + r_{\rm N/C} + r_{\rm S/C}}$$
(1)

to characterize the maturity of kerogen. The 1, $r_{\rm H/C}$, $r_{\rm O/C}$, $r_{\rm N/C}$ and $r_{S/C}$ are the atomic ratios of C/C, H/C, O/C, nitrogen/carbon (N/C) and sulfur/carbon (S/C), respectively. As shown in Fig. 4(c) and (d), The N/ C and S/C atomic ratios in the residue decrease over time. However, the N/C and S/C atomic ratios exhibit significant fluctuations with increasing temperature and increasing time. In particular, the S/C atomic ratio fluctuates greatly between the 150,000th and 390,000th steps (Fig. 4(d)). There exist very few N and S atoms in kerogen, and there is an order of magnitude difference between the number of N and S atoms and that of the H and O atoms. In addition, the van Krevelen diagram shows only the H/C and O/C atomic ratios; these are used to define the type of kerogen. The content of H atoms in the kerogen affects the hydrocarbon generation. The content of O atoms is directly related to the formation of carbon dioxide. When the S/C and N/C atomic ratios are ignored in Eq. (1), the simplified MMI using the atomic ratios is written as follows:

$$m = \frac{1}{1 + r_{\rm H/C} + r_{\rm O/C}}$$
(2)

Since the index is based on the molecular composition of OM, we call it the MMI. The atomic ratios of H/C and O/C are variables of the MMI. In kerogen pyrolysis, the dehydrogenation reaction, polycondensation reactions and side chain removal reactions occur to generate oil/gas. CO_2 is generated by the pyrolysis of oxygen-containing groups. The atomic ratios of H/C and O/C decrease with the thermal evolution of kerogen. As shown in Fig. A1, an increase in the MMI indicates an increase in the proportion of benzene rings in kerogen, a decrease in the proportion of –CH2- groups, and a decrease



Fig. 3. The evolution of OM in the van Krevelen diagram at different temperatures. The H/C and O/C atomic ratios of kerogen are between the two dotted lines. The solid lines show the evolution of type I, II, and III kerogens, and the arrows indicate the direction of increasing burial depth. In the inset in the upper right corner, the dark red polyline is the line connecting the data of the 390,000-step from 1900 K to 2800 K, and the dark red dotted line is a linear fit of the connection. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)



Fig. 4. Changes in the atomic ratios of OM during kerogen evolution. Trends of the (a) H/C atomic ratio, (b) O/C atomic ratio, (c) N/C atomic ratio, and (d) S/C atomic ratio at different temperatures.

in the proportion of oxygen-containing structures.

When m = 1, the kerogen is completely carbonized ($r_{\rm H/C} = r_{\rm O/C} = 0$), which is the limit state of *m*. At present, the evolution of OM maturity is primarily characterized by the VR. Based on the experimental data of the pyrolysis of the kerogen samples and coal [63–66], the values of *m* in the OM evolution are calculated; they are compared with the corresponding VR, as shown in Fig. 5. The relationship between the MMI and the VR of the residue is positive and approximately linear. The relationship between the H/C and O/C atomic ratios and the VR for the natural maturity is written as % Ro = $12\exp(-3.2r_{\rm H/C}) - r_{\rm O/C}$ (Vitrimat2018) [37]. In this study, we do not discuss the use of the MMI to calculate the VR. Our results show that the MMI is positively related to the VR, demonstrating that the proposed MMI is well suited to reflect the evolution of maturity.

Since *m* is a function of the molecular composition, we investigate the kinetics of the OM evolution from the perspective of the molecular structure as an independent index. The relationship between *m* and the H/C and O/C atomic ratios has been established. A 3D van Krevelen diagram was created (Fig. 6). It is observed that *m* increases with an increase in the buried depth.

3.1.3. Maturity versus weight loss

The ratio of weight loss reflects the quantity of kerogen to generate hydrocarbons. Kerogen pyrolysis simulations were performed at different temperatures. The weight loss of the kerogen increases over time under isothermal conditions, as shown in the histogram in Fig. 7(a). The relationship between the MMI and the weight loss w of kerogen is

established to determine the quantity of oil/gas generation. When kerogen reaches a certain maturity, the rates of weight loss and maturity evolution slow down. There is a positive linear correlation between weight loss and the MMI (Fig. 7(b)). The equation describing the relationship between *w* and *m* is $w = \lambda (m - m_0)$, where $\lambda = 8.43$ is the fitting parameter, *m* and m_0 are the current MMI and initial MMI,



Fig. 5. The correlation between the VR and the MMI. The points are obtained from the experimental data in Ref. [63–66].



Fig. 6. 3D van Krevelen diagram and the relationship between m and the H/C and O/C atomic ratios. The spheres indicate that the value of m increases with changes in the H/C and O/C atomic ratios in the residue at 1900 K.

respectively. The slope λ of the line does not change significantly with changes in the temperature, indicating that the temperature does not affect the relationship between m and w. The weight loss of kerogen occurs due to the generation of H₂O, CO₂, small hydrocarbons, and other products. These are the primary components of shale oil/gas. The w represents the weight loss, as well as the portion of oil/gas in mass. Therefore, the weight loss directly reflects the amount of produced oil/ gas $M_{\text{gas/oil}}$ (g) by kerogen pyrolysis ($M_{\text{gas/oil}} = wM_{\text{in}}$). The quantity of produced calculated oil/gas can be as follows: $M_{\text{gas/oil}} = wM_{\text{in}} = \lambda(m - m_0)M_{\text{in}}$, where M_{in} (g) is the initial mass of kerogen. We calculate the MMI value using the data in table 5 of Ref. [66]. The relationship between the MMI and the weight loss is plotted in Fig. B1. It is observed that relationship is also approximately linear, but the slope is smaller than that of the simulations. There may be two reasons: first, the sample used in the simulations is type III kerogen, and the sample of Ref. [66] is coal. At the same temperature, the order of the weight loss is type I kerogen > type II kerogen > type III kerogen > coal. Second, the residue we obtained consists of C₄₀₊ molecules, whereas the residue of Ref. [66] consists of C_{14+} molecules; therefore, the weight loss in our simulations is greater than that of Ref. [66].

In addition, the solid residue of kerogen pyrolysis can be divided



Fig. 8. Comparison of the bitumen and kerogen content in the organic residue for different values of m.

into two parts. The soluble part in the organic solvents is called bitumen, and the insoluble part is kerogen. The molecular weight of bitumen should not exceed 1,400 [67]. Therefore, bitumen and kerogen are distinguished by their molecular weight. We consider molecules with more than 100C atoms in the residue as kerogen molecules. The molecules from C_{40} to C_{100} are considered to be bitumen in this work, whose molecular weight typically exceeds 500. The bitumen molecules contain C, H, O, N, and S atoms. The C_{40-} molecules are oil and gas molecules, which contains CH₄, CO₂, H₂S, C₂-C₅, Naphtha, etc. The trends of the bitumen mass and kerogen mass versus m are shown in Fig. 8. As the MMI increases, the rate of kerogen decomposition decreases. The bitumen mass increased in the early stage of kerogen evolution and dropped in the later stage. Bitumen is produced by kerogen pyrolysis and is pyrolyzed into smaller molecules. The two reactions proceed simultaneously. When the rate of bitumen decomposition is higher than the rate of bitumen production, a decline in the bitumen mass occurs. As shown in the inset in Fig. 8, when the ratio of the bitumen content to the kerogen content in the residue is near 1, the bitumen mass begins to decrease.

3.2. Chemical kinetic model of kerogen based on MMI

The kerogen conversion rate is closely related to the temperature. The H/C and O/C ratios of the kerogen residue at different $(\mathbf{b}) = 1000 \text{ K}$

3.2.1. Comparison and selection of kinetic evolution equations



Fig. 7. (a) The histogram represents the relationship between the weight loss, MMI, time, and temperature. (b) The weight loss versus the MMI at different temperatures. Different colors in the histogram represent different temperatures, and the colors are the same as in the legend.

temperatures under isothermal conditions are obtained by simulation, and the MMI of OM is calculated. The rate of change of the MMI increases with increasing temperature (Fig. 9a). As shown in Fig. 9b, the temperature has a more significant effect on the reaction rate at the beginning of the reaction. At high temperatures, the MMI increases rapidly at the beginning of the reaction. The rate of change of the MMI ($\Delta m / \Delta t^*$) decreases and tends to be similar at different temperatures.

The initial stage of the kerogen has to be defined to analyze the evolution of kerogen. We assume that complete carbonization is the final state of kerogen; the conversion of the MMI is defined as:

$$x = \frac{m - m_0}{1 - m_0}$$
(3)

where m_0 is the initial MMI of the kerogen sample, and 1 represents the mature state of kerogen. *m* is calculated by Eq. (2). When m = 1, the kerogen is fully mature, and the kerogen conversion is 1. When $m = m_0$, no conversion occurs.

The conversion × is used to characterize the degree of kerogen conversion. In previous studies, the conversion was defined as $x_{\text{pre}} = (W_0 - W_t)/(W_0 - W_\infty)$, where W_0 , W_∞ , and W_t are initial mass, final mass, and mass of sample at time *t*, respectively [68,69]. The conversion x_{pre} is not directly related to changes in the kerogen structure, and can, therefore, not be related to the kinetic parameters. The evolution analysis is performed using the kinetic equation of solid-state decomposition [3770]:

$$\frac{\mathrm{d}x}{\mathrm{d}t} = kf(x) \tag{4}$$

where *k* is the rate constant (s⁻¹) and f(x) is the function of the reaction model [37]. Here, the Arrhenius equation is used to establish the models of hydrocarbon generation [43]. In this study, we assume that the rate constant *k* and temperature *T* also satisfy the equation. The Arrhenius equation is $k = \nu e^{-E/RT}$; Eq. (4) can be written as:

$$\frac{\mathrm{d}x}{\mathrm{d}t} = \nu \mathrm{e}^{-E/RT} f(x) \tag{5}$$

where *t*, ν , *E*, *R*, and *T* are the time (s), the pre-exponential factor (s⁻¹), the apparent activation energy (J/mol), the gas constant (J/mol/K), and the temperature (K), respectively.

There are several forms of the reaction model that are based on the mechanism of the chemical reaction order, the random nucleation and growth (the Avrami-Erofeev equation), the phase boundary controlled reaction (geometrical model), and the diffusion mechanism. The equations of several models are listed to compare and select the models [43,69–74]:

$$f(x) = \begin{cases} nx^{\frac{n-1}{n}} & \text{Power law} \\ n(1-x)[-\ln(1-x)]^{\frac{n-1}{n}} & \text{Avrami - Erofeev} \\ (1-x)^n & n^{\text{th - order}} \\ \frac{1}{2x} & 1D \text{ diffusion} \\ \frac{2}{3}(1-x)^{2/3}[1-(1-x)^{1/3}]^{-1} & 3D \text{ diffusion} \\ n(1-x)^{\frac{n-1}{n}} & \text{Geometrical model} \end{cases}$$
(6)

For isothermal reactions, the integration of Eq. (5) results in:

$$g(x) = \nu e^{-E/RT} t \tag{7}$$

where $g(x) = \int f^{-1}(x) dx$. Substituting Eq. (6) into Eq. (7), conversion *x* can be calculated by:

$$x = \begin{cases} (kt)^n & \text{Power law} \\ 1 - e^{-(kt)^n} & \text{Avrami - Erofeev} \\ 1 - e^{-kt} & 1^{\text{st}} - \text{order} \\ 1 - [1 - (1 - n)kt]^{1/(1-n)} & n^{\text{th}} - \text{order} (n \neq 1) \\ \sqrt{kt} & 1D \text{ diffusion} \\ 1 - [1 - (kt)^{1/2}]^3 & 3D \text{ diffusion} \\ 1 - (1 - kt)^n & \text{Geometrical model} \end{cases}$$
(8)

We established the relationship between ln(1-x) and t to select the kerogen pyrolysis model under isothermal conditions. The curve approaches a straight line at low temperatures. A concave downward curve is obtained at high temperatures. In this case, we choose a distributed reaction model or a model in which the activation energy varies with the conversion. The Avrami-Erofeev equation is not applicable here because it is a sigmoidal reaction model. The fitting curves obtained from the basic model are shown in Fig. C1. The conversion is calculated based on the OM structure, and directly affects the activation energy. Thus, we develop a model in which the activation energy varies with the conversion. The model is a the first-order reaction kinetic equation at different stages of pyrolysis. The evolution of kerogen is described well by the first-order reaction model at low temperatures but not at high temperatures (Fig. 10). The nature of the reactant and the type of broken chemical bonds are changing during the evolution of kerogen. The maturity of OM is accelerated rapidly at high temperatures; therefore, the rate of change of the activation energy increases as the kerogen conversion rate increases. The MMI is inversely related to the H/C and O/C atomic ratios of OM. The increase in the MMI is accompanied by increases in the proportion of C-C double bonds and aromaticity degrees and a decline in the heteroatoms in the OM [55,58]. The bond energy of C-heteroatoms (O, N and S) is lower than that of C-C, and the bond energies of the C-C double bond and the C-C



Fig. 9. (a) The MMI versus the temperature for different step (using 0.25 fs as the time step). (b) The average rate of increase of the MMI at different temperatures with an increment of 100 K ($R_m = \Delta m/\Delta t *$, where $t * = 4t/10^{-11}$ s).



Fig. 10. (a) ln(1-*x*) versus time *t* at different temperatures. The temperatures of the curves from top to bottom range from 1900 K to 2800 K in increments of 100 K. (b) Fitting curve of the first order chemical kinetic equation under isothermal conditions. The temperatures of the curves from bottom to top range from 1900 K to 2800 K.

bond in benzene are higher than that of the C–C single bond. The average bond energy in the molecule and the activation energy of the kinetic model increase with increasing MMI. Therefore, it can be considered that the activation energy is a function of m, and the conversion rate of OM declines with increasing MMI at the same temperature.

3.2.2. The time-temperature-MMI relationship

The first-order reaction kinetic model is selected to study the function of E(m):

$$\frac{\mathrm{d}x}{\mathrm{d}t} = \nu \mathrm{e}^{-E/RT} (1-x) \tag{9}$$

where *E* is an MMI-dependent variable. By substituting Eq. (3) into Eq. (9), we obtain:

$$\frac{d(m)}{dt} = \nu(m) e^{-E(m)/RT} (1 - m)$$
(10)

By taking logarithm on both sides of Eq. (10), the relationship of *m*-*T* is expressed as follows:

$$\ln \frac{dm}{(1-m)dt} = -\frac{E(m)}{RT} + \ln \nu(m)$$
(11)

The least-squares method is used to obtain the *m*-t curves of the simulation data, as shown in Fig. 11; 16 sample points with *m* ranging from 0.516 to 0.560 are used. The time t corresponding to different temperatures is calculated under isothermal conditions for the same MMI. Subsequently, the derivative of the *m*-t curves for the corresponding data points is calculated. The item on the left side of Eq. (11) is obtained: $(L = \ln \frac{dm}{(1-m)dt})$. When the MMI is higher than 0.536, there are fewer sampling points of *L* because the MMI of partial simulations cannot be obtained. As shown in Fig. D1, the relationship between L and 1/T for the same MMI is approximately linear, which indicates that the first-order kinetic model is appropriate. For simplification, we assume that the pre-exponential factor is constant, and the linear relationship of L-1/T is obtained. The slopes are - E/R, and the intercept is $\ln \nu = 29.63 \text{ s}^{-1}$. The activation energies at different MMI values are obtained. As shown in Fig. 11, the activation energies E increase with increasing m, and the relationship is approximately linear (E = b + am). The slope and intercept of the kerogen in this study are a = 855.11 KJ and b = -285.40 KJ. The activation energy of the sample ranges from 150 KJ to 350 KJ. According to the previous chemical kinetic model based on the hydrocarbon generation rate, the activation energy of kerogen is around 200 KJ, but the range of the activation energy of type III kerogen is large (170-400 KJ) [75]. By substituting E(m) into Eq. (11), the kinetic model of the maturity evolution (MEKM) is obtained:

$$\frac{\mathrm{d}m}{\mathrm{d}t} = \nu \mathrm{e}^{-(am+b)/RT} (1-m) \tag{12}$$

By integrating Eq. (12), the relationship among the time, temperature, and the MMI can be expressed as:

$$t = \frac{e^{b/RT}}{\nu} \int \frac{e^{am/RT}}{(1-m)} dm$$
(13)

Although the integral in Eq. (13) cannot be expressed as elementary functions, the value of the definite integral can be easily calculated by mathematical software such as Mathematica. In a previous study, the global first-order kinetic model did not adequately describe the evolution of kerogen due to the complex and non-uniform kerogen structure [76]. Common models that use x_{pre} as the conversion include the Friedman, Kissinger-Akahira-Sunose (KAS) and Flynn-Wall-Ozawa (FWO) models. The activation energy curves and the forms of these models of activation energy are complex. For example, the kinetic parameters of the Friedman, KAS and FWO models are calculated at isoconversional points ranging from 0.1 to 0.9 (with an increment of 0.05 or 0.1). In addition, there are 11 parallel first-order reactions with different activation energies in a previous model [77]. These resulted in complex equations which are inconvenient for engineering use. However, our proposed kinetic model provides a straightforward approach to calculate the time required for the kerogen to mature to a certain value at different temperature. For this sample, the initial MMI of the kerogen sample is m = 0.495. When VR greater than 2.0 %Ro, the shale gas reservoirs have significant mining value. As shown in Fig. 3, the MMI is about 0.65 at %Ro = 2.0 for type III kerogen. Table 2 shows the time required for the OM to reach a certain maturity (artificial



Fig. 11. The MMI versus the activation energy. The inset shows the *m*-*t* fitted curves at different temperatures.

Time (s) to reach maturity at different temperature.

T (°C)100200300400500600700800 $m = 0.625$ 7.67×10^{19} 4.50×10^{12} 9.05×10^7 4.62×10^4 170.05 2.30 0.076 4.75×10^{-3} $m = 0.650$ 7.92×10^{22} 1.09×10^{15} 8.53×10^9 2.24×10^6 5.04×10^3 46.41 1.13 0.056 $m = 0.675$ 8.23×10^{25} 2.66×10^{17} 8.08×10^{11} 1.09×10^8 1.50×10^5 945.27 17.04 0.65 $m = 0.700$ 8.60×10^{28} 6.52×10^{19} 7.71×10^{13} 5.35×10^9 4.50×10^6 1.94×10^4 257.95 7.75 $m = 0.725$ 9.04×10^{31} 1.61×10^{22} 7.39×10^{15} 2.64×10^{11} 1.36×10^8 3.99×10^5 3.93×10^3 92.35 $m = 0.750$ 9.59×10^{34} 4.01×10^{24} 7.15×10^{17} 1.31×10^{13} 4.12×10^9 8.29×10^6 6.04×10^4 1.11×10^3	.,	5	1						
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	<i>T</i> (°C)	100	200	300	400	500	600	700	800
	m = 0.625 m = 0.650 m = 0.675 m = 0.700 m = 0.725 m = 0.750	$\begin{array}{l} 7.67 \times 10^{19} \\ 7.92 \times 10^{22} \\ 8.23 \times 10^{25} \\ 8.60 \times 10^{28} \\ 9.04 \times 10^{31} \\ 9.59 \times 10^{34} \end{array}$	$\begin{array}{l} 4.50 \ \times \ 10^{12} \\ 1.09 \ \times \ 10^{15} \\ 2.66 \ \times \ 10^{17} \\ 6.52 \ \times \ 10^{19} \\ 1.61 \ \times \ 10^{22} \\ 4.01 \ \times \ 10^{24} \end{array}$	$\begin{array}{l} 9.05 \times 10^{7} \\ 8.53 \times 10^{9} \\ 8.08 \times 10^{11} \\ 7.71 \times 10^{13} \\ 7.39 \times 10^{15} \\ 7.15 \times 10^{17} \end{array}$	$\begin{array}{l} 4.62 \times 10^{4} \\ 2.24 \times 10^{6} \\ 1.09 \times 10^{8} \\ 5.35 \times 10^{9} \\ 2.64 \times 10^{11} \\ 1.31 \times 10^{13} \end{array}$	$\begin{array}{l} 170.05\\ 5.04 \times 10^{3}\\ 1.50 \times 10^{5}\\ 4.50 \times 10^{6}\\ 1.36 \times 10^{8}\\ 4.12 \times 10^{9} \end{array}$	2.30 46.41 945.27 1.94×10^4 3.99×10^5 8.29×10^6	$\begin{array}{c} 0.076 \\ 1.13 \\ 17.04 \\ 257.95 \\ 3.93 \times 10^3 \\ 6.04 \times 10^4 \end{array}$	$\begin{array}{l} 4.75 \times 10^{-3} \\ 0.056 \\ 0.65 \\ 7.75 \\ 92.35 \\ 1.11 \times 10^3 \end{array}$

maturity) under different isothermal conditions. Since the activation energy of OM increases with the increase in the MMI, the OM evolution becomes more difficult, and the hydrocarbon generation is slower at high MMI values. According to the experimental results in Ref. [78], the maturity of kerogen from 0.745 to 2.068 %Ro requires 2.51 \times 10⁶ s under confined laboratory conditions at a temperature of 400 °C. The corresponding MMI range is about 0.52–0.65. Equation (13) is used to calculate the required time in this range, which is 2.24 $\times~10^{6}$ s at 400 °C. This value is very close to the time obtained by the experiments, indicating that the relationship among time, temperature and the MMI still holds at lower temperatures. The equation can be used to choose the temperature and time for kerogen to reach artificial maturity. The MEKM needs to be further investigated and revised for kerogen evolution with a larger range of maturity, and the influence of pressure, heating rate, and minerals have to be analyzed. However, this work provides ideas for examining the chemical kinetic equation of kerogen pyrolysis based on the structure of OM and for determining the relationship between the activation energy and the MMI.

4. Conclusions

In summary, we proposed the MMI based on the H/C and O/C atomic ratios for evaluating kerogen maturity. An increase in the MMI indicates a decrease in the H/C and O/C atomic ratios. Thermal evolution experiments indicated a positive correlation between the MMI and the VR, a commonly used maturity index, thereby verifying the reliability of the MMI. MD simulations of the type III molecular model of kerogen from the Ordos basin demonstrated that the weight loss had a positive linear relationship with the MMI, accurately reflecting the hydrocarbon generation.

We investigated the changes in the MMI over time at different temperatures under isothermal conditions. The maturity evolution accelerated with increasing temperature, and the maturity rate decreased with increasing MMI at the same temperature. Several models of kinetic solid-state decomposition were used to establish the equations describing the kerogen maturity evolution; the first-order chemical kinetic equation was selected to investigate the relationship between the activation energy and the MMI.

The activation energy is related to the molecular structure of kerogen. The proposed conversion is directly related to maturity index; therefore, the relationship between the maturity index and the

Appendix A. Kerogen pyrolysis process

activation energy can be established. Simulations and numerical calculations indicated that the activation energy increased linearly with the MMI. The MEKM based on the first-order kinetic model was established, and it was found that the activation energy changed with the maturity. We determined the time to reach maturity of kerogen at different temperatures, which provides a method to select optimum time and temperature required for kerogen maturity in mining projects. Our findings provide insights into the evolution of kerogen at the molecular level and guidance to determine the heating temperature and heating time for artificial maturity. However, our work is based on simulations and on type III kerogen. The parameters corresponding to type I and type II kerogen, as well as the relationship between kinetic parameters and different types of kerogen, require further study to obtain a universal equation. Furthermore, we will conduct pyrolysis experiments on large rock masses and modify the current kinetic equations using a macro perspective for better applicability to actual conditions. The results of this study provide information on kerogen ripening, thereby improving oil and gas yields and reducing the costs of gas/oil exploitation.

CRediT authorship contribution statement

Xiaohe Wang: Methodology, Software, Formal analysis, Data curation, Writing - original draft, Visualization, Investigation, Writing review & editing. Ya-Pu Zhao: Methodology, Resources, Funding acquisition, Supervision, Project administration.

Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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As shown in Fig. A1, pyrolysis of the marked part indicates the removal of the side chain in the kerogen. The C-heteroatom bonds and the chemical bonds in the middle of the long chain are more easily broken. Dehydrogenation can also be observed. This indicates that, the aromatic and double/triple bond-containing units in the residue increase during kerogen pyrolysis.



Fig. A1. ReaxFF simulation of single kerogen pyrolysis at 2300 K. (a) The initial state of the single molecule. The molecules of the kerogen (b) at the 19 5000th step and (c) the 39 0000th step. The blue atoms are part of the long chain of kerogen.

Appendix B. The relationship between the MMI and weight loss

The atomic ratios of H/C and O/C of the kerogen residue are measured at different temperatures in the closed systems [66]. The MMIs are calculated. The relationship between the MMI and the weight loss is shown in Fig. B1.



Fig. B1. The weight loss versus the MMI of Morwell coal; the data are from Ref. [66].

Appendix C. Pyrolysis analysis using different basic kinetic models

The relationship between \times and *t* at different temperatures is fitted by Eq. (8) to establish a suitable evolution model of the maturity. As shown in Fig. C1(a) and (b), the conversion curves based on the first-order reaction kinetic model and geometrical model (n = 3) are fitted very well at low temperatures, but the curves do not agree well with the simulation data at high temperatures. The Avrami-Erofeev equation (n = 2) cannot be used to fit the simulation results (Fig. C1(c)) due to the random nucleation and growth behavior. The reaction randomly initiates at multiple sites, and subsequently, each location expands in space. The reaction rate is directly proportional to the area of the reaction interface, but as the reaction occurs, the reaction interface begins to overlap. Therefore, the reaction rate increases first and then decreases, exhibiting a sigmoidal response and we cannot fit the curve. The reaction rate is proportional to the reaction interface area increases in the initial stage of the reaction, and then decreases as the reaction regions begin to overlap. The overall evolutionary trends of the *m*-*t* curves based on the diffusion and power law (n = 1/2) models are consistent with the simulation results; however, the errors in the initial stage of the evolution are substantial (Fig. C1(d-f)). The results show that none of the above equations satisfactorily meet our needs. The reason may be that kerogen contains a variety of functional groups. During the pyrolysis process, the types of chemical bonds change, and the broken bonds constantly change, resulting in changes in the reaction. Therefore, the activation energy changes during the pyrolysis process. The evolution of kerogen has been investigated using the first-order kinetic equation, where the activation energy changes with the conversion, and the activation energy is calculated at the isoconversional points of the curve [77].



Fig. C1. Comparison of several chemical kinetic equations under isothermal conditions. The temperatures of the curves from bottom to top range from 1900 K to 2800 K in increments of 100 K.

Appendix D. Model reliability analysis

As shown in Eq. (11), *L* and 1/T need to satisfy a linear relationship if the first-order kinetic equation is used to describe the maturity evolution of kerogen. The values of *L* of several indices are calculated at different temperatures, since we believe that the kinetic parameters change with the kerogen structure. Fig. D1 shows the change in *L* with 1/T. The relationship is linear, indicating that the proposed kinetic equation is reasonable. The pre-exponential factor is fixed to simplify the kinetic equation. The relationship between the pre-exponential factor and activation energy is positive [52]. The change in the activation energy during the evolution is not monotonous and irregular both the pre-exponential factor and activation energy are used as fitting parameters. Since $k = ve^{-E/RT}$, a fixed pre-exponential factor is chosen to determine the changes in the activation energy with changes in the kerogen structure, although this may reduce the accuracy. The median value of the pre-exponential factor obtained by fitting is selected, and this value is on the order of 10^{13} which is consistent with a previous study [79].



Fig. D1. Linear relationships between L and 1/T.

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