Machine-learning integrated glassy defect from an intricate configurational-thermodynamic-dynamic space

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(Received 13 January 2021; revised 25 March 2021; accepted 29 July 2021; published 13 August 2021)

Optimizing materials' properties and functions by controlling defects in the crystalline phase has been a cornerstone of materials science and condensed matter physics. However, this paradigm has yet to be established in the broadly defined amorphous materials, which implies the identification of very subtle structural features in an otherwise uniformly disordered medium. Here we propose and define a new integrated glassy defect (IGD), based on machine learning strategy informed by atomistic physics, and also by an extremely wide configurational, thermodynamic, and dynamic variables space of the disordered state. The IGD simultaneously includes positional topology and vibrational features, as well as the local morphology of the potential energy landscape. This unprecedented combination gives rise to a much more comprehensive and more effective definition of the "glassy defect," much beyond the conventional, purely structural input. IGD can be used not only as an efficient predictor of athermal plasticity but is also transferable to detect both short-time vibrational anomalies (the boson peak), and long-time relaxation and diffusion dynamics in glasses. The integrated strategy is instrumental to build the long-sought structure-property relationship in complex media.

DOI: 10.1103/PhysRevB.104.064108

I. INTRODUCTION

Owing to plenty of attractive mechanical, physical and chemical properties and a wide range of potential structural and functional applications, the metallic glasses (MGs) are both of engineering significance and great scientific relevance for the broad communities of materials science and condensed matter physics [1-5]. Despite decades of relentless pursuit, establishment of the structure-property relationship in such disordered materials is still one of the most elusive yet most intriguing unsolved problems up to date [6-13]. In contrast with their crystalline counterparts, whose structural defects are easily identified from the periodic arrangement of atoms in the lattice, the atomic-scale structure of amorphous materials is usually featureless. The structure of glass lacks either translational or rotational periodicity, with each atom residing in its own, individual atomic environment. Thus it is rather difficult to find a physics-motivated descriptor, like the Burgers' vector of dislocation in crystal, that is capable of characterizing the possible structural defects in glasses, which act as plasticity-carriers under external mechanical and/or thermal stimuli [14]. The lack of a priori structural defects thus prevents establishing an intuitive one-to-one structureproperty relationship in the widespread domain of amorphous materials.

Great efforts have been devoted to identifying possible structure-property relationships in the disordered materials over the past decades. Among these attempts, the most successful representatives include the mean-field free volume [15] and shear transformation zone (STZ) models [16–18]. However, no structural defects that could play the same role as dislocations in crystals, have been reported in the literature about glassy materials [19]. Until recent years, a few effective structural descriptors have been used to explain the observed dynamics of amorphous materials. Such structural signatures can be categorized into three groups. The first category is based on purely static structure, such as the short-range Voronoi polyhedra [7,20] and the related local five-fold symmetry parameter [21,22], as well as the Voronoi cell anisotropy [23,24], the inversion symmetry breaking [25], the two-body excess entropy [26,27], the local coordination number [28], and other structural order metrics [29–31], etc. The second class involves descriptors of thermodynamic response, e.g. soft vibrational modes [32-34], vibrational mean-squared displacement (vMSD) or Debye-Waller factor [35,36], the flexibility volume [37,38], and finally the local thermal energy [39]. The third group contains further dynamic features, which includes the local yield stress [40], the gradient along the minimum energy pathway of STZ on the potential energy landscape (PEL) [41], etc. However, these physics-motivated parameters usually partially forecast the nature of the localized plastic flow in glasses. And often the prediction is either material-specific, or deformationprotocol dependent [41].

2469-9950/2021/104(6)/064108(14)

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Instead of the conventional knowledge-driven strategy, the new machine learning (ML) paradigm is especially suitable for constructing a robust correlation between structures and functions in glasses [8,42-48]. It has been set in practice by combining a series of particle-position based symmetric Gaussian functions, and by exploring interstice structural distributions in both short and medium range via ML models. In all the pioneering works, the machine-learned structural defects, e.g., the glass "softness" [43], the "quench-in softness" [45], and the "structural flexibility" [48] are strongly correlated with the elementary excitation in different glasses. However, the protocols are only based on purely static structure. The lack of high-order features may cause incomplete description of the dynamics in glass. For example, strong spatiotemporal correlation has been found between structure and dynamics in model glasses [29,31], which suggests opening up a new avenue of research, where an overarching structureproperty "super-relationship" can be developed based on even broader physical input and not just the structural features. Actually, the recent concept of the flexibility volume [37] goes in this direction as it combines both structural (Voronoi volume) and thermodynamic (vibrational) feature of a specific atom to predict dynamics.

Therefore a novel proposition about a structure-property super-relationship must simultaneously account for all (structural, thermodynamic, dynamic) physical aspects that are associated with properties of glass. To this end, we propose a machine-learning integrated glassy defect (IGD) of MGs via extraction of all configurational, thermodynamic and dynamic features that are coupled and coexisting in the inherent configuration of disordered phase. The extensive ML process is conducted by using atomic coordinates, vibrational analysis and the PEL morphology, respectively, as different but equally important fingerprints of the underlying glass physics. The integrated defect via ML-termed integrated glassy defect-serves as an unprecedented signature of the athermal local structural deformation (plasticity), as well as thermal short-time vibrational anomalies, long-time diffusion, and slow relaxation dynamics in the amorphous alloys.

II. METHODOLOGY

A. Molecular dynamics

All of the molecular dynamics (MD) simulations here are performed by using the open source LAMMPS code [49], with the Finnis-Sinclair-type embedded-atom method empirical potential [50] being adopted to describe the interatomic interaction of the Cu₅₀Zr₅₀ metallic glasses. We prepare ten independent glass samples and each of them contains 19 652 atoms, with 3D dimensions of $\sim 70 \times 70 \times 70$ Å. For the glass structure preparation, the samples are first melted from their crystalline phases (B₂ phase, body-centered cubic) from 0 K to 2000 K, and then being equilibrated for 2 ns at 2000 K before being quenched to the glassy state at 0 K, with a cooling rate of 10^{10} K/s. Periodic boundary conditions (PBCs) and *NPT* ensemble (constant number of atoms, constant pressure, and constant temperature) are applied for all the atomistic simulations. Temperature is controlled by the Nosé–Hoover thermostat [51]. Stress tensor is kept zero



FIG. 1. The radial distribution function of a $Cu_{50}Zr_{50}$ metallic glass. The split of the second peak in RDF indicates glass nature of the atomic model.

within the Parrinello–Rahman barostat [52]. The MD time step is 2 fs to numerically integrate Newton's equation of motion. Figure 1 gives the radial distribution function (RDF) of one $Cu_{50}Zr_{50}$ sample. It clearly indicates the nature of glass structure by the split of second peak.

Athermal quasistatic shear (AQS) simulations [53] with simple *xy*, *yz*, and *zx* shearing deformation protocols are performed at a step size of $\Delta \gamma = 1 \times 10^{-5}$. Each deformation increment is followed by operation of energy minimization to remove all the thermal effect. In this way, the strain rate effect on the mechanical response is avoided in the shear deformation and, thus, reflecting intrinsic nature of the local plastic event carried out by the atomic rearrangement—shear transformation.

B. Construction of the structural-thermodynamic-dynamic space

1. Structural features

We adopt a family of symmetric Gaussian functions to describe the information embedded in the structural space. The structural descriptor G - i for each atom, which has been used to calculate the "softness" [43] and details the potential energy landscape for complex materials [42], is defined as

$$G_i = \sum_{j}^{N_i} \exp[-(R_{ij} - \mu)^2 / L^2].$$
 (1)

Here R_{ij} denotes the distance between atom *i* and *j*. N_i is the number of the neighboring atoms around the *i*th atom. μ and *L* are constants that need to be tested and optimized. Actually, the Gaussian structural function is a weighted sum of a group of the Gaussian functions. Parameter μ controls the position of the highest weight and *L* is a broadening coefficient. According to the RDF of the present Cu₅₀Zr₅₀ model glass as shown in Fig. 1, the parameter μ is set from 1.5 to 7.5 Å with an interval of 0.2 Å. It makes sure that all the effective

structural information from short-range to medium-range order is contained in the ML model. Moreover, the parameter Lis set as 3.5 Å for each Gaussian structural function. Therefore there are altogether 31 Gaussian structural functions included in the machine learning model. Gaussian functions at longer distance has been tested but make trivial contribution to the effectiveness of IGD and therefore not considered in the ML model.

A new purely static structure feature proposed here is the two-body excess entropy at single-particle level, which naturally encompasses positional information and their correlation in space. It is defined as the two-body term of the infinite-term expansion of the excess entropy, which represents the loss of configurational entropy with respect to the ideal gas state owing to the positional correlation in some ordered phase [26]. This two-body approximation has been applied to account for the structure-dynamic relationship of the glass-forming liquids [54]. Therefore it is certainly an intriguing pure positional feature that can enrich the information of the structural space in the machine learning model. The two-body excess entropy, or the local structural entropy, of the *i*th atom is calculated according to the equation

$$S_{2,i} = -\frac{1}{2} \sum_{v} \rho_v \int_0^{r_{\text{cutoff}}} \left\{ g_i^{uv}(\mathbf{r}) \ln g_i^{uv}(\mathbf{r}) - \left[g_i^{uv}(\mathbf{r}) - 1 \right] \right\} d\mathbf{r}.$$
(2)

Here *u* and *v* represent the types of particles (Cu or Zr atoms in the present case), ρ_v is the number density of the *v* type particles, and g_i^{uv} denotes the local RDF between the particle *i* of type *u* and other particles of type *v*. The cutoff distance for the integration is set from 3 to 15 Å with step of 0.5 Å. Furthermore, the freedom of choice in the cutoff distance provides immense room to construct the structural spaces for machine learning. On the basis of two-body entropy, another 25 structural features are augmented to the Gaussian functions.

2. Thermodynamic features

To detail the thermodynamic information in a quantitative manner, the vibrational mean-squared displacement (vMSD), or the Debye–Waller factor, is defined according to the equation:

$$\left\langle \Delta r_i^2 \right\rangle = \left\langle |\mathbf{r}_i(t) - \mathbf{r}_{i,\text{equil}}|^2 \right\rangle_{\tau}.$$
 (3)

Here $\mathbf{r}_i(t)$ is the instantaneous position at different times during tracing for $\tau = 100$ ps at different temperatures, from 25 to 500 K with an interval of 25 K. $\mathbf{r}_{i,equil}$ is the equilibrium position of the *i*th atom in the inherent structure after energy minimization. The angular brackets imply the time average. This appropriate time duration ensures that the atoms vibrate around their thermodynamic equilibrium positions without dynamic hopping from one energy basin to another. Thus we obtain 20 features to construct the thermodynamic space preparing for the machine-learning model. The wide temperature range enables inclusion of possible anharmonic nature of the local energy basin.

3. Dynamic features

To assign a series of meaningful dynamic properties to the atoms in glass, the activation-relaxation technique nouveau (ARTn) [55,56] is adopted to extract the single-atom activation energies. In the framework of ARTn, the "activation" is initiated by imposing a random small displacement to the local cluster centered on a chosen atom. In the present work, the perturbation is restricted to a specific atom by setting the cutoff distance to be 2 Å, which is shorter than the first maximum of RDF, g(r), of the Cu₅₀Zr₅₀ glass, as shown in Fig. 1. The activation direction for a possible event is chosen randomly, with magnitude of the perturbation displacement being fixed 0.1 Å. Then the activation is driven along the minimum Hessian direction. The increment movement is 0.15 Å. When the lowest eigenvalue of Hessian matrix is less than $-0.30 \text{ eV}/\text{Å}^2$, the system is pushed towards a connecting saddle point by using the Lanczos algorithm. During the "relaxation" process, the maximum force tolerance of 0.05 eV/Å is used for converging to the saddle point. As shown in Fig. 2(e), the wide distribution of energy barriers for an atom indicates the complexity, or multiplicity, of the activation paths on the PEL. Therefore single activation energy of an atom is not enough to detail the local topology of PEL where initial state resides. For statistical purpose, each atom is furthermore activated for 24 times with random initial perturbation direction. Consequently, 24 activation energies for each atom is arranged in order according to their magnitude as $\{\Delta Q_1, \Delta Q_2, \ldots, \Delta Q_{24}\},$ where $\Delta Q_1 < \Delta Q_2 < \cdots < \Delta Q_{24}.$ Finally, we adopt such arrangement to detail the distribution of activation energies for an atom. We therefore obtain 24 features accounting for the dynamic information of an atom by including both difficulty (the barrier height) and multiplicity (possible paths) of the local structural excitations.

The distributions of activation energies for all the atoms, Cu atoms and Zr atoms are shown in Figs. 2(a)-2(c), respectively. It shows that the activation energy is distributed over a very broad range, indicating a strong dynamic heterogeneity as frequently reported in the literature, whereas the distribution for the Cu atoms is more concentrated than that of the Zr atoms. This is because the coordination number of Zr atoms is higher than that of Cu atoms, resulting in a greater diversity in the local structural environment of Zr atoms. Compared with Cu atoms, the peak position of the Zr barrier distribution shifts to the right. This is due to that Zr atoms are heavier than Cu atoms, and the former are difficult to be activated under the same external conditions. In other words, compared with Cu atoms, Zr atoms require a longer time to relax into stable positions corresponding to the deeper basin of PEL. This phenomenon may be the result of the larger constraints that Zr atoms undertake in CuZr glass than Cu atoms.

In Fig. 2(d), we show the spatial distribution of ΔQ_1 in a slice chosen on the *x*-*y* plane of the model. This plot shows the topological information on activation energy and indicates the spatial heterogeneity of the PEL in glass.

C. Supervisory signal for classification—shear transformation

To identify the atoms that have undergone structural rearrangement, we use the nonaffine squared displacement D_{\min}^2 [17] and monitor its jump as global strain evolves. To calculate



FIG. 2. Dynamic features in $Cu_{50}Zr_{50}$ metallic glass shown by potential energy landscape. The distribution of activation energies for (a) all atoms, (b) Cu atoms, and (c) Zr atoms, respectively. (d) Color map of the spatial distribution of atomic activation energies. The shown slice is normal to the *z* direction with a thickness of 5 Å. (e) The wide distribution of activation barriers for two specific atoms. Each atom has been activated for 24 times along random directions.

the parameter, the first step is to optimize a local affine transformation matrix, \mathbf{J}_i , that best maps $\{\mathbf{d}_{ji}^0\} \rightarrow \{\mathbf{d}_{ji}\}, \forall j \in N_i$, where N_i is the number of the nearest neighbors of the *i*th atom, and \mathbf{d}_{ji}^0 and \mathbf{d}_{ji} are the bond vectors for the reference and the current configurations between the *j*th and *i*th (central) atoms, respectively. The local nonaffine squared displacement of the central atom *i* relative to its nearest neighbor atoms *j*, is then defined as

$$D_{i,\min}^2 = \frac{1}{N_i} \sum_{j} \left(\mathbf{d}_{ji} - \mathbf{J}_i \mathbf{d}_{ji}^0 \right)^2.$$
(4)

In the present simulations, we monitor a flow reference ΔD_{\min}^2 to compare two configurations that are close by to one another, i.e., consecutive configurations separated by a global shear strain difference of $\Delta \gamma = 0.01\%$ under AQS. A typical example is shown in Fig. 3(a), where ΔD_{\min}^2 of specific atoms is plotted as a function of shear strain up to $\gamma = 5\%$. Atoms I and II can be observed to undertake obvious jump at about $\gamma = 1.6\%$ and 1.8%, respectively, whereas atom III exhibits no jump seen by ΔD_{\min}^2 . Figure 3(b) shows the distribution of the maximum ΔD_{\min}^2 of the atoms. Here, we chose the turning point of 0.05 Å² as the threshold to judge whether atoms are taken to be the ones that have undertaken rearrangement or not. For each sample (as we have ten samples), we perform AQS along xy, yz, and zx directions, respectively. The ΔD_{\min}^2 for each atom in the three AQS loading protocols is monitored and, once the value of ΔD_{\min}^2 exceeds the threshold of 0.05 Å², the corresponding atom will be labeled as a rearranged atom. As shown in Fig. 3(b), where the position of the threshold value is marked using dashed line, the rearranged particles contain about 5% of all atoms.



FIG. 3. (a) ΔD_{\min}^2 as a function of the global shear strain for three specific atoms in Cu₅₀Zr₅₀ under AQS to a shear strain $\gamma = 0.05$. ΔD_{\min}^2 evaluates the nonaffine displacement between two configurations that are close by to one another with shear strain difference of $\gamma = 0.01\%$. Atoms I and II have apparently experienced obvious jumps in ΔD_{\min}^2 (and likely local structural excitation) but not atom III. (b) Distribution of the maximum jump of ΔD_{\min}^2 with the blue line denoting the frequency for different ΔD_{\min}^2 , whereas the red line characterizing the cumulative frequency.



FIG. 4. Contour plot of cross-validation accuracy. The RBF (Gaussian) kernel function is used and predictions from models with different parameters are shown. The *x*-axis is $\log_2 C$ and the *y*-axis is $\log_2 \gamma$. The best model is identified to be the one with the largest cross-validation accuracy. And thus parameters are set as C = 4 and $\gamma = 0.03125$.

D. Support vector machine model

training set is The given as the form of $\{(\mathbf{x}_1, y_1), \dots, (\mathbf{x}_N, y_N)\}$, where N denotes the number of atoms and $\mathbf{x}_i = \{x_i^1, \dots, x_i^M\}^T$ describes the feature space of atom i, with M denoting the number of features. In the present work, M = 100. Here, $y_i = 1$ if the *i*th atom have undergone obvious shear transformation, while $y_i = -1$ for the atoms that are marked as nonrearranged ones. The aim of our SVM model is to find a hyperplane in the high-dimensional feature space that can separate data points with different value of y_i as preciously as possible. For this purpose, the SVM algorithm of the LIBSVM package [57] is used to solve the following primal optimization problem:

$$\min_{\boldsymbol{\omega}, \xi, b} \frac{1}{2} \boldsymbol{\omega}^T \boldsymbol{\omega} + C \sum_{i=1}^{N} \xi_i$$

subject to $y_i(\boldsymbol{\omega}^T \boldsymbol{\phi}(\mathbf{x}_i) + b) \ge 1 - \xi_i,$
 $\xi_i \ge 0, \ i = 1, \dots, N,$ (5)

Here, $\phi(\mathbf{x}_i)$ maps \mathbf{x}_i into a higher-dimensional space, $\boldsymbol{\omega}$ is the vector variable used to construct the hyperplane, and C > 0 is the regularization parameter. Due to the high dimensionality of $\boldsymbol{\omega}$, this dual problem is always solved by defining the kernel function as $K(\mathbf{x}_i, \mathbf{x}_j) = \phi(\mathbf{x}_i) \cdot \phi(\mathbf{x}_j)$. In the present work, the radial basis function (RBF, Gaussian) kernels with the form of $K(\mathbf{x}_i, \mathbf{x}_j) = \exp\{-\gamma \|\mathbf{x}_i - \mathbf{x}_j\|^2\}$ are adopted. So (C, γ) are the flexible parameters to be decided. We provide a possible interval of *C* and γ in the grid space. The tunable parameters are then optimized through cross-validation in order to obtain the highest accuracy. The heat map of cross-validation accuracy for different (C, γ) parameters is shown in Fig. 4. It indicates that the cross-validation accuracy is found to have a maximum value when $C = 2^2$ and $\gamma = 2^{-5}$. These values are therefore used in the present SVM model for classification.



FIG. 5. Phonon features for the $Cu_{50}Zr_{50}$ metallic glass. (a) The VDOS for the system. (b) The reduced VDOS $g(\omega)/\omega^2$ for the system. It confirms the existence of boson peak in $Cu_{50}Zr_{50}$ with the dashed line identifying the Debye level. (c) VDOS for several specific atoms. (d) The reduced VDOS $g(\omega)/\omega^2$ or intensity of boson peak for several different atoms.

E. Short-time vibrational anomaly-boson peak

To test the correlation between IGD and the short-time thermal properties of metallic glass, we propose and implement a single-atom level intensity of boson peak, which is the excess vibrational mode in the low frequency domain of phonons in glass, compared with the Debye squared model. First of all, the vibrational, or phonon, density of states (VDOS) for the system are calculated by direct diagonalization of the Hessian matrix, which is evaluated at a local energy minimum position of the potential energy landscape an inherent structure. The Hessian matrix are constructed by evaluating the spring constants of each atom from the empirical potential. The single-atom VDOS of the atom i is then formulated as [58],

$$g_i(\omega) = \frac{1}{3N} \sum_j \delta(\omega - \omega_j) |\mathbf{e}_j^i|^2.$$
(6)

Here, *N* is the number of atoms in the system. ω_j and \mathbf{e}_j give the normal model frequency and the corresponding polarization vector of the vibrational mode *j*, respectively. Compared with the Debye squared model, i.e., $g(\omega) \propto \omega^2$, the intensity of the single-particle boson peak I_{BP} is obtained by finding the maximum value of the reduced VDOS, i.e., $I_{\text{BP}} = \max[g_i(\omega)/\omega^2]$.

Figure 5(a) shows the VDOS of $Cu_{50}Zr_{50}$ metallic glass. In Fig. 5(b), we show the reduced VDOS by the Debye-squared model, $g(\omega) \sim \omega^2$ (the VDOS divided by ω^2). It indicates the existence of a boson peak in the system and shows that the boson peak can be clarified at around 5 THz. Figure 5(c) shows the calculated single-particle VDOS for several atoms and the corresponding boson peaks for the specific atoms are shown in Fig. 5(d).



FIG. 6. Long-time dynamics for $Cu_{50}Zr_{50}$ metallic glass. (a) The static structure factor of $Cu_{50}Zr_{50}$. (b) The mean-squared displacement at 700 K for all atoms in the system. (c) The non-Gaussian parameter at 700 K for all atoms. (d) Self-intermediate scattering function with wave vector q = 2.7 Å⁻¹ and temperature T = 700 K for all atoms.

F. Long-time dynamics-diffusion and relaxation

1. Diffusive mean-squared displacement

A commonly used long-time diffusive feature of amorphous solids is the mean-squared displacement (MSD), which quantifies how far a particle has moved with respective to its initial position as a function of time, i.e.,

$$\Delta r_i^2(t) = \langle [\mathbf{r}_i(t) - \mathbf{r}_i(0)]^2 \rangle.$$
(7)

Here $\mathbf{r}_i(t)$ and $\mathbf{r}_i(0)$ denote the positions of the particle *i* at the current and the initial configuration, respectively. The angle bracket $\langle \cdots \rangle$ represents an ensemble average. Here MSD is calculated at 700 K for the Cu₅₀Zr₅₀ sample. Note that the diffusive MSD is different from the vibrational MSD as shown in Eq. (3), the latter describes a thermodynamic response.

The diffusive mean-squared displacement as a function of time at 700 K for $Cu_{50}Zr_{50}$ sample is shown in Fig. 6(b). It indicates that MSD in metallic glass shows three stages. At very short timescales, particle motion is free from the influence of the neighboring atoms and therefore show ballistic behavior with MSD is proportional to t^2 . As the timescale increases, neighboring atoms function as obstacle and block the further movement of the central atom. Therefore topological excitation for particles become difficult and there is certainly a plateau shown in Fig. 6(b). Eventually, atoms will break away from the bondage of the surrounding atoms and undergo random walk diffusive motion.

2. Non-Gaussian parameter

The non-Gaussian parameter is commonly used to measure the dynamical heterogeneity of a disordered system. While the diffusive MSD $[\Delta r_i^2(t)]$ is related to the second order of the local atom position, the non-Gaussian parameter is calculated by the fourth order of the particle's position. It is defined as

$$\alpha_2(t) = \frac{3\left\langle\sum_i^N \left[\mathbf{r}_i(t) - \mathbf{r}_i(0)\right]^4\right\rangle}{5\left\langle\sum_i^N \left[\mathbf{r}_i(t) - \mathbf{r}_i(0)\right]^2\right\rangle^2} - 1.$$
(8)

Here *N* is the number of atoms in the system. For Brownian motion, the atomic displacement follows Gaussian distribution. The non-Gaussian parameter therefore characterizes the degree of deviation from the Gaussian distribution of particle motion. Thus $\alpha_2(t) = 0$ for Brownian motion. For the present metallic glass, the distribution of atomic displacements becomes non-Gaussian at intermediate times as shown in Fig. 6(c). This is due to the development of balance between the mobile and immobile atoms in the system. Therefore $\alpha_2(t)$ is always positive at any time. The maximum value of $\alpha_2(t)$ measures the heterogeneity of diffusion, and the time when $\alpha_2^{\text{max}}(t)$ appeared indicates the duration of heterogeneity establishment.

3. Self-intermediate scattering function and the α -relaxation time

To understand the feature of relaxation dynamics, we investigate the self-intermediate scattering function (SISF) and the α relaxation time of the present Cu₅₀Zr₅₀ metallic glass. The generalized form of SISF is defined as

$$F_{\rm s}(q,t) = \frac{1}{N} \sum_{l}^{N} \langle \exp\{-i\mathbf{q} \cdot [\mathbf{r}_{l}(t) - \mathbf{r}_{l}(0)]\} \rangle, \qquad (9)$$

where *N* is the number of atoms, **q** is the wave-vector corresponding to the main peak of the static structure factor S(q). In the present work, the wave-vector is chosen 2.7 Å⁻¹ as shown in Fig. 6(a). The evolution of SISF is similar to that of the diffusive MSD. Figure 6(d) shows the SISF of the whole Cu₅₀Zr₅₀ glass sample as a function of time. It shows a feature of two-step relaxation, i.e., the short-time β -relaxation and the long-time α -relaxation. The α -relaxation time τ_{α} is thereafter defined as the timescale when SISF decays to e^{-1} , as labeled by a horizontal dashed line in Fig. 6(d).

III. RESULTS

A. Framework of machine learning

Our goal is to develop a supervisory model, using the atomistically-informed machine learning, to simultaneously include the structural, thermodynamic, and dynamic aspects of the glass physics. Crucially the model should be capable of distinguishing "fertile" atoms that are responsible for the plastic rearrangements from those "sessile" atoms that are not.

Figure 7 shows the workflow illustrating the classification process via machine learning. The first step consists of collecting the dataset: we simulate a binary $Cu_{50}Zr_{50}$ system and 10 independent glass configurations are prepared by a rapid cooling method, with each sample containing 19 652 atoms. This composition has been shown to be the most challenging one for predictions of glassy and plastic behavior, owing to a lower degree of both structural and dynamic heterogeneity compared to other stoichiometries [48]. Therefore it provides an upper threshold for predictability. But this choice, on the other hand, represents the best ground to demonstrate the validity of the ML strategy. As shown in Fig. 7, there are three categories of the input features. First,



FIG. 7. Machine-learning encoding of the integrated glassy defect. A fingerprint vector of each atom— \mathbf{x}_i —is constructed from the combined configurational, thermodynamic, and dynamic spaces. Then, all the descriptors are trained by the SVM model, which classifies the atoms to be either structural defect or glassy matrix, with the nonaffine atomic strains as the supervisory signal.

the radial symmetry Gaussian functions and the two-body excess entropy are used to characterize the static structural features of each atom. These quantities naturally include both radial and structural-order information about the glassy structures. Second, the vMSD, or the Debye-Waller factor, at different temperature is utilized to characterize the thermodynamic fingerprints of each atom. Deviations from the harmonic approximation (higher-order thermal response) become prominent with increasing temperature. Third, a series of meaningful dynamic properties can be captured by the local topologies of the PEL. A series of activation energies provide information about steepness (or height) and multiplicity (or width) of the possible shear transformation pathways. A recent work [59] pointed out the importance of the PEL topology, and has included the arithmetic mean energy barrier as the supervisory signal of ML to predict β -relaxation in a metallic glass from purely static structure. In contrast, here we employ a hierarchically-sorted list of activation energies of possible structural excitations as the learning descriptors relevant to the topology of PEL. All together, we have built an abundant configurational-thermodynamic-dynamic phase space of glass for ML classification. The couplings between the different features have been considered. Specifically, we construct a dataset consisting of 56 structural (31 Gaussian functions and 25 two-body entropies), 20 thermodynamic, and 24 dynamic descriptors for each atom, respectively. Consequently, the feature vector reads $\mathbf{x}_i = \{x_i^1, \dots, x_i^M\}^T = \{G_i(r_1), \dots, G_i(r_{31}); S_{2,i}(r_1), \dots, S_{2,i}(r_{25}); \Delta r_i^2(T_1), \dots, \Delta r_i^2(T_{20}); \Delta Q_1, \dots, \Delta Q_{24}\}^T$ with M = 100.

To identify an essential structural rearrangement, AQS deformation [53] is conducted up to a global shear strain

magnitude of 0.05. We track possible STZ events by monitoring the instantaneous jump in the nonaffine displacement $D_{i,\min}^2$ [17], which plays the role of a supervisory signal in local plastic events. The next task is to select, at random, a subset of atoms as the training set and label the atoms with an index either $y_i = -1$ or 1. As shown in Fig. 3(b), an atom *i* is labeled as $y_i = 1$ if it rearranges within $\Delta D_{i,\min}^2$ is higher than 0.05 Å, and $y_i = -1$ if it does not. Approximately, 5% of all atoms have undergone structural rearrangements after AQS loading up to 5%. The training set is constructed by selecting all the atoms that have undergone rearrangements $(\sim 10\ 000\ \text{atoms})$, and an equal number of atoms that do not experience rearrangement in the first nine samples (among total ten samples). In this work, we train our machine-learning architecture using the support-vector machine (SVM) scheme, which builds a hyperplane in the multidimensional space to best separate the data points with different labels. Once this hyperplane is established for the training set, the tenth sample is treated as the testing set for calibration.

B. Predicting plastic atoms via machine learning

Figure 8 illustrates the capability of the proposed ML model in identifying whether an atom is susceptible to plastic rearrangement (or equivalently, belongs to flow defects) or not. Figure 8(a) visualizes the spatial distribution of the atoms that have undergone, or not, plastic rearrangements: among them, purple spheres mark the atoms that are predicted to act as defects by the ML model, while yellow spheres represent the atoms in the glassy matrix which remain inactive during the deformation. It implies that atoms identified as defects



FIG. 8. Prediction of athermal excitation. (a) Spatial distribution of the atoms that have undergone shear transformations, in which the purple ones are predicted as rearranged. (b) Contour map of ΔD_{\min}^2 in a slice of thickness 3.5 Å. White spots are ML predicted arranged ones. (c) The probability that an atom is predicted as active versus ΔD_{\min}^2 .

by the SVM model are very likely to participate in plastic deformation.

For the testing sample, the prediction accuracy is 78.4%; and the ML model captures 76.4% of the real rearrangements up to global shear strain magnitude of 5%. Figure 8(b) shows the contour map of the magnitude of the instant jumps in nonaffine displacement, ΔD_{\min}^2 , under AQS deformation. We notice that the distribution of ΔD_{\min}^2 is inhomogeneous— atoms with high ΔD_{\min}^2 tend to aggregate spatially into clusters, which are responsible for initiating the plastic shear transformations. For a direct comparison, white spots are superimposed to mark the positions of the atoms that are predicted as defects by ML model. The good overlap implies that the spatial distribution of the rearranged atoms is also heterogenous and, interestingly, almost coincides with the regions of high ΔD_{\min}^2 . This indicates that plastic rearrangements have a high propensity to originate from the plastically active regions predicted by the ML model. Figure 8(c) shows the probability of an atom will undergo plastic deformation, which goes up with increasing ΔD_{\min}^2 and saturates at a value of approximately 0.87 after $\Delta D_{\min}^2 = 0.1$ Å². This is meaningful since the more plastically active the atom is, the more likely it is to be predicted as glassy defect by the ML model.

C. Integrated glassy defect

The value of the integrated glassy defect—IGD that is a parameter assigned for the *i*th atom—is quantified by the decision value of the ML model. It distinguishes the glassy defects from the inert glassy matrix. This scalar value is proportional to the orthogonal distance between a given position in the input space and the hyperplane constructed by the ML model, with the same scale factor for all atoms. Notably, when IGD > 0, the corresponding data point in the input space lies on the glassy defect side of the hyperplane; and IGD < 0 otherwise.

Figure 9 shows the features of the IGD. Figure 9(a) is a 3D snapshot with atoms colored according to the magnitude of their IGD parameter value. We notice that the spatial distribution of IGD is heterogeneous with a strong spatial correlation. Figure 9(b) displays the probability distribution of IGD for the rearranged (red), nonrearranged (blue), and all atoms (black), respectively. There exists a two-peak feature in the total distribution, with the right peak denoting the defect atoms. The rearranging and nonrearranging atoms are separated fairly well in the IGD distribution. Compared with the nonrearranging atoms, the peak position of the rearranging atoms shifts to the right. This indicates that the machine-learned scalar parameter, IGD, is indeed an effective predictor of the atomic plastic rearrangements. It is indeed a physically-relevant measure of the degree of structural defect in glass. Besides, IGD is distributed over a very broad range, indicating strong structural heterogeneity as commonly observed in experimental characterizations [19], which also resembles the inhomogeneous distribution of the nonaffine displacements shown in Fig. 3(b). It should be noted that the distribution of IGD is different from that of softness in Ref. [44], the latter shows a symmetric distribution peaked at the origin. The broad distribution of IGD mainly comes from the additional input features beyond "softness." For example, vMSD usually exhibits some distributions with a Gaussian core and non-Gaussian tails [37]. Such non-Gaussian tail is usually the physical origin of the dynamic heterogeneity in glasses [60,61] and is the cause for the broad and asymmetric feature of distribution of IGD.

To measure the universal spatial distribution of IGD, we define a normalized spatial autocorrelation functions, C(r) =



FIG. 9. Features of the integrated glassy defect. (a) A 3D snapshot with particles colored by the magnitude of IGD. A small fraction of the atoms on the cubic corner was removed to see the inner atomic environement. (b) IGD distribution for different atoms. (c) Spatial autocorrelation function versus distance for ΔD_{\min}^2 and IGD.



FIG. 10. Partial RDFs for the group of atoms having the lowest 10% and the highest 10% IGD in a $Cu_{50}Zr_{50}$ metallic glass.

 $\frac{\langle \Delta P_{r_0} \Delta P_{r_0+r} \rangle - \langle \Delta P_{r_0} \rangle^2}{\langle \Delta P_{r_0}^2 \rangle - \langle \Delta P_{r_0} \rangle^2}, \text{ where } P \text{ represents a physical entity. The}$ angle brackets $\langle \cdots \rangle$ denote ensemble average. P_{r_0} and P_{r_0+r} are the values of P for the central atom at reference position r_0 , and the one at a distance of r from the reference atom, respectively. The operator Δ denotes the deviation from the ensemble average value. The calculated data for ΔD_{\min}^2 and IGD are plotted in Fig. 9(c). They both decay exponentially with respect to r. We adopt an empirical function $C(r) \propto$ $\exp(-r/\xi)$ to fit the correlation data, which brings about ξ as the physically spatial correlation length. The spatial correlation lengths for ΔD_{\min}^2 and IGD are almost identical, with $\xi_{\Delta D_{\min}^2} = 3.1 \text{ Å}$ and $\xi_{\text{IGD}} = 3.2 \text{ Å}$, respectively. This supports the validity of the IGD as a signature of plasticity. Both correlation lengths are approximately 1.2d, where d is the effective diameter of a single particle. Here d = 2.7 Å as determined from the position of the first peak in the RDF, which has been shown in Fig. 1. It indicates that the sweeping scale of IGD is consistent with the rearrangement size. The conclusion is consistent with a previous report from Cubuk et al. [8].

In Fig. 10, we compare the radial distribution functions (RDFs) of two extreme cases—the 10% atoms with the highest IGD values and those 10% with the lowest IGD values. It indicates that high-IGD atoms present a lower first peak which simultaneously moves to shorter distance compared with that of the low-IGD atoms. Thus the formers are alike the liquid atoms with high mobility.

D. Capacity of IGD in predicting athermal structural excitations

To get deeper insights into the correlation between IGD and the irreversible atomic rearrangements, we compare the spatial distribution of IGD with the nonaffine deformation field in Fig. 11(a). The white bubbles represent the atoms which have undergone shear transformations. The bubble size is proportional to the magnitude of ΔD_{\min}^2 . It is clearly seen that most of the shear transformations take place in the regions with high values of IGD. The machine-learned IGD thus identifies glassy defect with great propensity to undergo



FIG. 11. Capacity of IGD in predicting athermal shear transformations. (a) Contour map of IGD. White bubbles indicate the location of events, and the bubble size is proportional to ΔD_{\min}^2 . (b) Correlation between IGD and ΔD_{\min}^2 in the testing set. Each data point represents an average value of 0.25% of all atoms. The inset includes both training and testing set.

shear transformations. As such, the IGD could be regarded as a quantitative parameter to identify defect in glass, in analogy to the Burgers' vector in crystals. Note that not all high-IGD regions should experience plastic rearrangement, which is a stochastic phenomenon and sensitive to the loading protocol and thermal fluctuation [41,62]. It is the anisotropic interaction between the glassy defect and the high-dimensional loading direction that cooperatively determines if a glassy defect would lead to real shear transformation. As a result, the rationale for the structure-property relationship in an amorphous system is expected to be statistical. The statistics is shown in Fig. 11(b), with atomic-resolution ΔD_{\min}^2 being plotted against IGD. Each data point denotes a coarse graining of 0.25% of all atoms, with nearly \sim 50 atoms in each bin. There exists a strong correlation between IGD and ΔD_{\min}^2 . The atoms with higher values of IGD contribute more to the nonaffine deformation. This result is consistent for both the testing set shown in the main plot, and for the training plus testing set shown in the inset of Fig. 11(b). The agreement once again shows that there exists a robust correlation between the IGD parameter and the plastic deformation in glass.



FIG. 12. (a) The prediction accuracy of models with different input descriptors: excess entropy $S_{2,i}$, Gaussian structural function G_i , activation energy ΔQ_i , and vibrational mean-squared displacements vMSD. (b) Absolute value of the predictive power factor for IGD in comparison with the other four physical descriptors.

To demonstrate the efficiency of the integrated strategy in predicting plasticity of glass, we compare IGD with the existing individual physical models/parameters, each taking only one physical aspect (either configurational, thermodynamic, or dynamic) into account. Following the training and prediction protocol as mentioned above, models with only one of {vMSD, ΔQ , G and S_2 } as input descriptors are developed. As shown in Fig. 12, model prediction accuracy for the testing set differs largely with different input descriptors. The predicting accuracy for vMSD is 72.5%, followed by 64.2% for ΔQ , 61.5% for G, and 55.4% for S₂, respectively. Thus the thermodynamic feature is most relevant to structural excitation. Note that the predictor learned from only a family of Gaussian functions is exactly the definition of the "softness" metric [43]. Compared with the L-J model there, the Cu-Zr metallic glass described by the many-body EAM potential sets up an upper bound of difficulty for prediction via machine learning. The improved predictability demonstrated by IGD stresses the necessity of including extra thermodynamic and dynamic input for predicting the physical properties of generic, real, and complex structural materials.

It should be noted that the prediction accuracy here is not a superior indicator to evaluate the prediction power of plasticity of our simulation results. As there is only 5% of atoms in the testing set that are labeled as plastic ones, even an unintelligent model which predicts all atoms as nonrearranged ones will achieve 95% prediction accuracy in the testing set. To further quantify the predictive capability of metrics in assessing glassy plasticity, a power factor is further introduced as $\chi = \frac{P_R(X_i > X_{lop5\%})}{P_R(X_i < X_{low5\%})}$, as there is nearly 5% of all atoms are recognized as rearranged ones in our simulations. Here, X_i is the magnitude of the feature X for the particle *i*. $P_R(X_i > X_{top5\%})$ denotes the probability that a particle rearranges with X_i higher than the top 5% of all atoms, and $P_R(X_i < X_{1005\%})$ otherwise. Thus the predictive power factor is the ratio of the probability of rearrangements for the atoms with highest X_i with respect to that for atoms with the lowest X_i . It should be noted that this equation only suits for parameters $P_R(X_i)$ that monotonically increase with X_i . When $P_R(X_i)$ and X_i are inversely proportional or anticorrelated, χ is replaced by its reciprocal. The higher the magnitude of χ , the better the predictor X in discriminating between plastically active and inactive atoms.

The predictive power factor of different ML models is calculated and plotted in Fig. 12(b), where IGD shows the highest bar. It shows that IGD is superior to any other physical model in predicting plasticity. Even if the basic predictors are of poor predictive power when considered separately, once they are all integrated into IGD via the present ML protocol, the predictive powder does improve drastically. This observation implies that the structural, thermodynamic and dynamic descriptors are neither orthogonal nor absolutely correlated with each other. If they were absolutely correlated, there would be no room to improve the prediction power via integration and, thus, there would be no synergy when they are combined together. We also noticed that vMSD and ΔQ serve as the most important descriptors in the machine-learning process, while models with only structural features, i.e., G or S_2 , represent poor performance in predicting plasticity. It demonstrates the necessity of including extra thermodynamic and dynamic features as done in our ML process. The inclusion of the thermodynamic and dynamic components not only enhances the classification (since the prediction accuracy of ML model with all of vMSD, ΔQ , G, and S₂ is nearly 80%, as opposed to $\sim 60\%$ accuracy achieved by the scheme with only structural features), but also improves the predictive capability of plasticity in metallic glasses.

Our interpretation to this argument is in term of the spatial autocorrelation of the SVM models with different input descriptors, as shown in Fig. 13. It implies that predictors learned from structural features decreases very quickly with increasing distance. Indeed, it exhibits a decay length of only 1.9 Å for S_2 and 2.0 Å for G, which is much shorter than the size of atom rearrangement—3.1 Å as shown Fig. 9(c). This is presumably a possible explanation for the poor predictive capability of the purely structural function, which lacks information about medium- to long-range interactions. Besides, atomic structures vibrate under the influence of thermal fluctuations, therefore the definition of glassy defect from static structure might be not unique. In a real thermal glass, the relationship between structure and property is rather complex such that unstable phonon saddles are important, as



FIG. 13. Semi-logarithmic plot of the spatial autocorrelation function versus distance for the predictors learned from (a) vMSD, (b) ΔQ , (c) *G* and *S*₂, respectively. (d) The dashed lines are the best fits according to the empirical equation $C(r) \propto \exp(-r/\xi)$, defining correlation length ξ .

evidenced by the instantaneous normal mode analysis of the mechanical stability [63]. This is also the reason why the flexibility volume [37] instead of Voronoi volume correlates strongly with structural excitation owing to the fact that the former has crucially incorporated the thermodynamic Debye–Waller factor.

E. Transferability of IGD

The remaining question is whether the IGD—learned from supervised machine learning with athermal mechanical excitation as supervisory signal—can be transferred to predict also the thermal (or dynamic) properties of glasses. The latter properties are important for many applications and for routine material characterization. We test the IGD by correlating it with several important short-time and long-time properties that have not been considered at all in the ML protocol thus far. The dynamic properties include the vibrational boson peak, diffusion heterogeneity and the α relaxation, which are properties that span multiple time scales.

1. Correlating IGD with boson peak

First of all, we begin with the correlation between IGD and boson peak, the latter of which is a universal short-time vibrational anomaly—with extra soft modes over the Debye squared law—in a wide range of amorphous solids [24,64]. For this purpose, we calculate an atomistically resolved boson peak intensity in terms of the partial vibrational mode anomaly at atomic scale. The intensity of boson peak is represented by the peak value of the reduced vibrational density of states [VDOS, $g(\omega)$] for a single atom. As shown in the section methodology, the normal mode analysis is performed by directly diagonalizing the dynamical matrix (or Hessian matrix) of the system. Once the whole vibrational spectra are available, they are projected onto a single atom *i*, i.e., $g_i(\omega)$. Since the Debye model gives a quadratic distribution of the normal-



FIG. 14. Transferability of IGD in predicting dynamic properties of glass. (a) Reduced VDOS for the atoms with different values of IGD. (b) Correlation between the boson peak intensity and IGD. Each data point denotes the average value of 2.5% of all atoms. (c) Long-time diffusive MSD of atoms with different values of IGD at 700 K. (d) Non-Gaussian parameter corresponding to (c). Inset: α_2^{max} vs IGD. (e) Self-intermediate scattering function of atoms with different IGD. (f) α -relaxation time as a function of IGD.

mode frequency— $g(\omega) \propto \omega^2$, the single-particle intensity of boson peak can be derived as the height of the peak in the reduced VDOS over the Debye model $I_{\text{BP}} = \max[g_i(\omega)/\omega^2]$.

Figure 14(a) displays the reduced VDOS, $g_i(\omega)/\omega^2$, for the atoms with different mean values of IGD. As seen in Fig. 14(a), atoms with different values of IGD display different intensity of boson peaks. These boson peaks are arranged from the weakest to the strongest as IGD increases. It indicates that defects characterized by high value of IGD have lower tendency to participate in the high-frequency vibrations, thus giving rise to a relatively high intensity of boson peak at lower frequency. To further confirm the correlation, we directly plot the intensity of boson peak, IBP, versus IGD using a bin size of 500 atoms, which is nearly equal to 2.5% of all atoms in the testing sample. As shown in Fig. 14(b), a good linear correlation exists between IGD and $I_{\rm BP}$. Therefore IGD can be also used to predict the boson peak in glasses, with even better predictability than our earlier proposed purely structural metric-the short-range orientational order parameter defined as the longest vector from a central atom to its Voronoi polyhedron vertex [24].

2. Correlating IGD with diffusion heterogeneity

We can now consider how the IGD parameter correlates with the long-time diffusion dynamics. Here, the diffusive MSD is utilized to benchmark a direct link between IGD and the slow dynamics. Figure 14(c) depicts the diffusive MSD at 700 K for the atoms with different values of IGD. Obviously, the atoms with the highest IGD are these ones first escape from the caging plateau. In other words, they are the most active atoms that contribute to the diffusion dynamics. At the same time, the slowing down of dynamics for the low-IGD atoms is accompanied by an increasing dynamic heterogeneity, which is signaled by the rise of the non-Gaussian parameter α_2 with decreasing IGD, as shown in Fig. 14(d). Generally, the peak value of the non-Gaussian parameter, α_2^{max} , can be used to quantify the degree of dynamic heterogeneity. As seen in the inset of Fig. 14(d), we indeed find a strongly inverse correlation between the value of IGD and the magnitude of α_2^{max} . It actually reveals the liquid-like nature of the atoms with high value of IGD, and the solid-like nature of the low-IGD atoms. This is in agreement with the common sense that dynamic heterogeneity of a disordered material diminishes with increasing temperature upon crossing the glass-to-liquid transition [65,66]. Finally, α_2^{max} of the low-IGD atoms rises on a longer time-scale. This phenomenon means that the low-IGD atoms are in relatively deep glassy state, which takes a longer time to escape from the relatively deep basin of the β relaxation on the PEL.

3. Correlating IGD with the α relaxation

The other long-time dynamic feature to be examined is the slow relaxation behavior. To this end, we investigate the self-intermediate scattering function [SISF, $F_s(\mathbf{q}, t)$] of the atoms with different values of IGD. The results are shown in Fig. 14(e). It is evident that the relaxation dynamics slows down dramatically with decreasing value of IGD, represented by an extended plateau on the SISF curve, which corresponds to the secondary β -relaxation process. This trend indicates that motion of the low-IGD atoms is highly confined by the neighboring atoms, displaying a significant cage effect [67]. The revealed scenario for relaxation is consistent with that of diffusive MSD shown previously in Fig. 14(c), as both of them have the same origin in the local basin climbing process on the PEL.

In general, the characteristic timescale of the relaxation dynamics can be quantified by the α -relaxation time τ_{α} , which is defined as the time where SISF has decayed to e^{-1} , as marked by the horizontal dashed line in Fig. 14(e). The α -relaxation times for those atoms with different value of IGD are shown in Fig. 14(f). A very strong correlation is revealed between IGD and the α -relaxation time. Thus one can treat IGD as an effective indicator of the relaxation propensity at atomic scale.

In short sum, the newly developed IGD parameter proves highly versatile in being able to predict the short-time boson peak vibrational phenomenon, the long-time thermallyactivated diffusion and the α -relaxation dynamics. Surprisingly, these dynamic features have never been considered in the supervised machine learning model in which only athermal shear transformation is implemented as the supervisory signal. In this sense, the proposed concept of integrated glassy defect can serve as a generalized "superdefect," in analogy to the conventional crystalline imperfections—like vacancies, dislocations, grain boundaries etc.—to identify the carriers of plasticity in amorphous solids [14].

IV. CONCLUDING DISCUSSION

In conclusion, we identified a "superdefect"- termed IGD-to build possible structure-property relationship for the disordered materials by using extensive machine learning classification from a wide, intricate and partially entangled configurational-thermodynamic-dynamic space of data. IGD is glassy defect in the sense that the atom with high value of IGD has the highest propensity to undergo plastic shear transformation under athermal mechanical perturbations. As a step beyond the usual purely static structural descriptors, the present machine-learned IGD incorporates also thermodynamic and dynamical features characterized by the vibrational excitations and the thermal-activation events from probing the morphology of local potential energy landscape. Information from a single physical input can only partially capture the nature of the plastic deformation. In the case of complex media, it is the synergistic cooperation of both structural and thermodynamic-dynamic fingerprints that jointly determines the properties.

The integrated defect also allows one to disentangle the respective roles of different sectors of the overall phase space in governing the properties of glasses. Amongst the versatile descriptors is the thermodynamic feature that is crucial for predicting (athermal) structural excitation in glasses, and also provides a physical foundation for the successes of the vibrational amplitude and the flexibility volume as effective signatures of glass dynamics. In addition to the plastic deformation, the IGD is also shown to be a quantitative metric for other important and general thermal properties, such as the short-time low-frequency vibrational anomaly—the intensity of boson peak, as well as the long-time α -relaxation and diffusion heterogeneity in amorphous alloys.

Our method relies on static structure, thermodynamics as well as dynamics of a group of atoms. Thus the methodology is applicable directly to other glass systems, where Gaussian functions, two-body excess entropy, vibrational mean-squared displacement as well as activation energies can be calculated at atomic scale. The "softness" with only Gaussian functions as input has been tested vastly in different systems, such Lennard-Jones (LJ) mixture, Oligomer as well as Granular materials, and all shows acceptable predicting capacity [8,43]. Here, the present strategy suggests that the combination of configurational-thermodynamic-dynamic features can construct comprehensive atomic environment and yield a powerful predictability of IGD. Thus one can reliably infer that the IGD will perform as well for other disordered systems since the real-atom CuZr system always represents an upper bound of prediction for the property of glasses [48].

The proposed concept of IGD opens up new opportunities to optimize the physical properties of disordered materials by modulating the material processing conditions, besides the straightforward chemical-design of material structure.

ACKNOWLEDGMENTS

This work is financially supported by the National Key Research and Development Program of China (Grant No.

- 2017YFB0701502), the National Natural Science Foundation of China (Grant No. 12072344), and the Youth Innovation Promotion Association of Chinese Academy of Sciences (Grant No. 2017025).
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